

# **Characterizing Cloud Distributions as Functional Forms for QUICR: Uncertainties due to Fitting Techniques and Shattered Artifacts**

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**4 November 2013  
QUICR Breakout Session**

# Issues for QUICR

- QUICR requires in-situ data on  $N(D)$ ,  $IWC$ ,  $\beta$ ,  $N_T$  and functional fits for  $N(D)$  for developing & evaluating retrieval algorithms

# Issues for QUICR

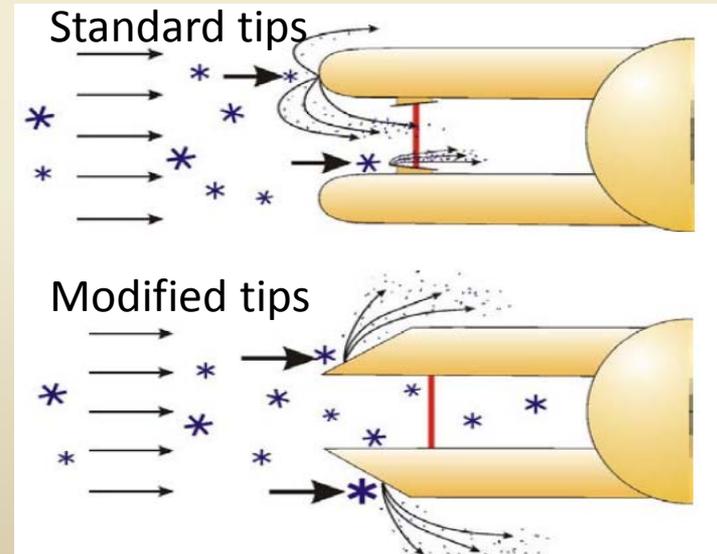
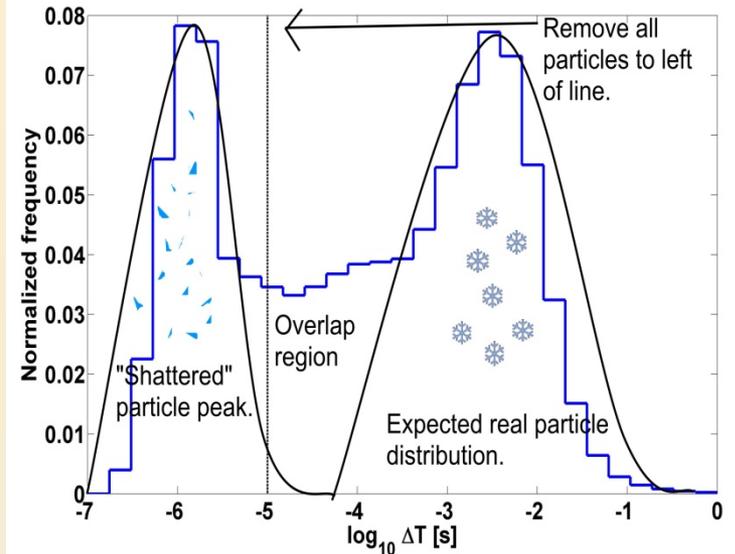
- QUICR requires in-situ data on  $N(D)$ ,  $IWC$ ,  $\beta$ ,  $N_T$  and functional fits for  $N(D)$  for developing & evaluating retrieval algorithms
- What is uncertainty on these bulk parameters induced by shattering of large ice crystals on inlets & tips of in-situ probes?

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- QUICR requires in-situ data on  $N(D)$ ,  $IWC$ ,  $\beta$ ,  $N_T$  and functional fits for  $N(D)$  for developing & evaluating retrieval algorithms
- What is uncertainty on these bulk parameters induced by shattering of large ice crystals on inlets & tips of in-situ probes?
- What is uncertainty induced by fitting algorithms on derived gamma fit parameters characterizing size distributions?

# Effect of Shattering

- Ice crystal size distributions (SDs) from forward scattering and optical array probes (OAPs), like 2DC, may be biased by shattering
- Modified tips for OAPs & varying processing techniques based on particle interarrival distance (time) have been used to correct for artifacts



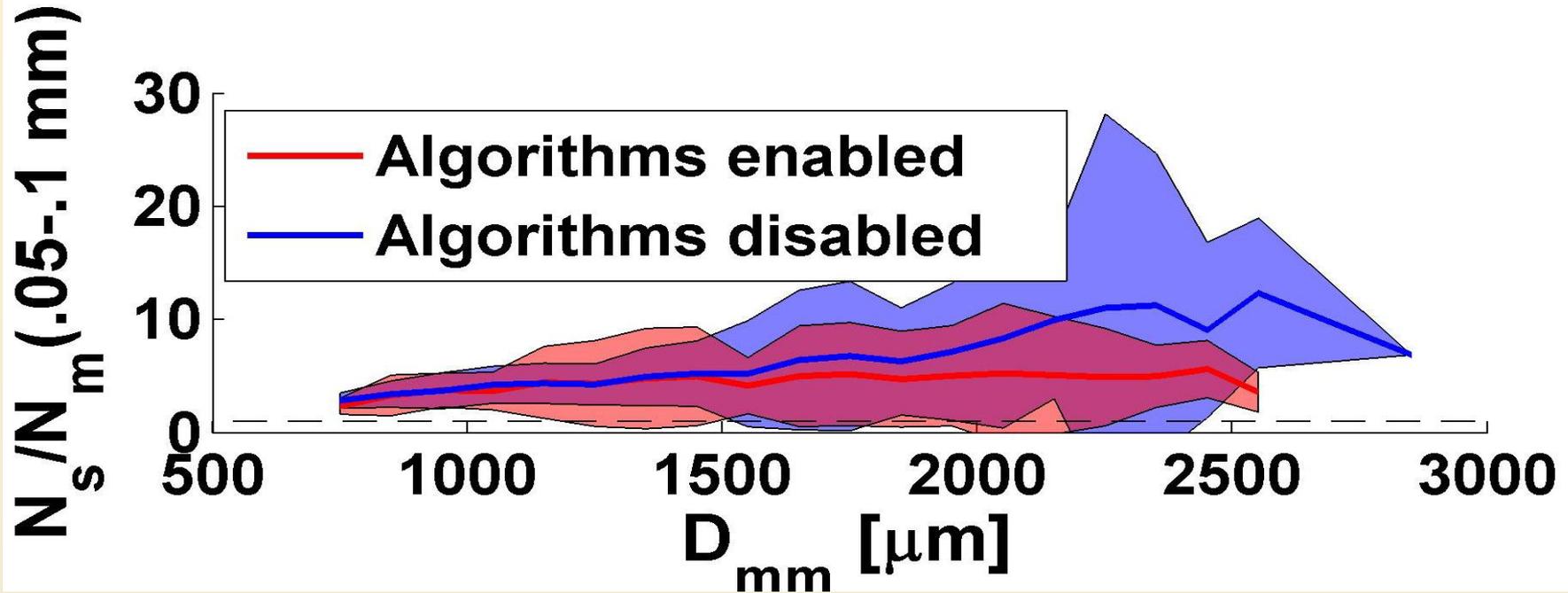
Korolev and Isaac (2006)

# Last Spring

- Showed data from 2 campaigns with co-located standard & modified 2DCs to investigate:
  - Identified conditions most conducive to shattering
  - Determined effect of shattering on bulk properties

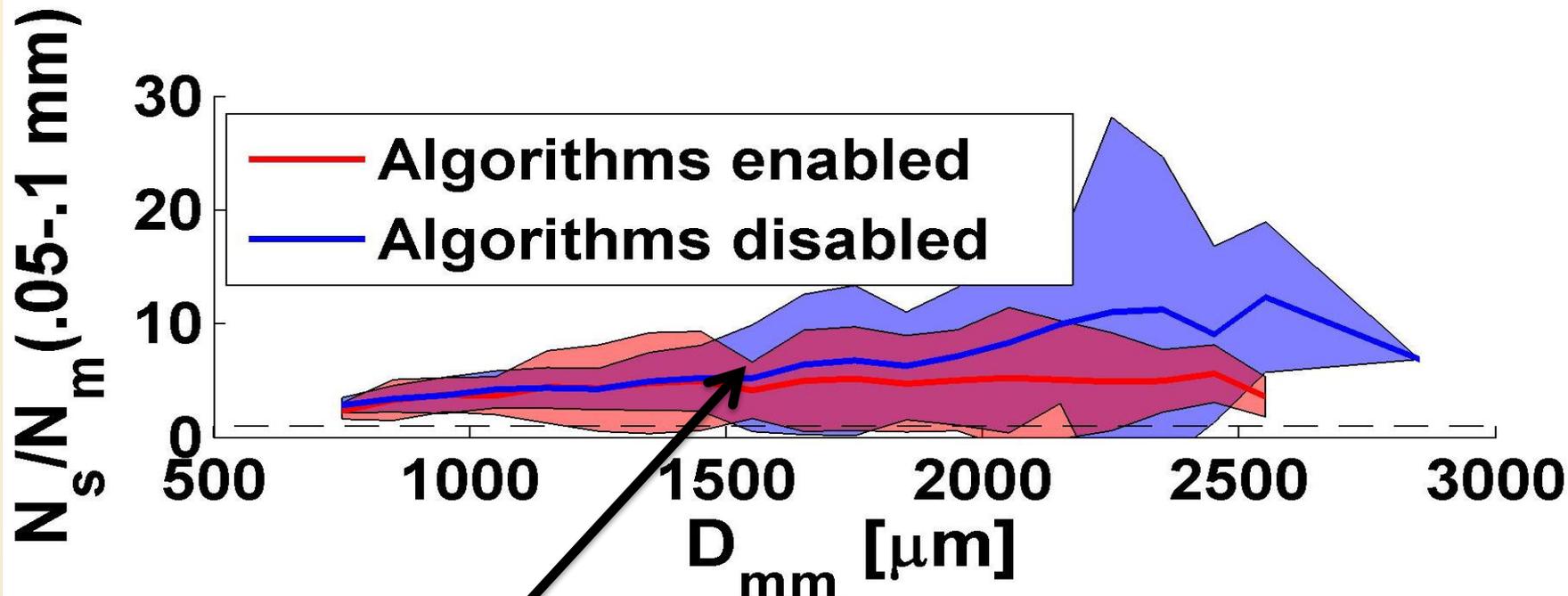
Campaign	Platform	Time + Location
Instrumentation Development and Education in Airborne Science phase-4 (IDEAS)	National Center for Atmospheric Research C-130	Research flight 3 (25 October) and 4 - 1 November 2011 near Cheyenne, WY
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# Compare Standard & Modified 2DC



Compare numbers of particles from standard tips ( $N_s$ ) with number of particles from modified tips ( $N_m$ ) from IDEAS

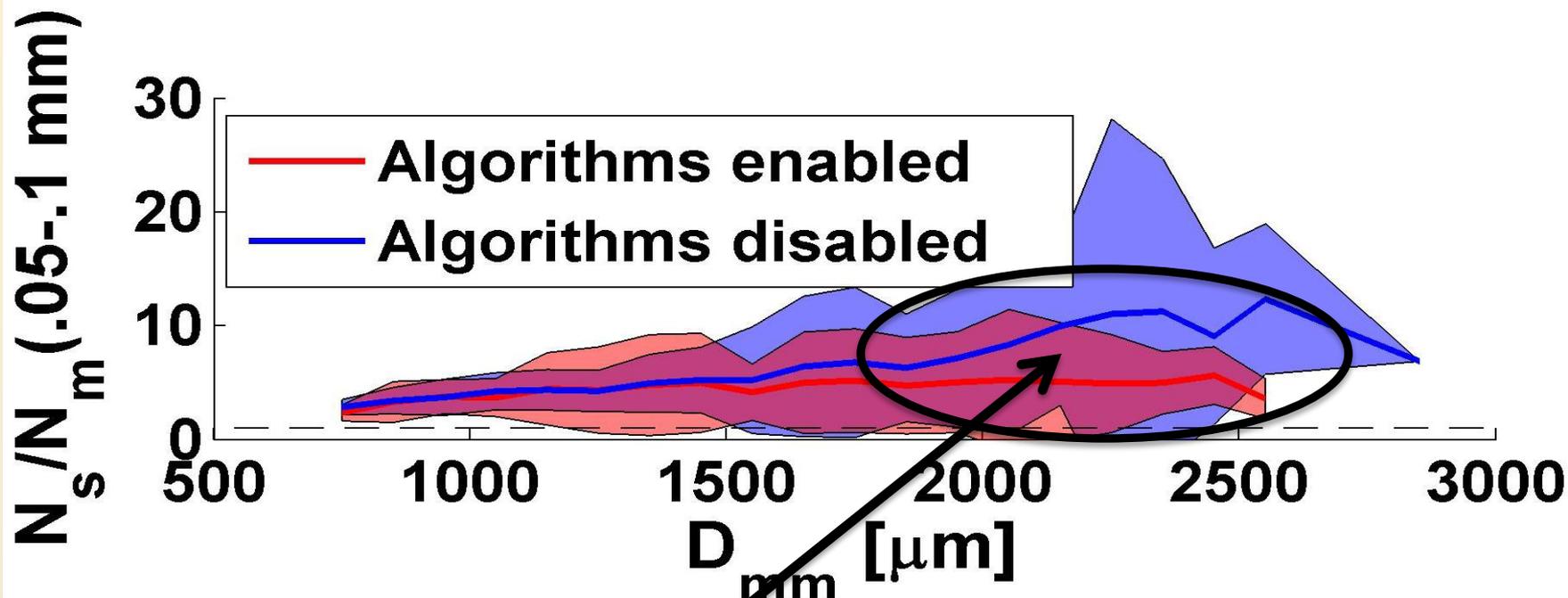
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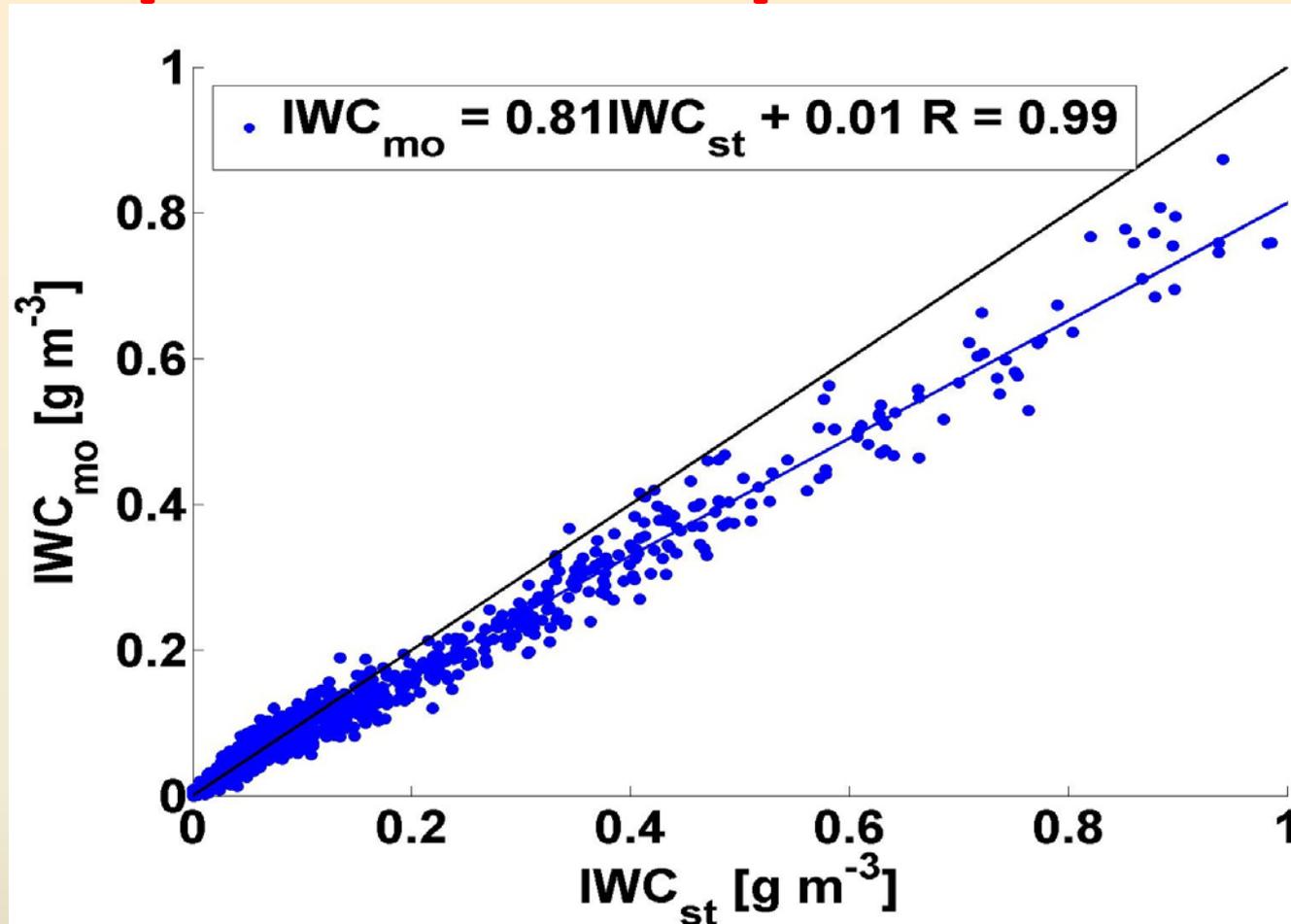


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Ratio of  $N_s/N_m$  increases with median mass diameter  $D_{mm}$

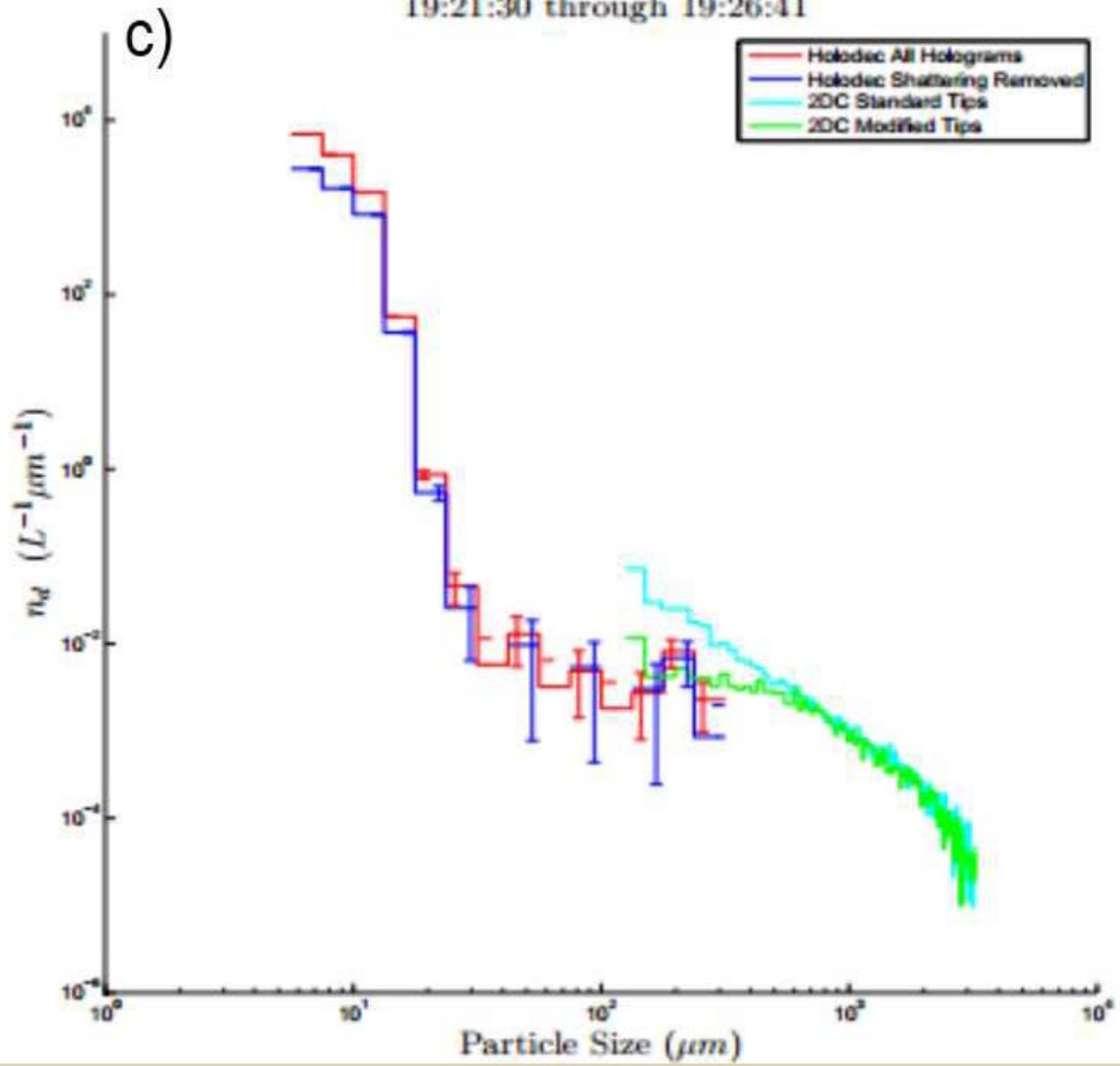
# Impact on bulk parameters



$IWC_{mo}$  vs.  $IWC_{st}$  for IDEAS+ISDAC shows ~20% difference, which is less than uncertainty in IWC due to m-D relation

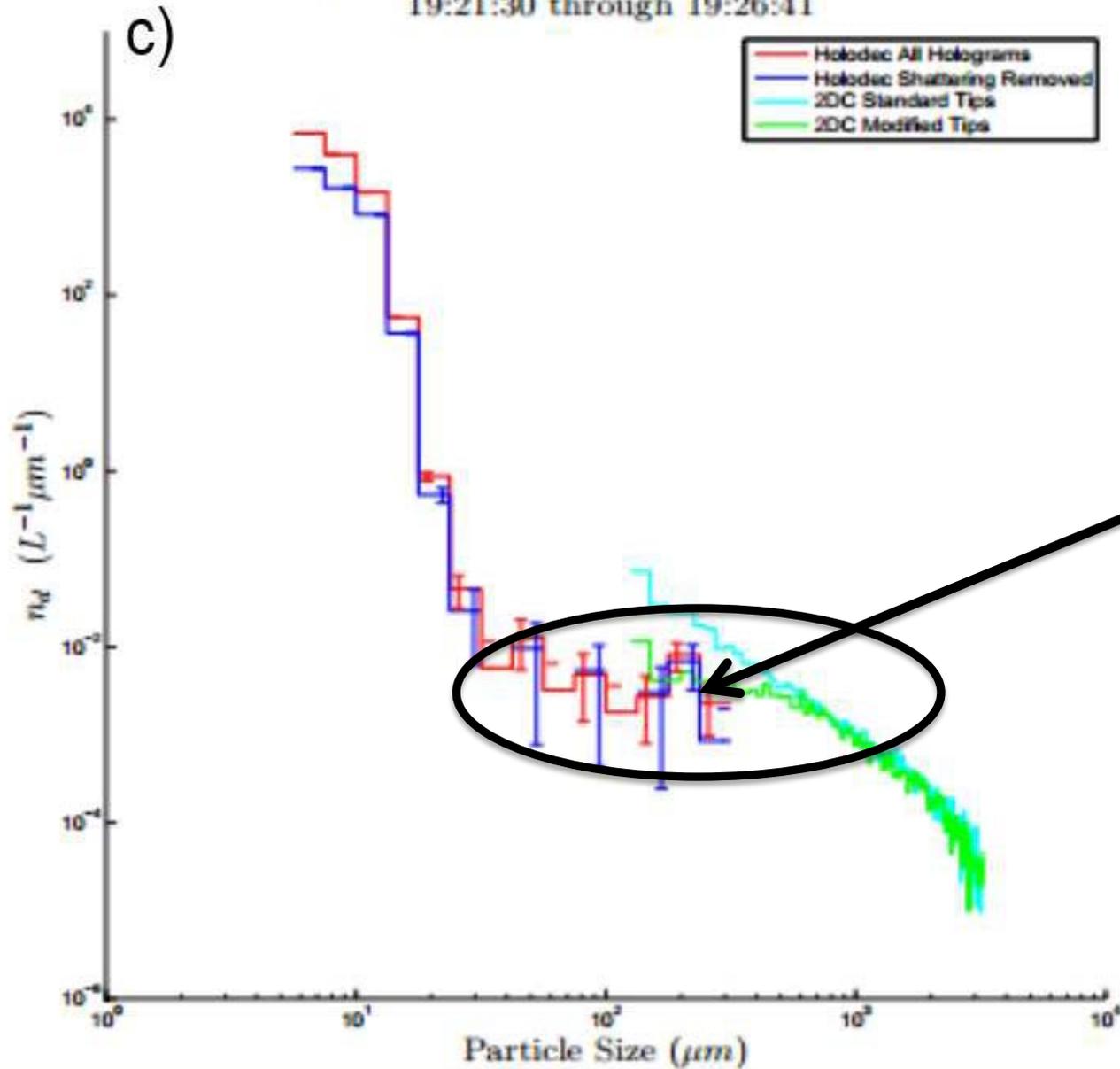
In-situ data provide reasonable IWC estimates

Average Size Distributions for Holoddec and 2DC  
19:21:30 through 19:26:41



**Comparison of  
2DC/ HOLODEC  
during IDEAS  
shows good  
agreement**

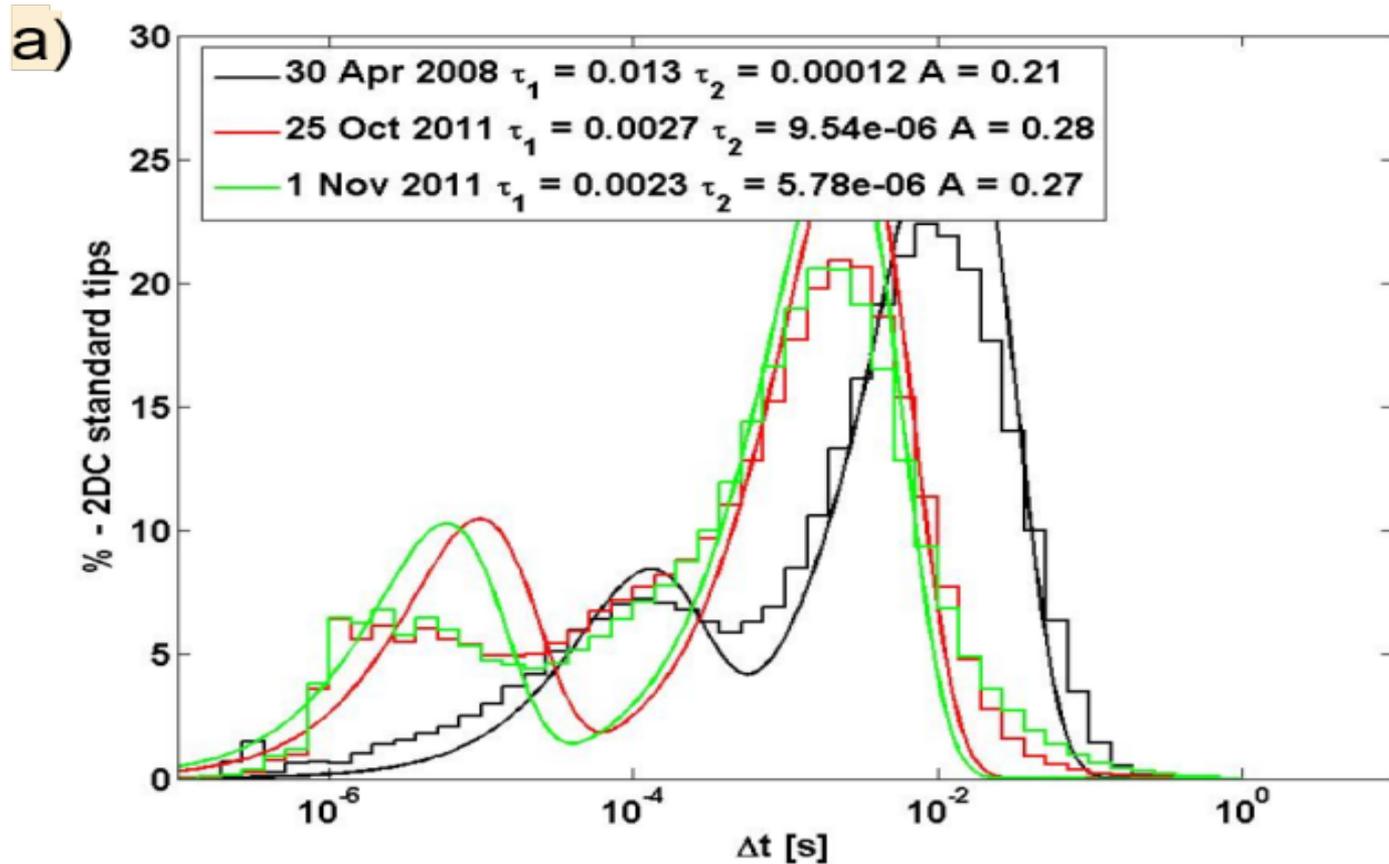
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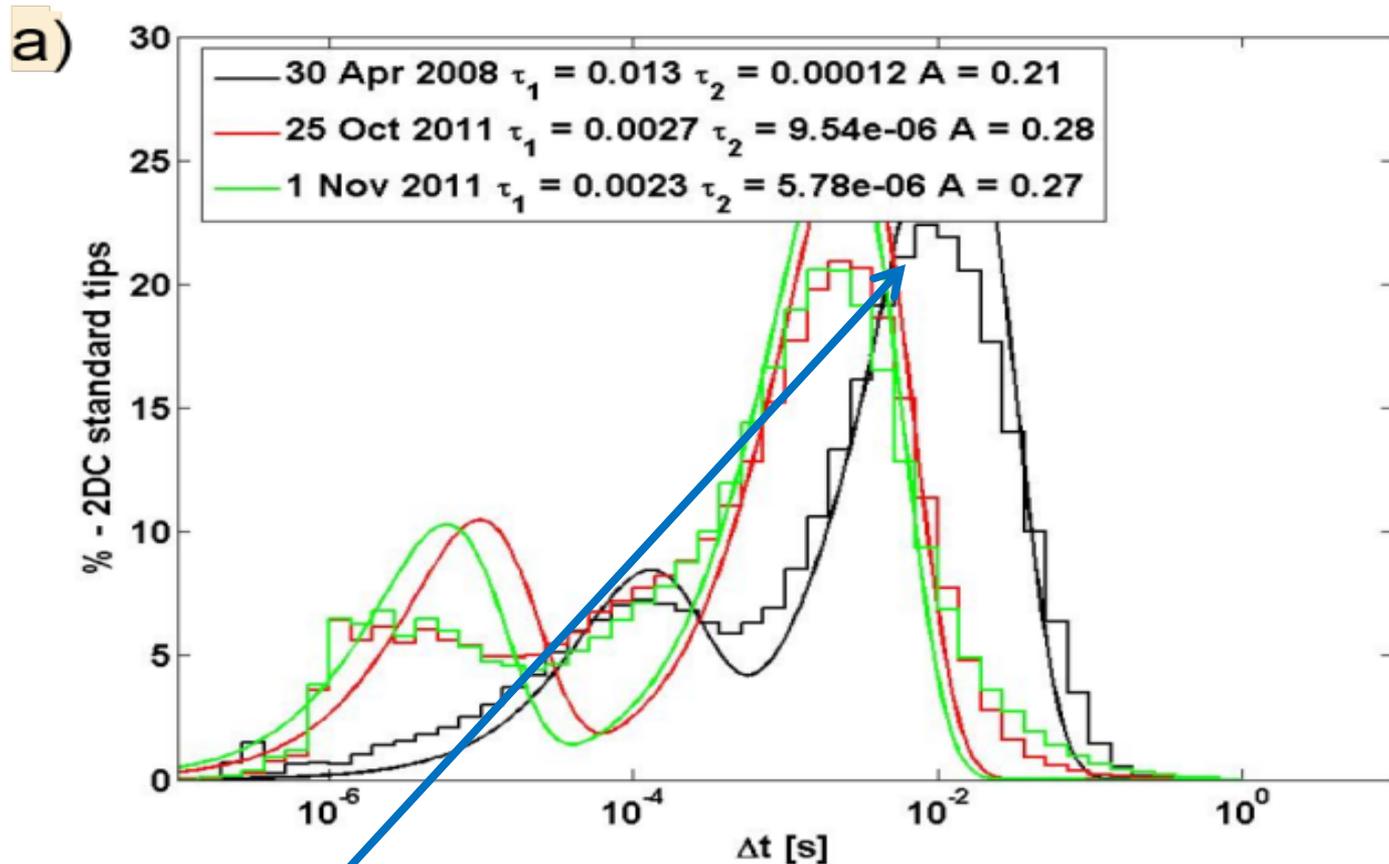
**→ Suggests  
algorithms +  
tips does  
reasonable job  
removing  
artifacts**

# Efforts to Understand Shattering



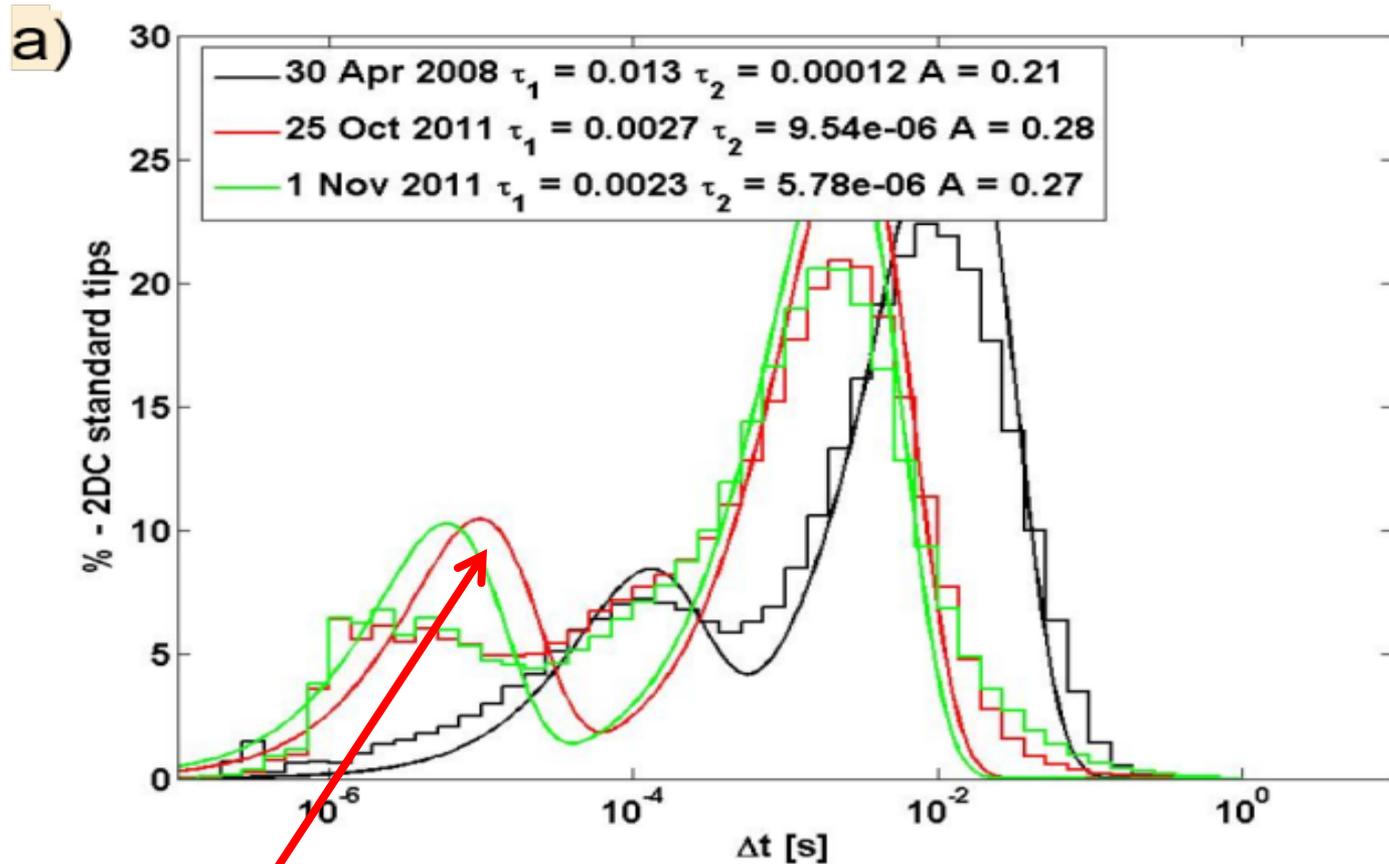
- Look at distribution of interarrival times on probe

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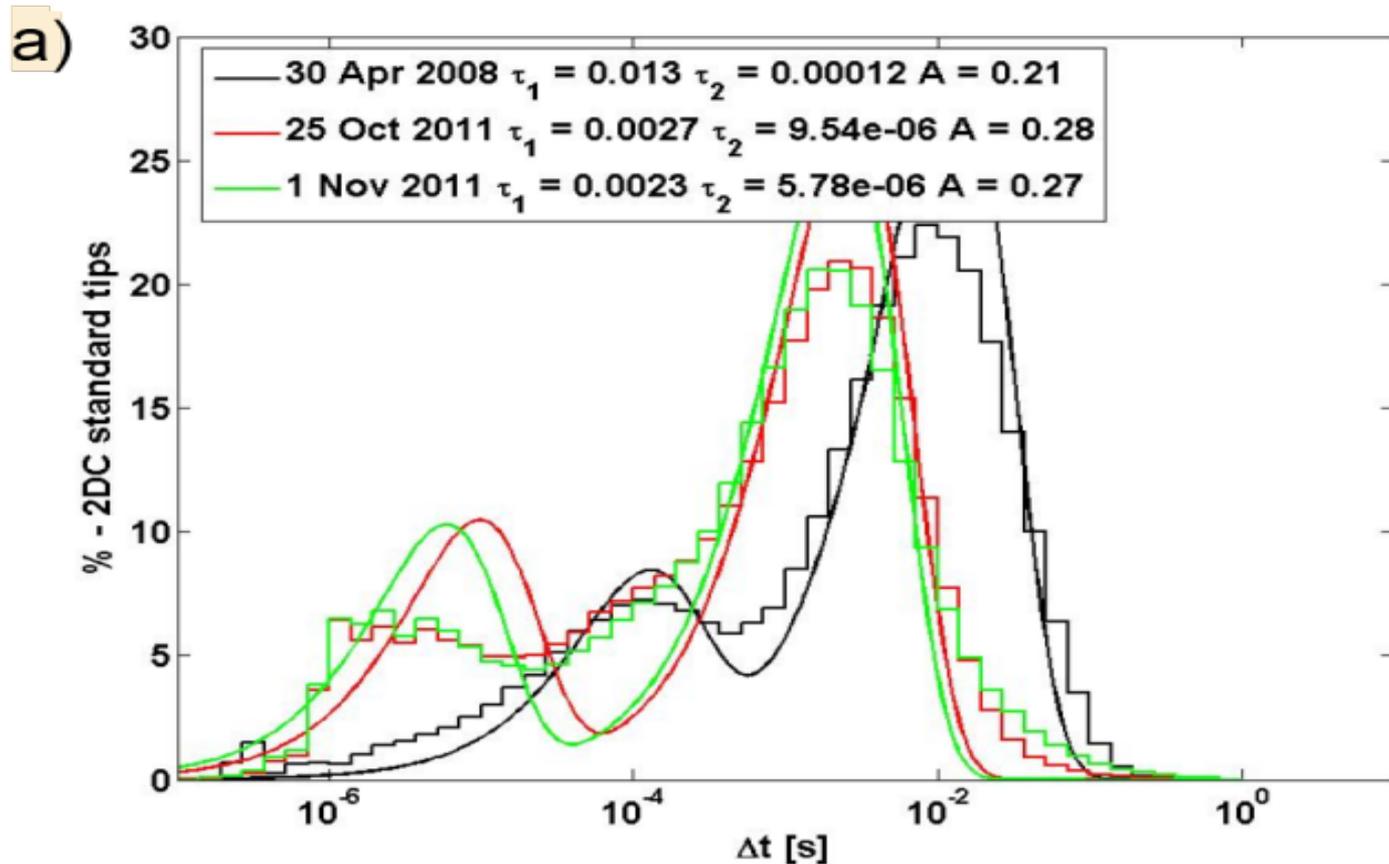
- Look at distribution of interarrival times on probe
- Larger interarrival times correspond to naturally occurring particles ( $\tau_1$ )

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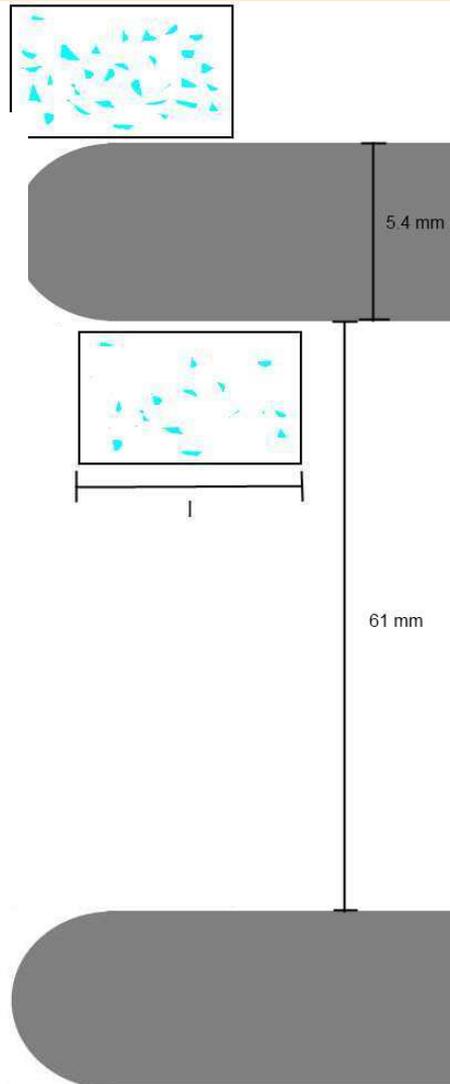
- Look at distribution of interarrival times on probe
- Smaller interarrival times correspond to shattered artifacts ( $\tau_2$ )

# Efforts to Understand Shattering



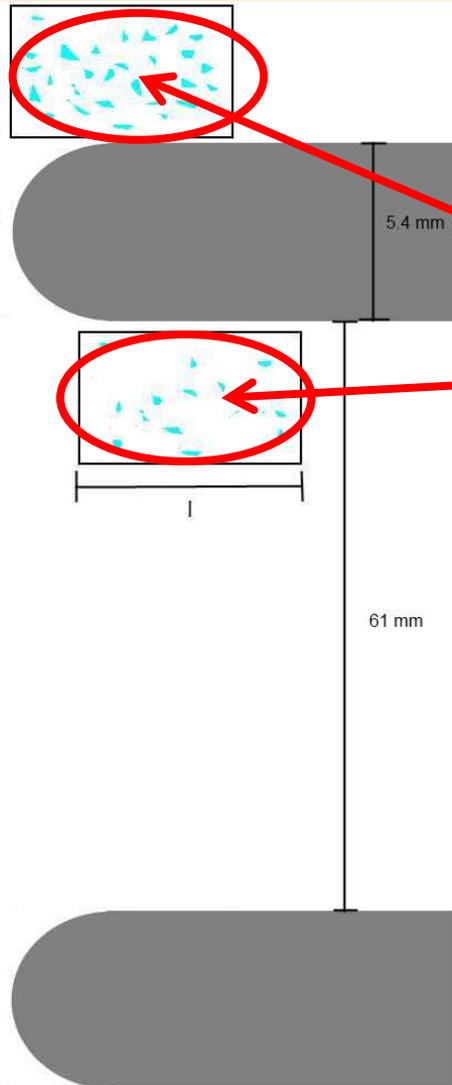
- Look at distribution of interarrival times on probe
- Why is there a difference in location of peaks between ISDAC/IDEAS?

# Modeling Shattering



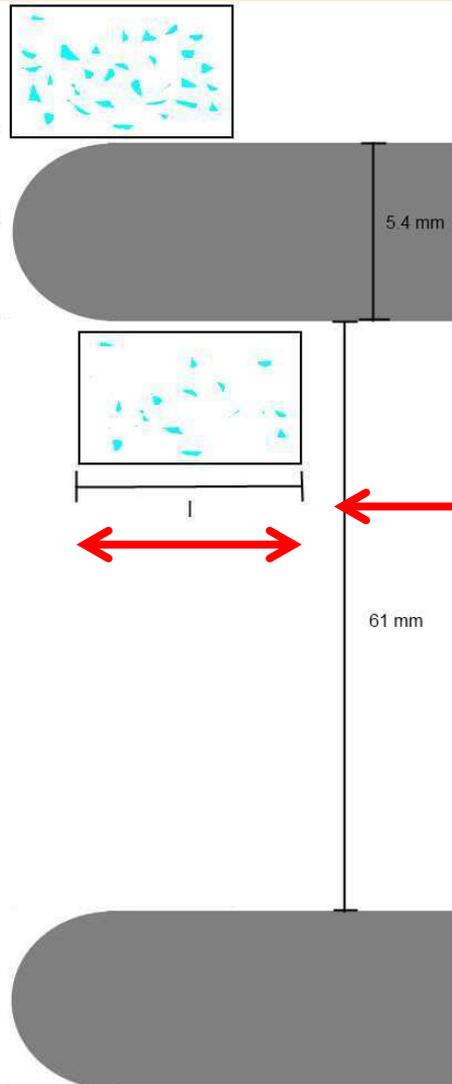
- Develop model to characterize shattering on probe tips

# Modeling Shattering



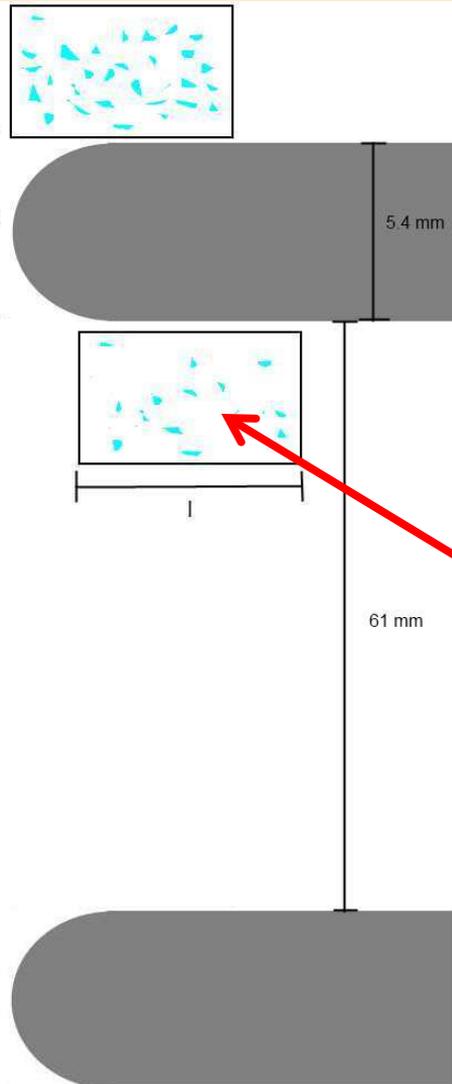
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  - Particles hitting tips shatter into fragments

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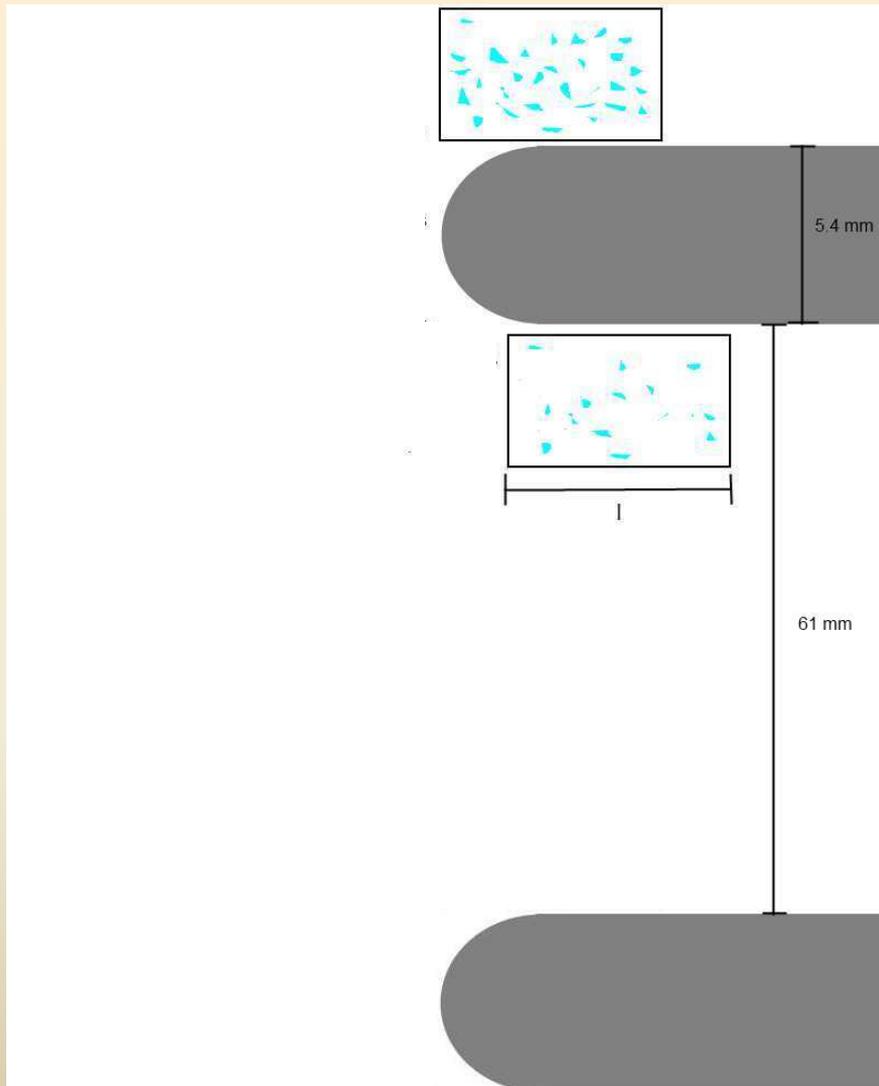
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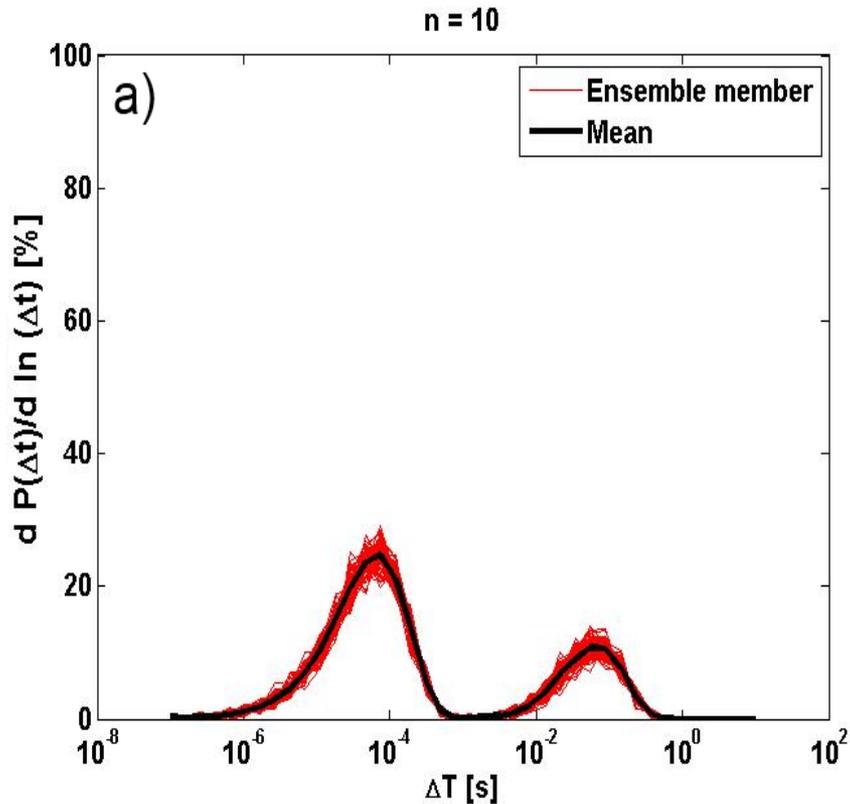
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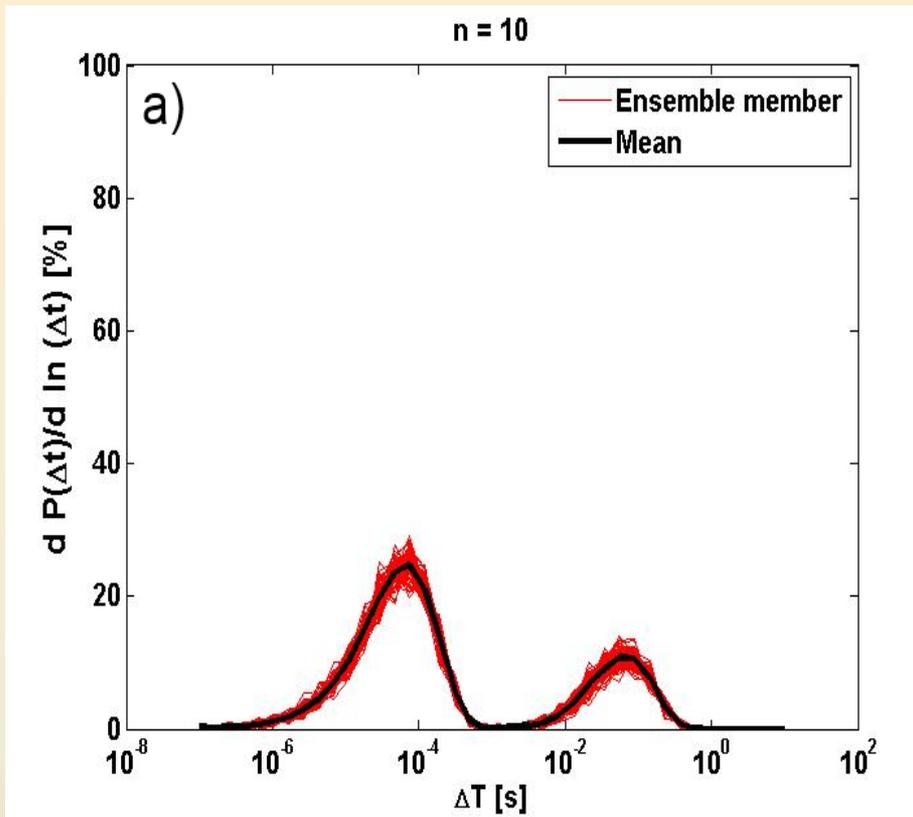
- **Develop model to characterize shattering on probe tips**
  - Particles hitting tips shatter into  $n$  fragments distributed by Poisson statistics across length  $l$  in direction of flight
  - Probability of single fragment entering sample volume is  $k$
- **Compute distribution of interarrival times for IDEAS/ISDAC using observed concentrations**

# Modeling Shattering



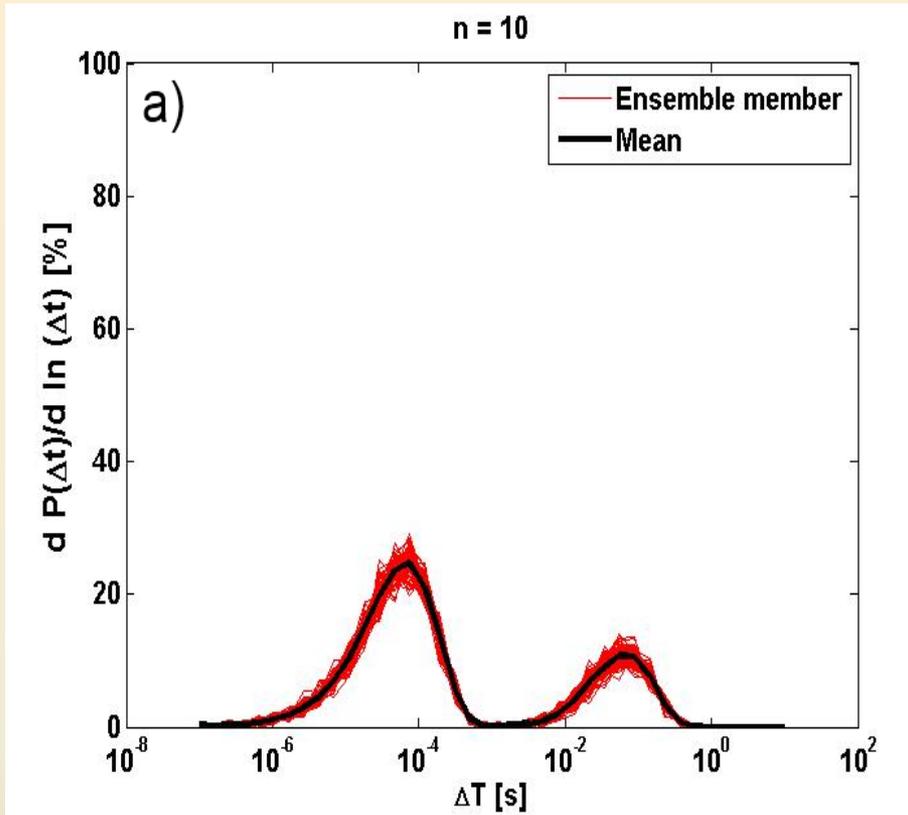
- Example of calculation for  $N=1 \text{ L}^{-1}$ ,  $n=10$ ,  $l = 1 \text{ cm}$ ,  $k=5\%$

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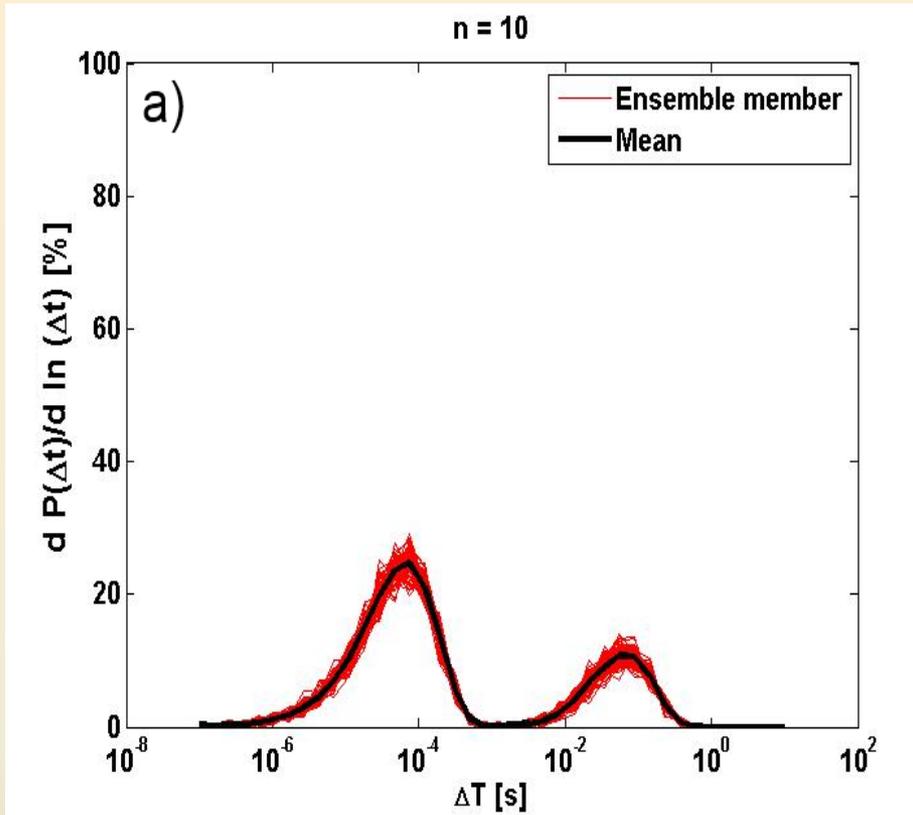
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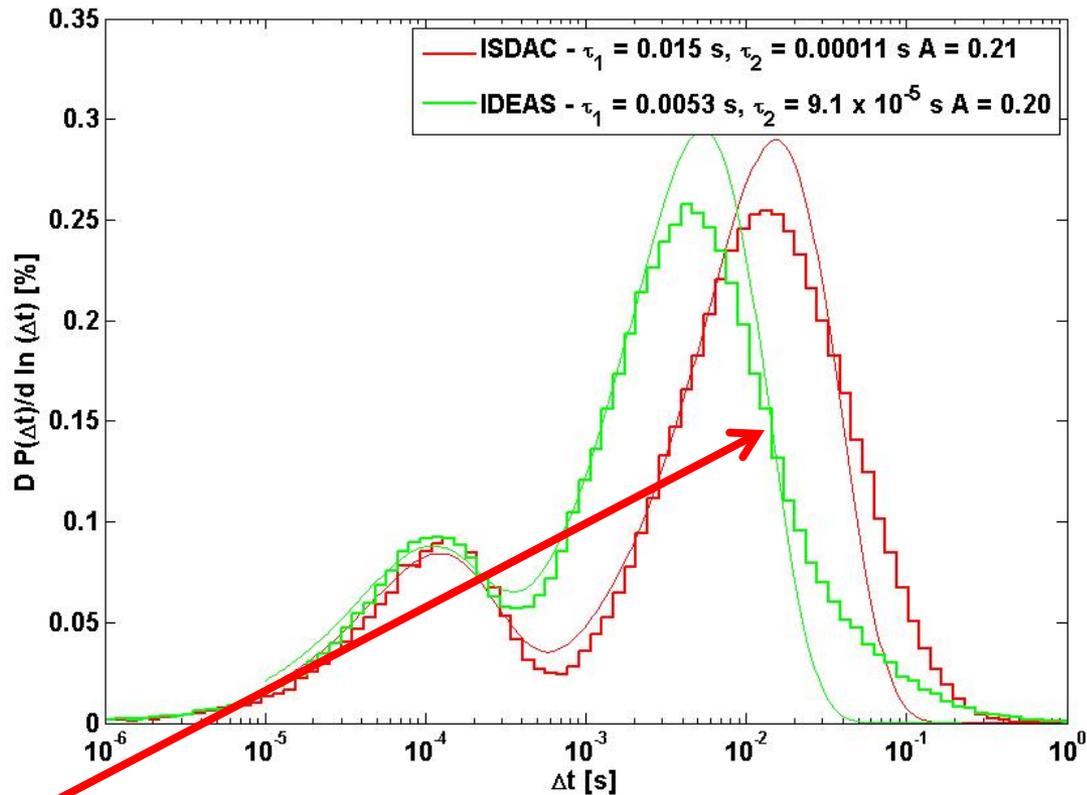
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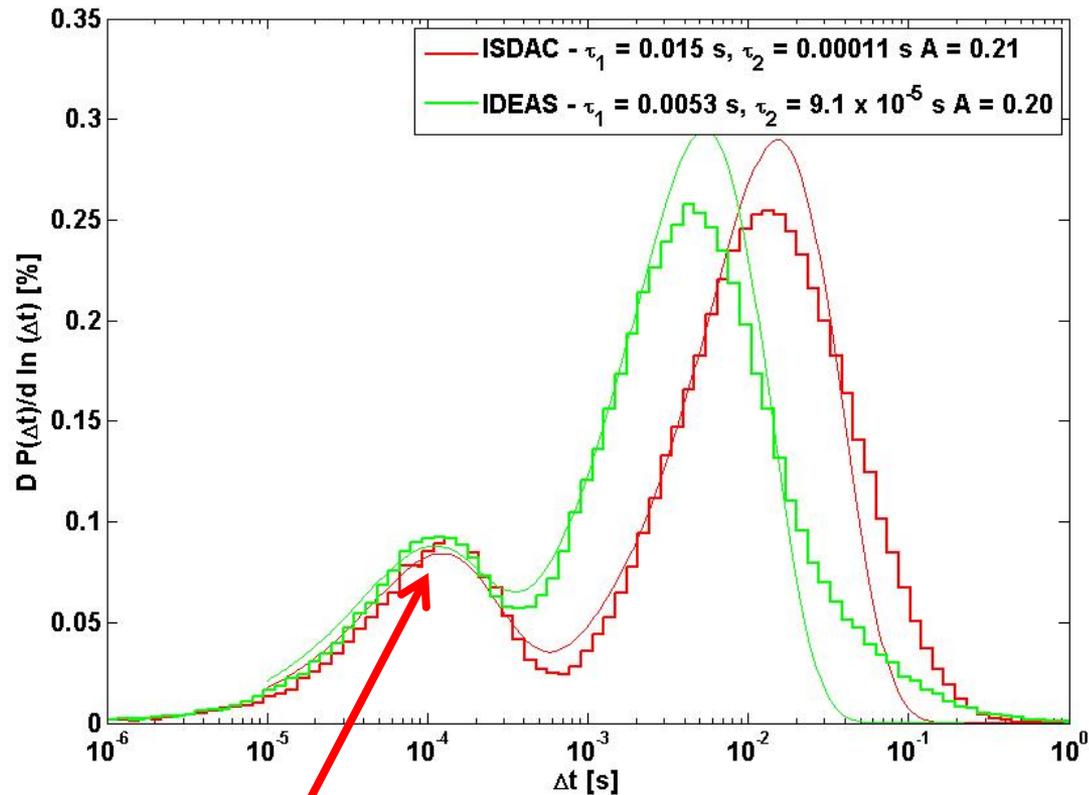
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- $\tau_1$  (natural particles) inversely correlated with  $N$ , TAS but not  $l$  or  $n$
- $\tau_2$  (artifacts) correlated with  $l$ , and inversely correlated with TAS,  $N$  and  $n$

# Simulation of ISDAC/IDEAS



- Location of natural mode differs due to varying concentration between project

# Simulation of ISDAC/IDEAS



- Location of natural mode differs due to varying concentration between project
- Location of shattered mode similar (but differed in observations): perhaps  $l$ ,  $k$  or  $n$  differed due to variations in characteristics of crystals

# Gamma Distribution:

*Mathematical Representation of Size Distributions*

$$N(D) = N_0 D^\mu \exp(-\lambda D)$$

- $N(D)$  = Number Distribution Function
- $N_0$  = intercept
- $\mu$  = shape
- $\lambda$  = slope

# Gamma Distribution:

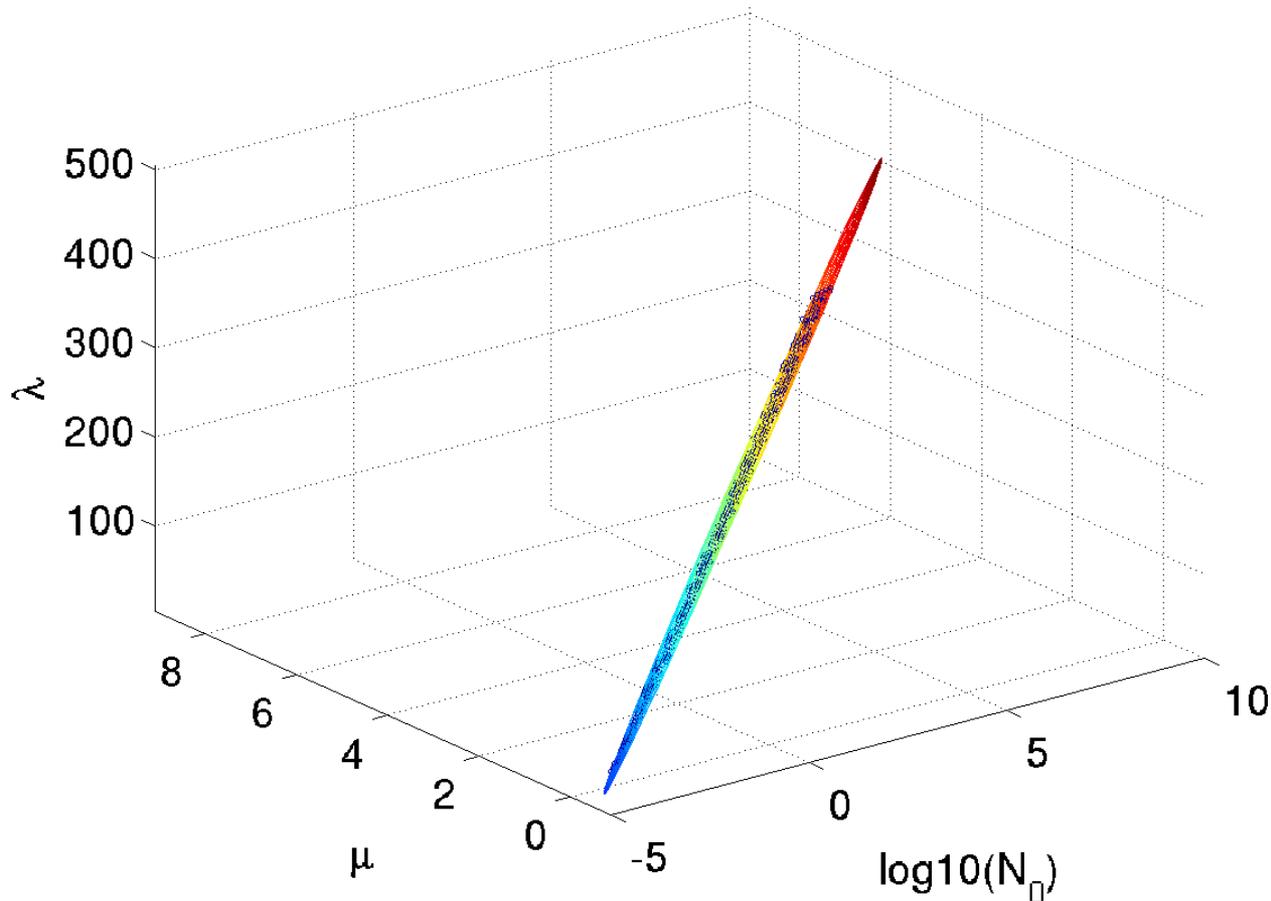
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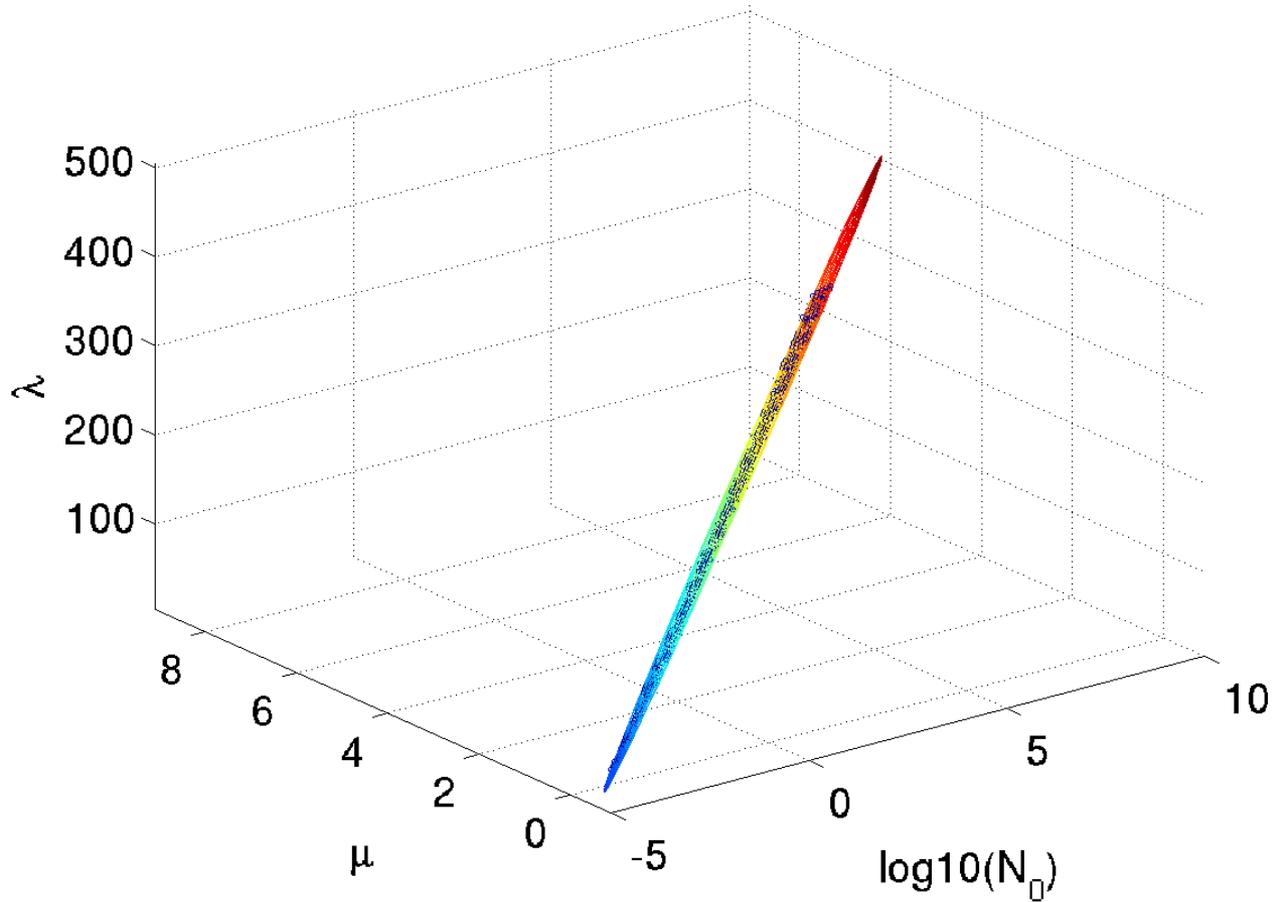
Have determined methodology for quantifying uncertainties in  $N_0$ ,  $\mu$ , and  $\lambda$  based on uncertainties in measured size distributions

## Ellipsoid Hull



- There is broad range of  $N_0/\mu/\lambda$  that fit SD well**
- Range determined by IGF technique that allows derived/observed moments to differ by  $\Delta\chi^2$**
  - Can't represent by single  $N_0/\mu/\lambda$  value**

## Ellipsoid Hull



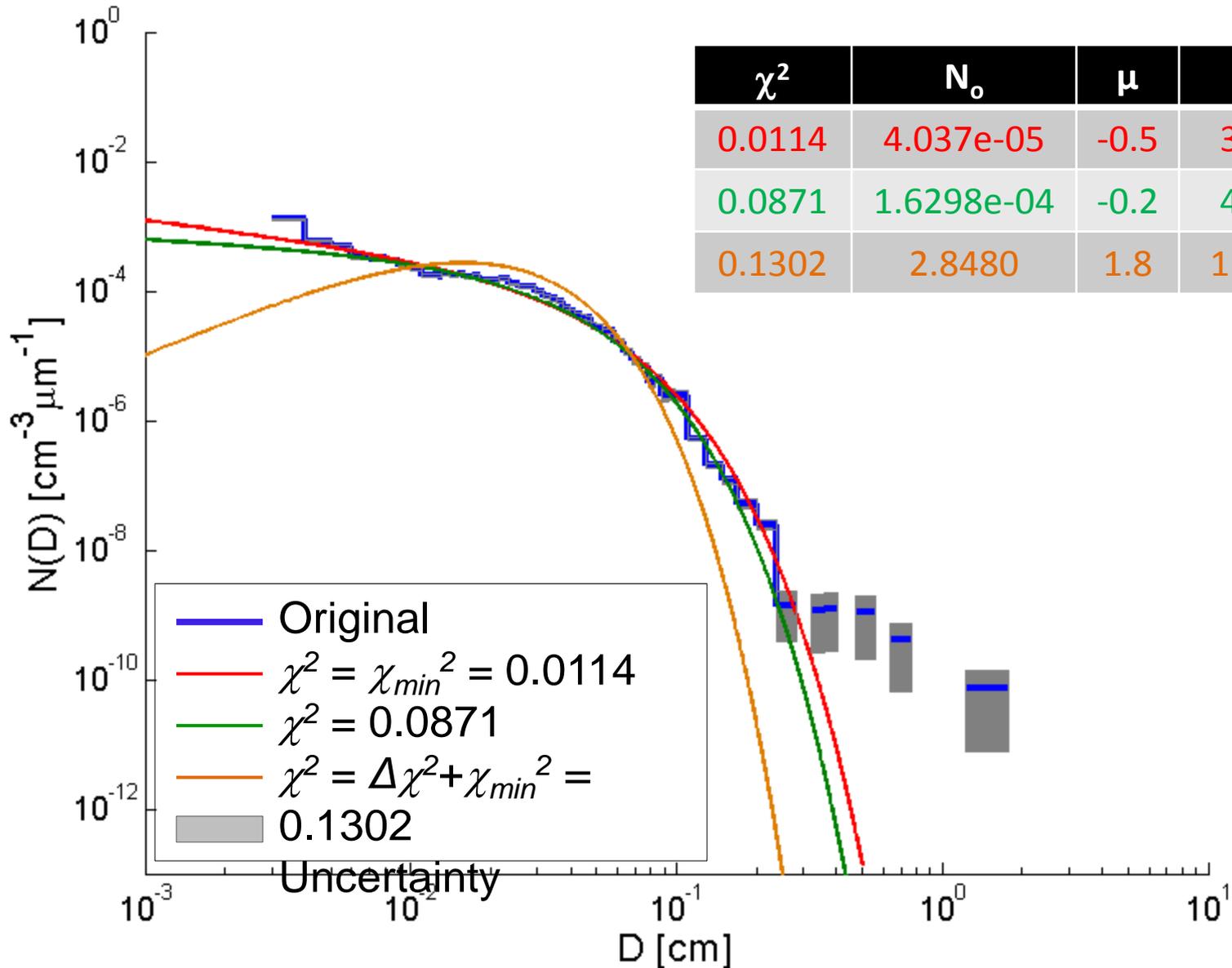
**But how big is  $\Delta\chi^2$ ?**

**$N_0/\mu/\lambda$  determined depend on tolerance allowed**

# Determination of $\Delta\chi^2$

- Uncertainty in measured SD determined by square root of # of particles in each bin, gives  $\Delta\chi^2$
- If  $\Delta\chi^2 < \chi_{min}^2$  for fit then  $\Delta\chi^2 = \chi_{min}^2$

# 1 SD Example: Aug. 20, Time: 170840



# Conclusions

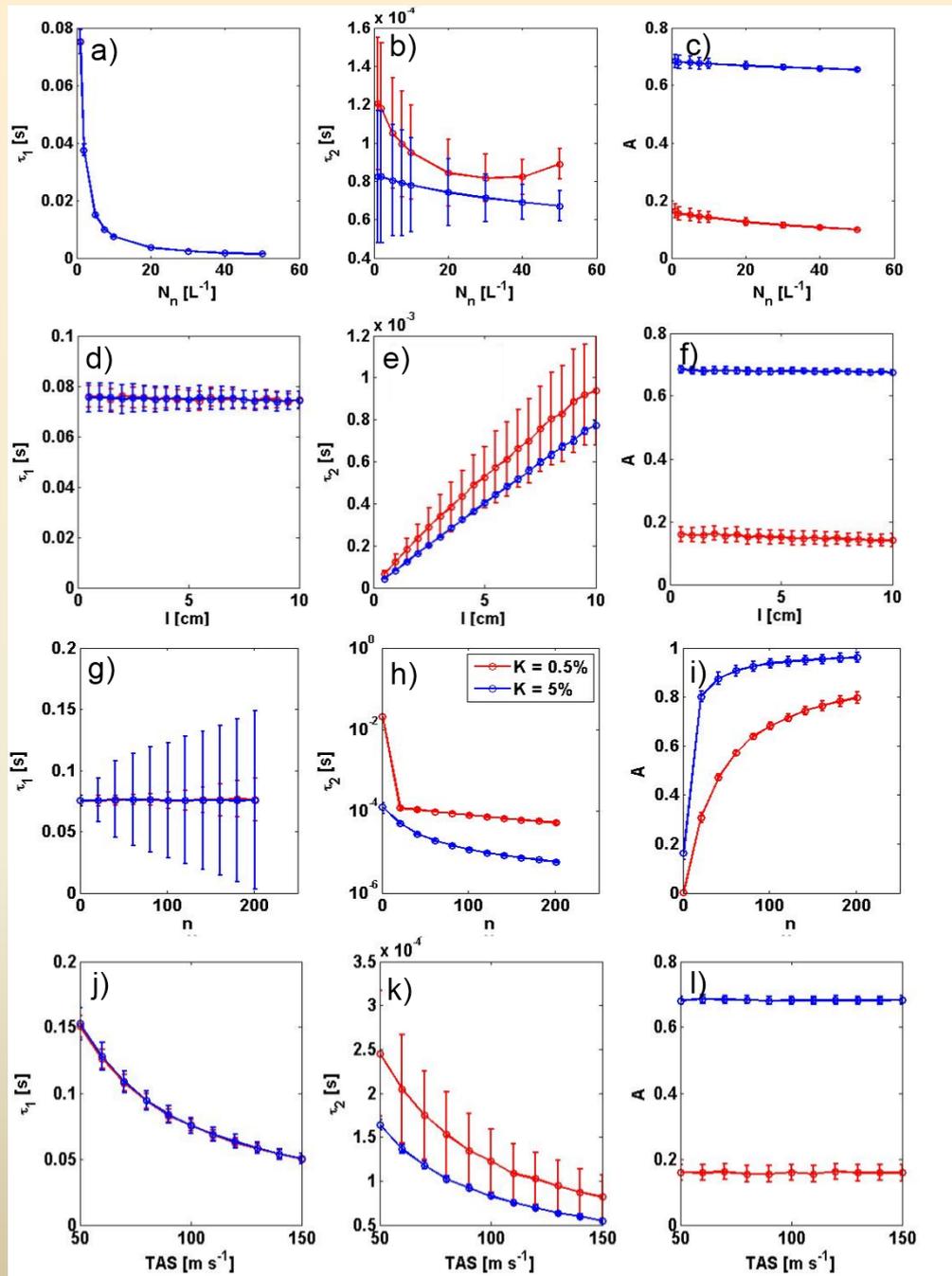
- **Modified tips & processing algorithms combined best mitigate existence of shattered particles**
- **Modified tips reduce  $\beta$ , IWC by  $\sim 20\%$ , no systematic bias in  $r_e$**
- **Theoretical model does reasonable job describing shattering, but still unclear on what basis of shattering depends on**
- **Quantitative basis for determining range of  $N_0$ ,  $\mu$ ,  $\lambda$  describing gamma fit distribution established**

# Next Steps

- **Conduct fits to SDs measured during past campaigns:**
  - Currently working on MC3E/SPARTICUS data
  - IGF can accommodate for missing crystal ranges due to shattering
- **QUICR ramifications:**
  - Level of uncertainty in bulk parameters different (determined on parameter by parameter basis)

# Determination of $\Delta\chi^2$

- Calculate uncertainty in each 10-s  $N(D)$  → create  $N(D)_{min}$  ( $N(D)_{max}$ ) from  $N - \sqrt{N}$  ( $N + \sqrt{N}$ )
- Compute 3 moments for each  $N(D)$  uncertainty
- Calculate  $\chi^2$  (comparing to moments of original  $N(D)$ ) for each uncertainty →  $\chi^2_{N(D)_{min}}$ ;  $\chi^2_{N(D)_{max}}$
- $\Delta\chi^2 =$  average of both  $\chi^2$
- If  $\Delta\chi^2 < \chi_{min}^2$  for fit then  $\Delta\chi^2 = \chi_{min}^2$



Investigated location of modes ( $\tau_1$ ,  $\tau_2$ ) and relative importance of different modes as function of input parameters

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- Showed data from 2 campaigns with co-located standard & modified 2DCs to investigate:
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1. Showed shattering increased with  $D_{mm}$  & amount of riming
2. Both modified tips & algorithms needed to remove artifacts
3. Tips more effective than algorithms for removing artifacts
4. Bulk IWC,  $b$  could be estimated within about 20%