



# Comprehensive, rapid cloud drop & ice crystal formation parameterizations: Developments and evaluations

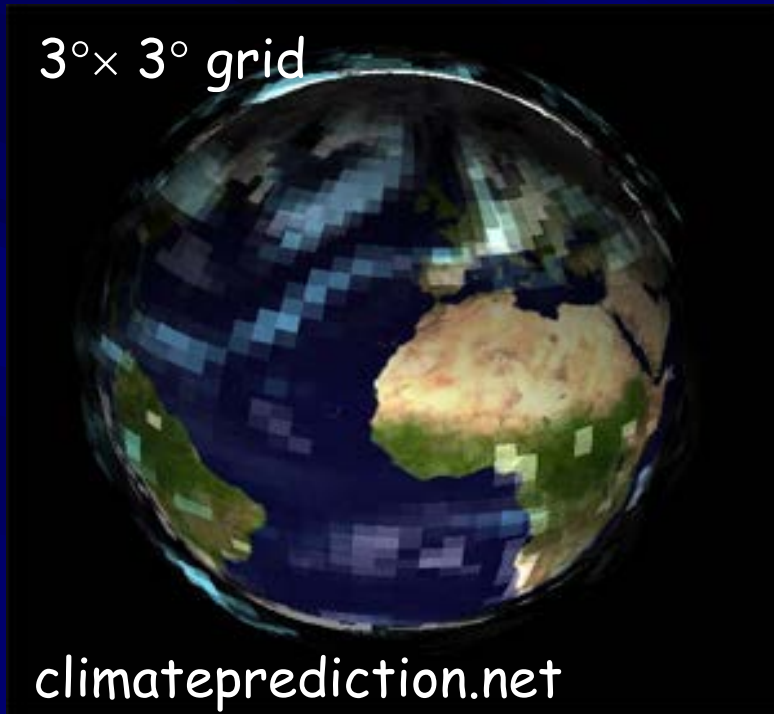
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DOE ASR Science Team Meeting  
San Antonio, Texas  
31 March 2011

**Acknowledgments: NASA, NSF, NOAA, ONR, CIRPAS  
Nenes group, Seinfeld/Flagan group (Caltech),  
Adams/Pandis group (CMU), University of Crete**

# Problems with GCM assessments of aerosol indirect effect



- Cloud formation happens at smaller spatial scales than global climate models can resolve.
- Aerosol-cloud interactions are complex.
- Climate models provide limited information about clouds and aerosols.
- Describing cloud formation explicitly in global models is VERY expensive. These calculations need to be simplified (“parameterized”).

# GCMs Need Fast Physics: Simple expressions capturing important cloud physics

**Goal:** Predict drop/ice number concentration in "characteristic" cloud types.

## Dynamics

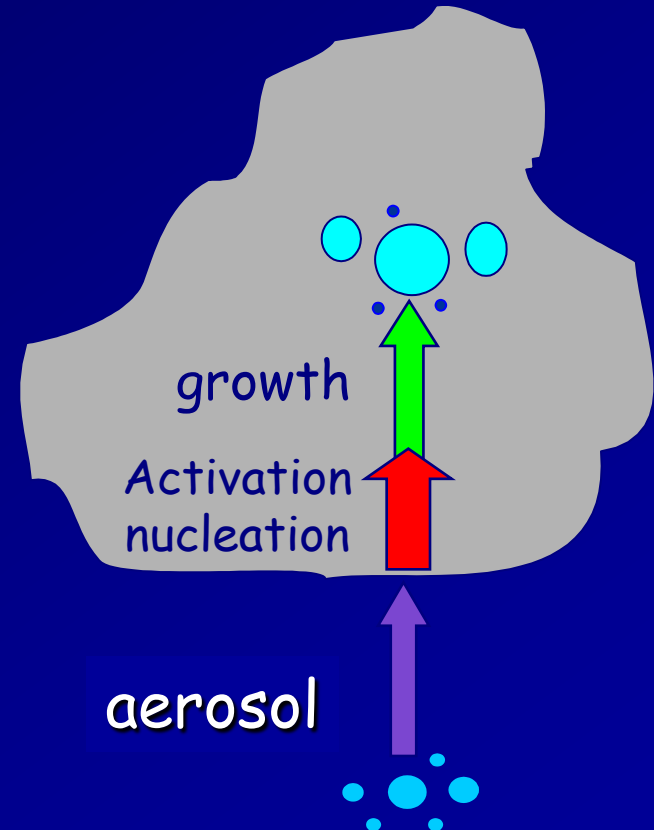
- **Updraft Velocity**
- Large Scale Thermodynamics

## Particle characteristics

- **Size & Concentration**
- **Chemical Composition**

## Cloud Processes

- **Cloud droplet formation**
- **Ice crystal formation**
- **Effects of entrainment/mixing**
- Collision/coalescence
- "Scaleup" of processes

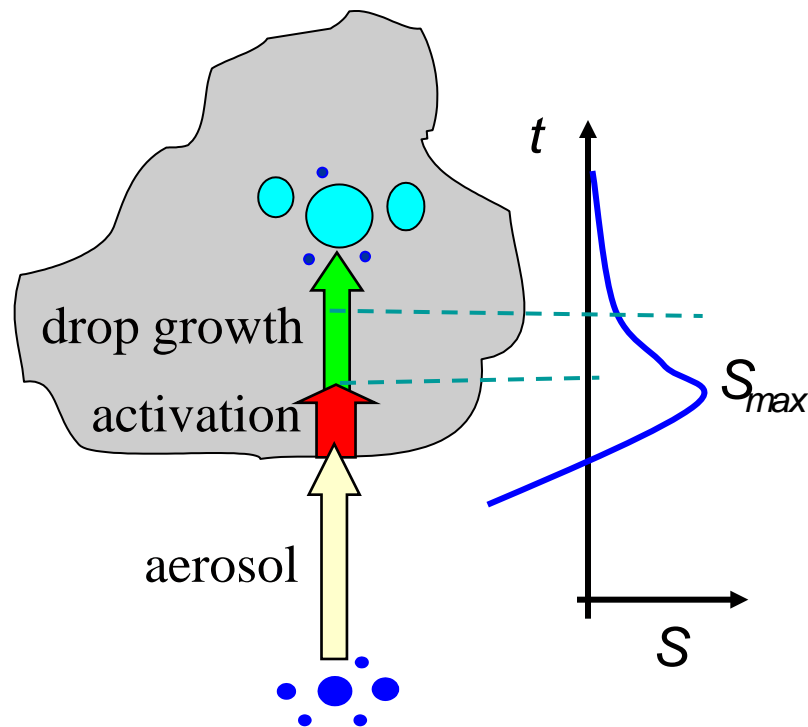


Links/feedbacks need to be incorporated (at appropriate scales).  
VERY challenging problem (Stevens and Feingold, 2009)

# Liquid Phase Clouds

**Approach:** use the “simple story” (1D parcel theory)

**Basic ideas:** Solve conservation laws for energy and the water vapor condensing on aerosol particles in cloudy updrafts.



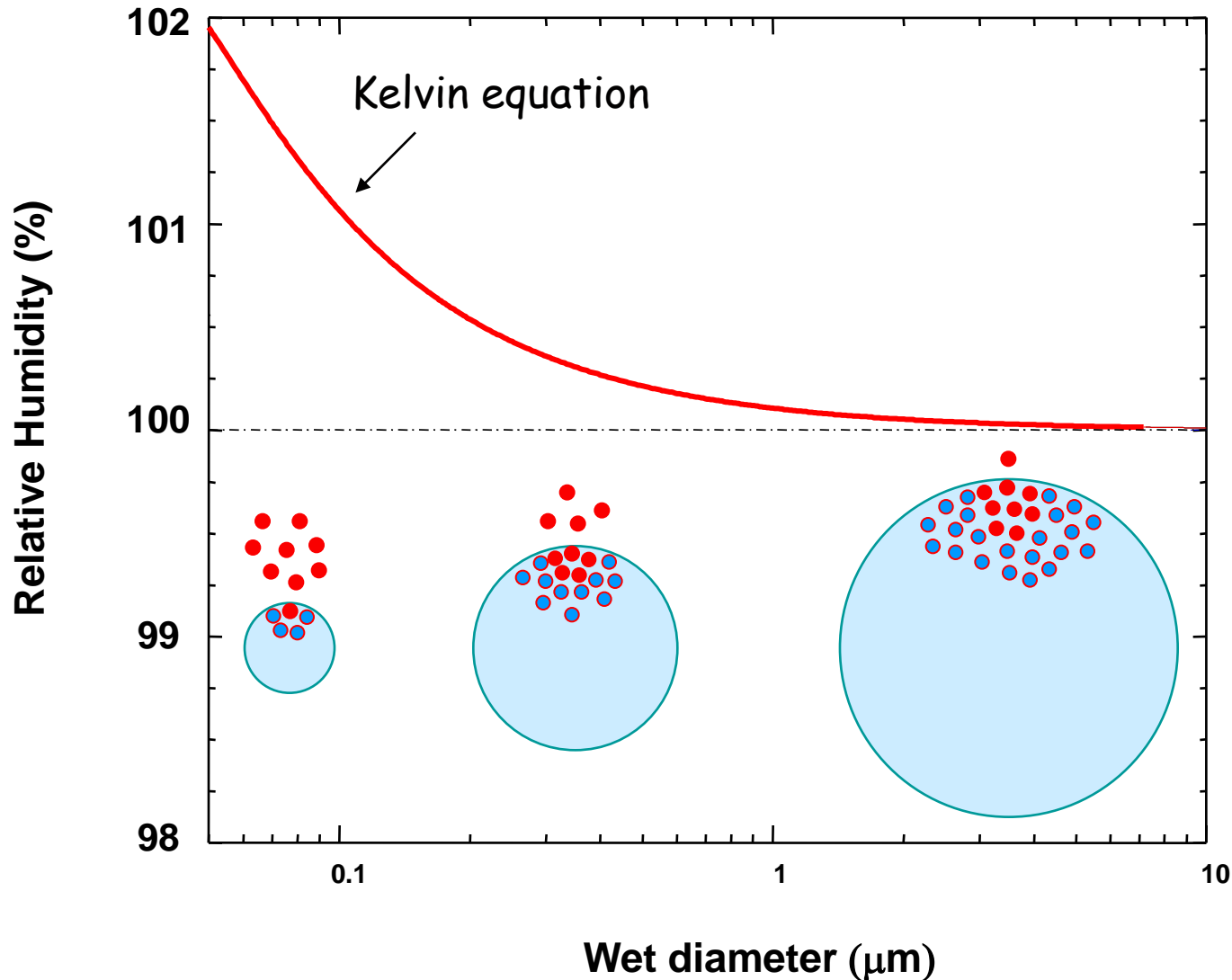
**Conceptual steps are:**

- Air parcel cools, exceeds dew point
- Water vapor is supersaturated
- Droplets start forming on existing CCN.
- Condensation of water on droplets becomes intense.
- $S$  reaches a maximum
- No more additional drops form

**A “classical” nucleation/growth problem**

# So... when does an aerosol particle act as a CCN ?

Start from a pure H<sub>2</sub>O drop



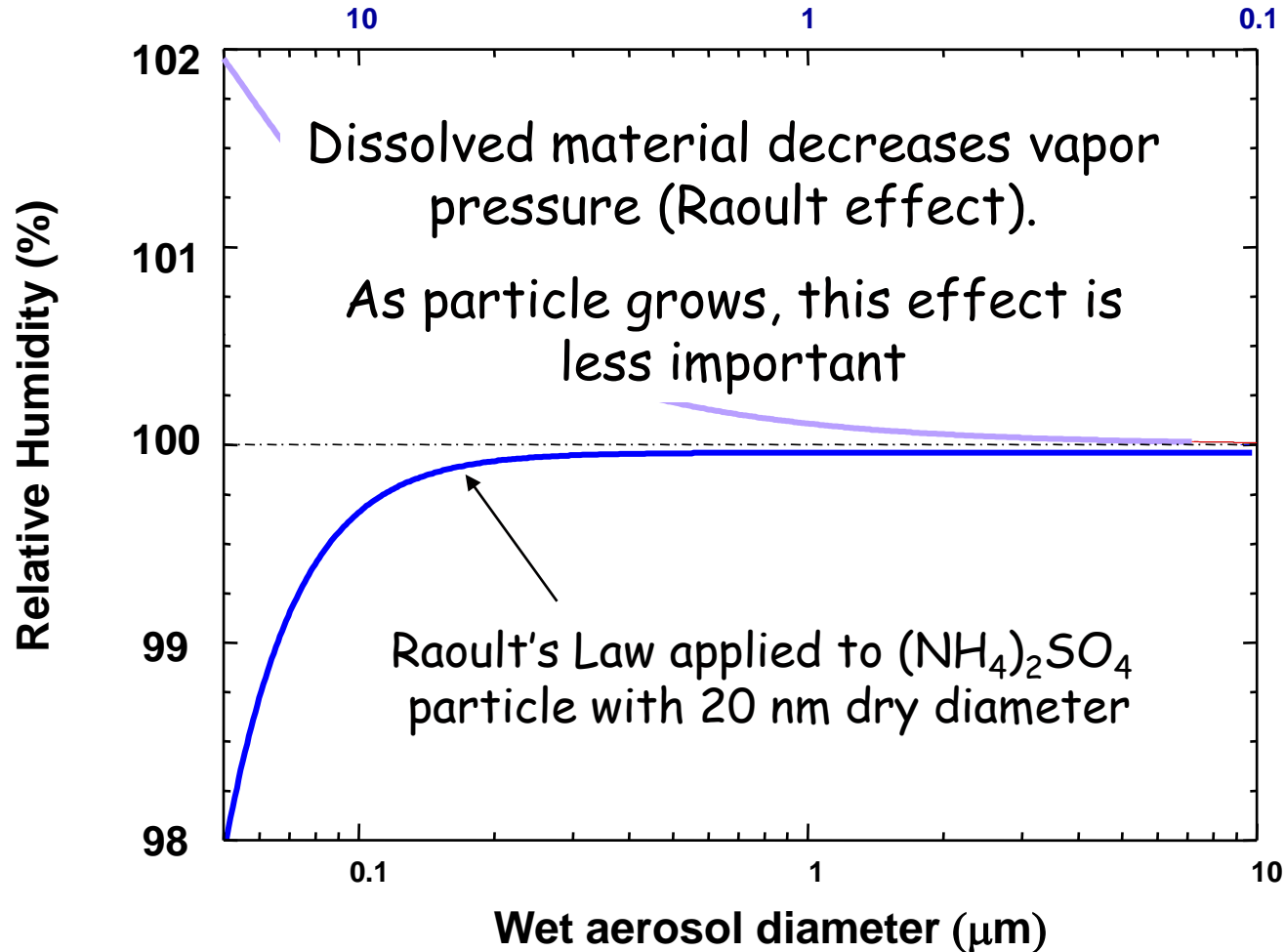
As the droplet size decreases, its equilibrium vapor pressure increases (Kelvin effect).

Less molecules around in small drops to "pull" H<sub>2</sub>O in the droplet phase

# When does an aerosol particle act as a CCN ?

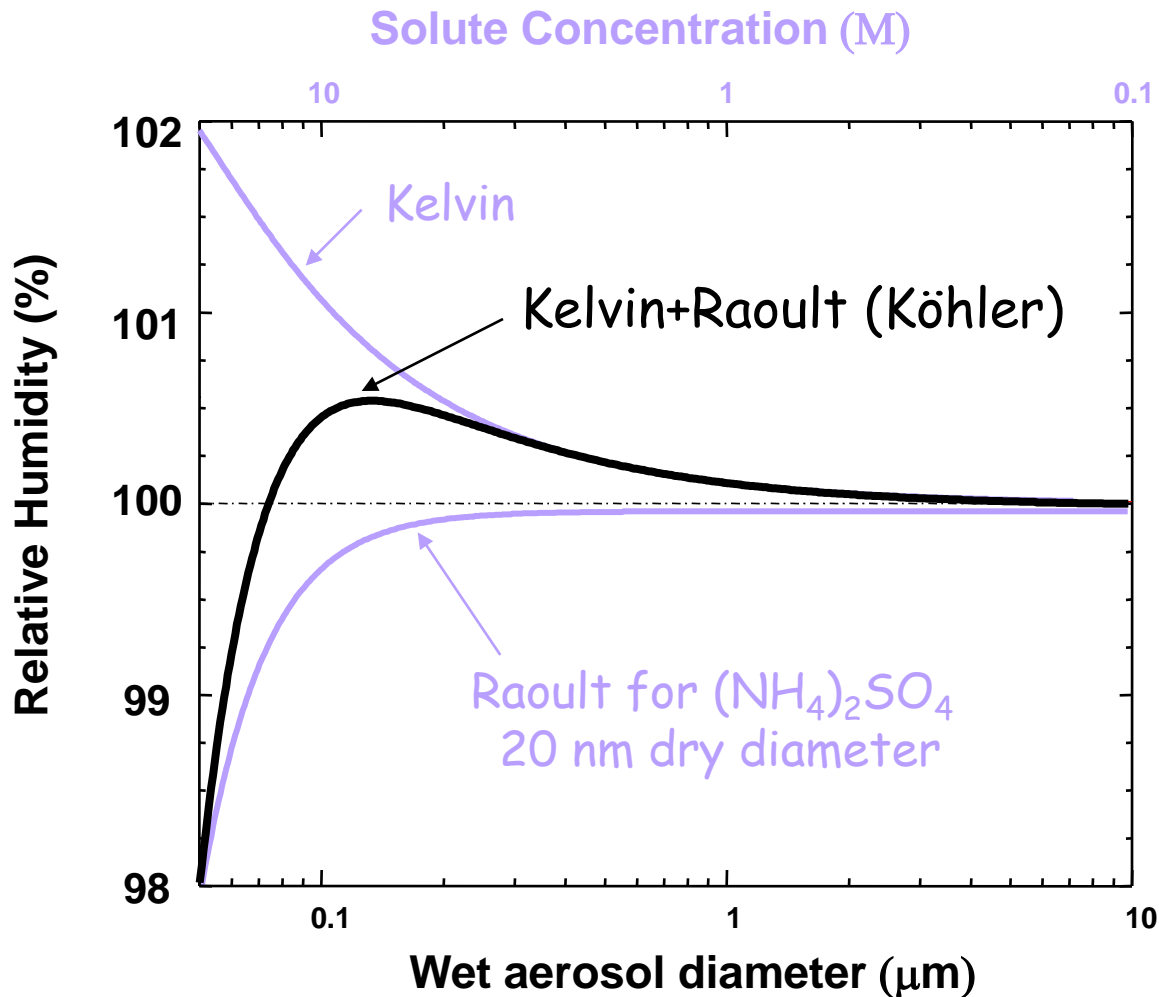
Take same drop and add some solute; e.g.,  $(\text{NH}_4)_2\text{SO}_4$

Solute Concentration (M)



# When does an aerosol particle act as a CCN ?

Put both effects together: You get the equilibrium vapor pressure of a wet aerosol particle.

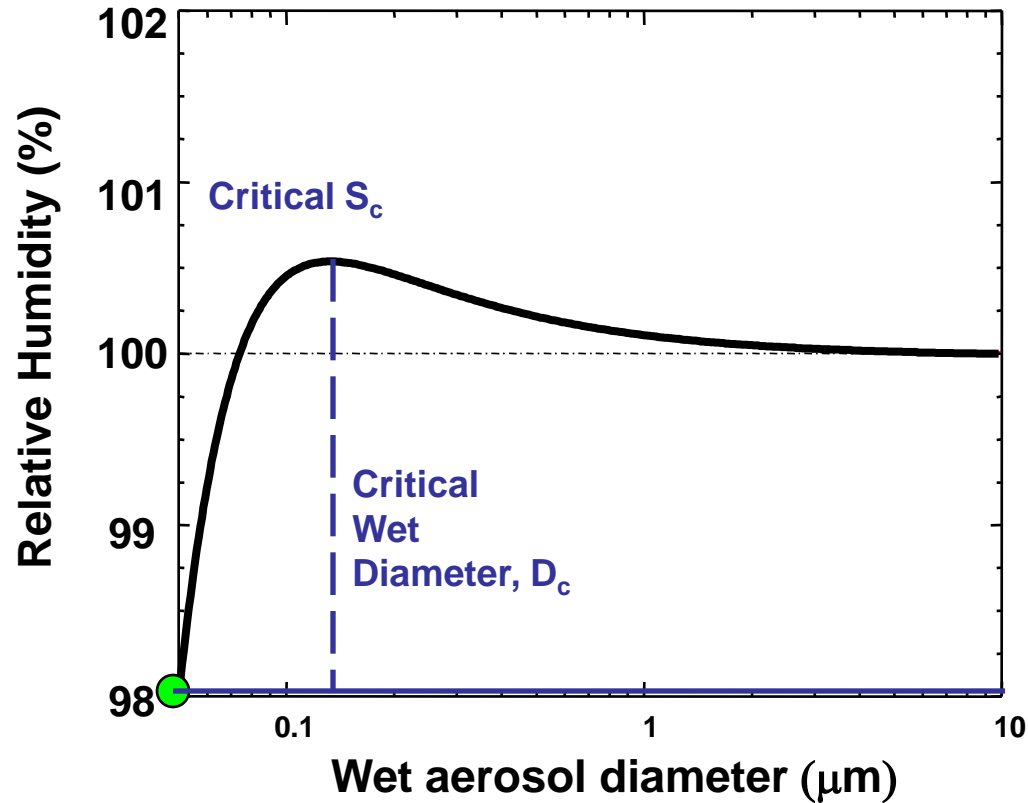
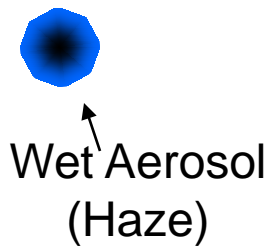


The combined Kelvin and Raoult effects is known as the **Köhler equation (1922)**.

You can be in equilibrium even if you are above saturation.

# When does an aerosol particle act as a CCN ?

Dynamical behavior of an aerosol particle in a variable RH environment.

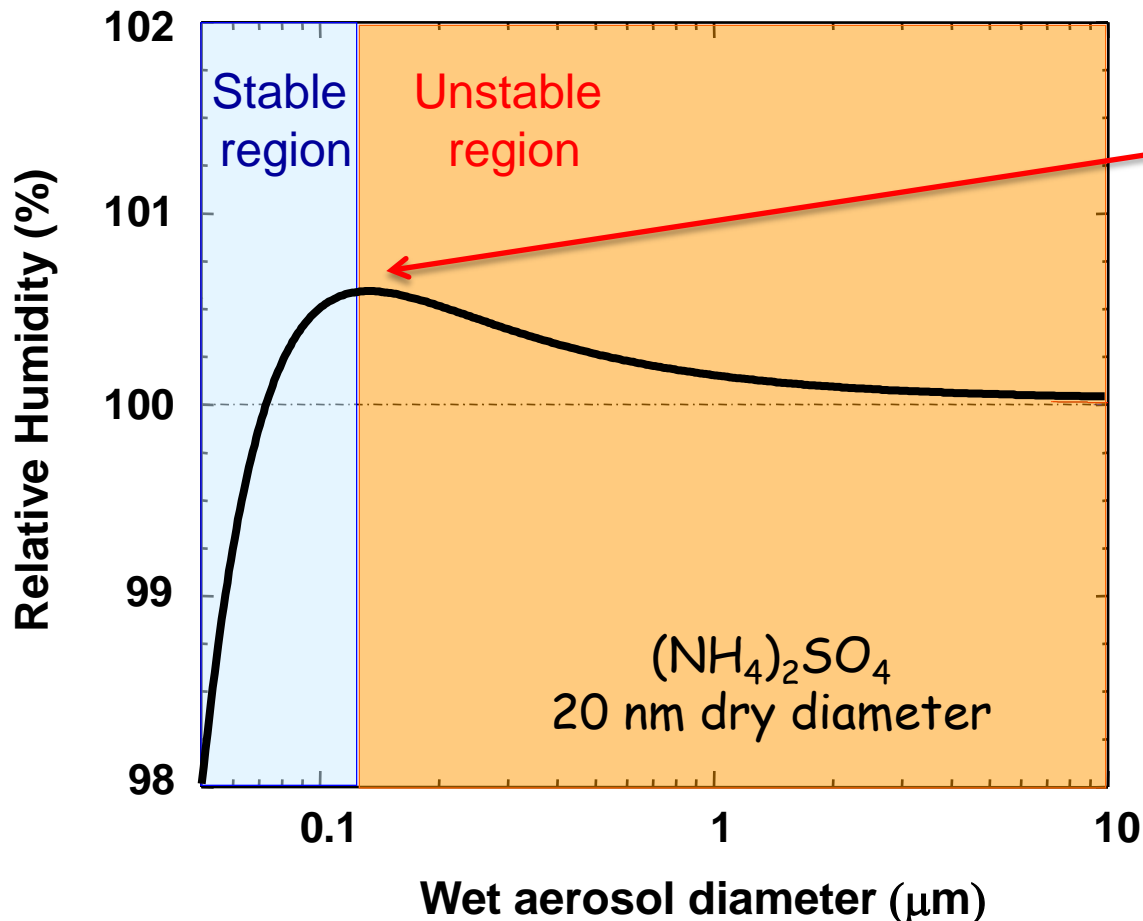


**When ambient saturation ratio exceeds  $S_c$ , particles act as CCN.**



# When does an aerosol particle act as a CCN ?

When the ambient saturation ratio  $S > S_c$  AND the wet size is larger than  $D_c$ . ( $S > S_c$  sufficient; Nenes et al., 2001).



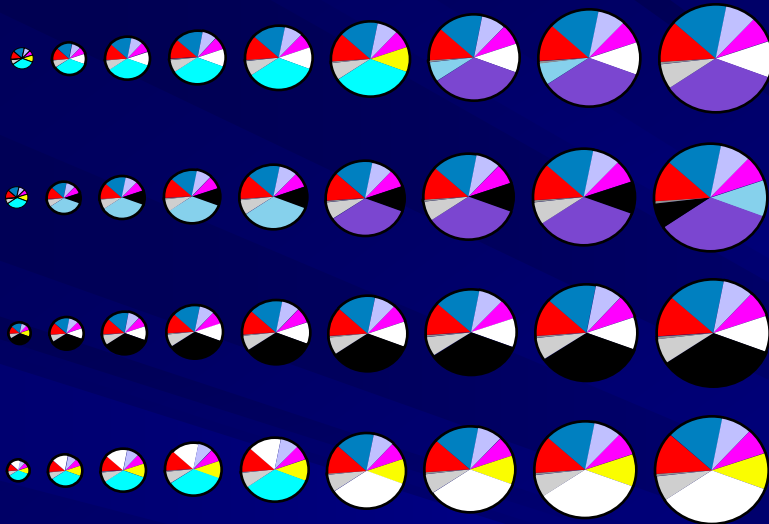
$$S_c = \left( \frac{4A^3}{27B} \right)^{1/2}$$

$A$ : surf. ten. parameter  
 $B$ : solute parameter

$$S_c \sim d_{\text{dry}}^{-3/2}$$

$$S_c \sim \epsilon_{\text{soluble}}^{-1/2}$$

# Aerosol Problem: Complexity



## An integrated "soup" of

- Inorganics, organics (1000's)
- Particles can have uniform composition with size...
- ... or not
- Can vary vastly with space and time (esp. near sources)

## Organic species are a headache

- They can facilitate cloud formation by acting as surfactants and adding solute (hygroscopicity)
- Oily films can form and delay cloud growth kinetics

## In-situ data to study the aerosol-CCN link:

Usage of CCN activity measurements to "constrain" the above "chemical effects" on cloud droplet formation.

# Understanding & parameterizing CCN activity...

Petters and Kreidenweis (2007) expressed the solute parameter in terms of a "hygroscopicity parameter",  $\kappa$

$$s_c = \left( \frac{4A^3}{27B} \right)^{1/2} \longrightarrow s_c = \left( \frac{4A^3}{27\kappa} \right)^{1/2} d^{-3/2}$$

$\kappa \sim 1$  for NaCl,  $\sim 0.6$  for  $(\text{NH}_4)_2\text{SO}_4$ ,  $\sim 0-0.3$  for organics

$\kappa$  rarely exceeds 1 in atmospheric aerosol

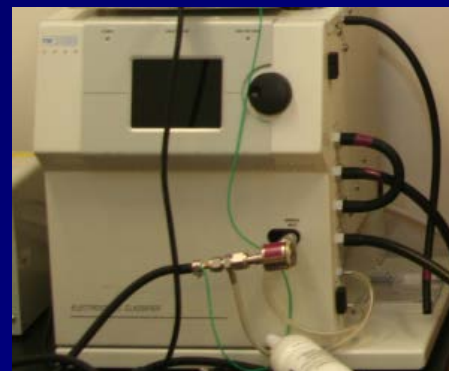
Simple way to think of  $\kappa$ : the "equivalent" volume fraction of NaCl in the aerosol (the rest being insoluble).

$\kappa \sim 0.6 \Rightarrow$  particle behaves like 60% NaCl, 40% insoluble

# Quantifying hygroscopicity: size-resolved CCN measurements



Polydisperse  
Aerosol



Scanning Mobility Particle Sizer

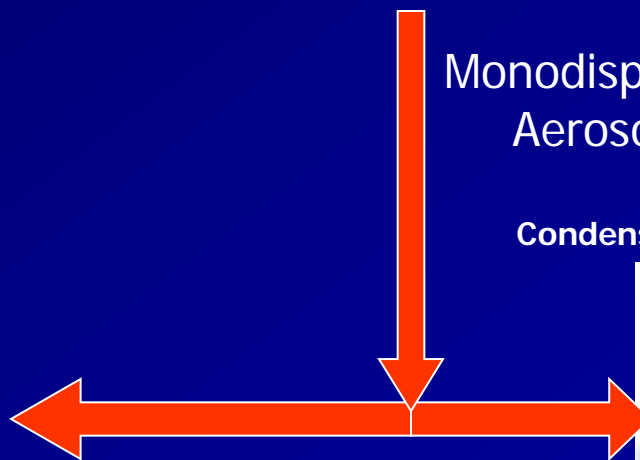
Size Selection

Monodisperse  
Aerosol

Condensation Particle Counter, 3010

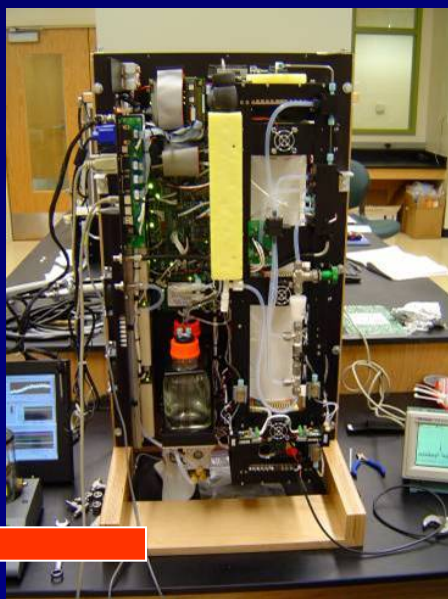


Count CN



Particle Detection

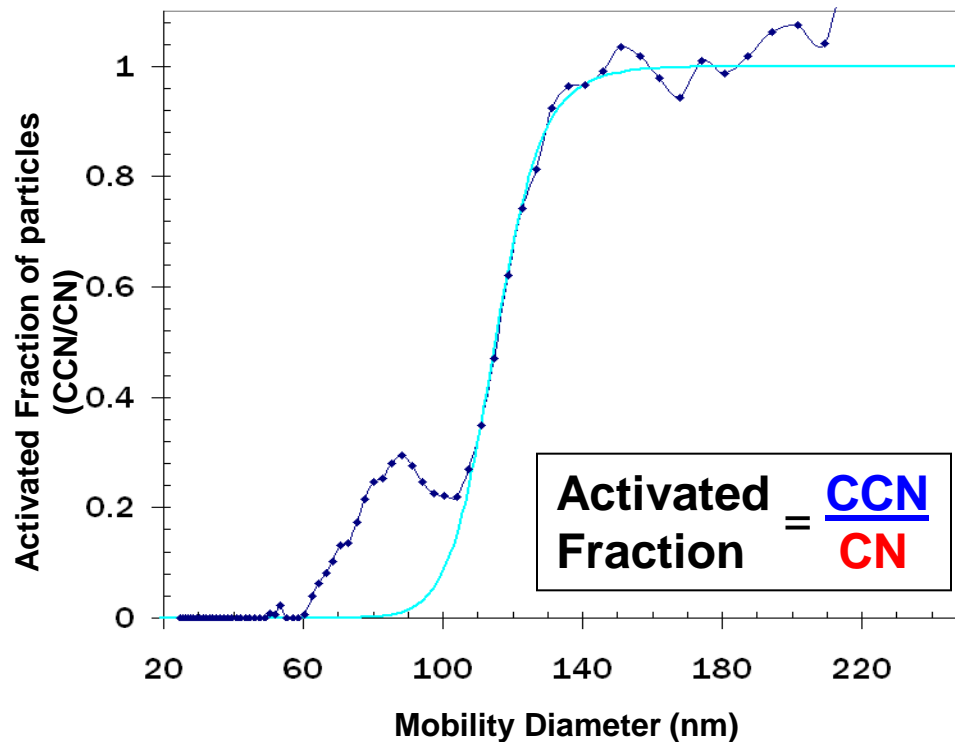
Count  
CCN



Continuous Flow Streamwise  
Thermal Gradient Counter

# Quantifying hygroscopicity: size-resolved CCN measurements

Results: "activation curves"  
CCN/CN as a function of  $d$



Count  
CCN

Continuous Flow Streamwise  
Thermal Gradient Counter

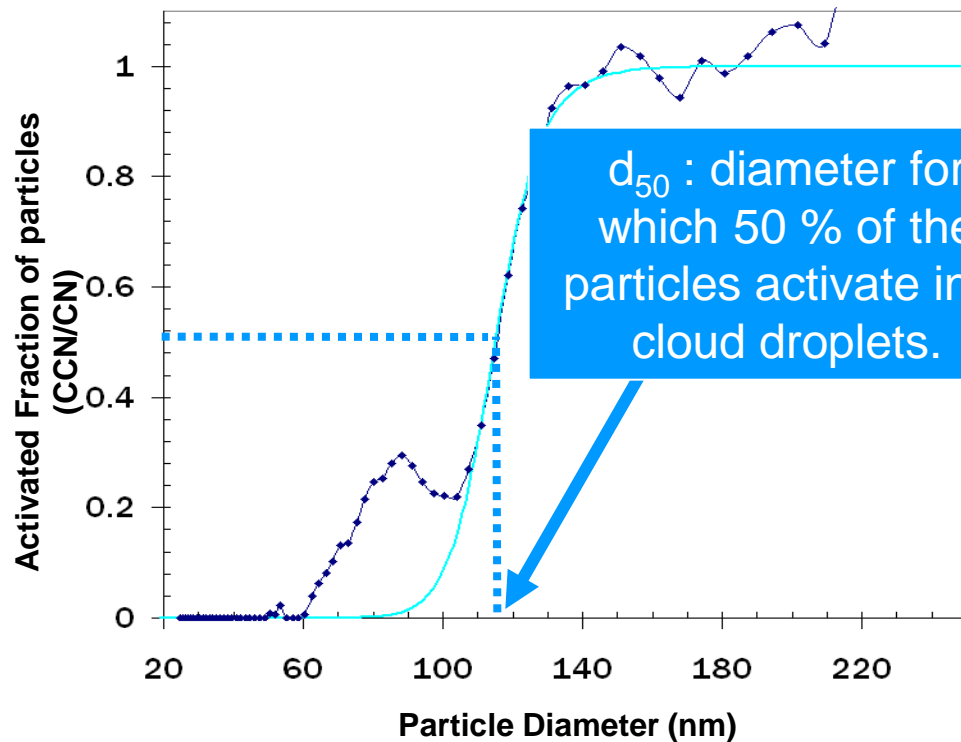
Particle Counter, 3010



Count CN

# Determining $\kappa$ : size-resolved CCN measurements

$d_{50} \downarrow$ : aerosol becomes more hygroscopic



Count  
CCN

Continuous Flow Streamwise  
Thermal Gradient Counter

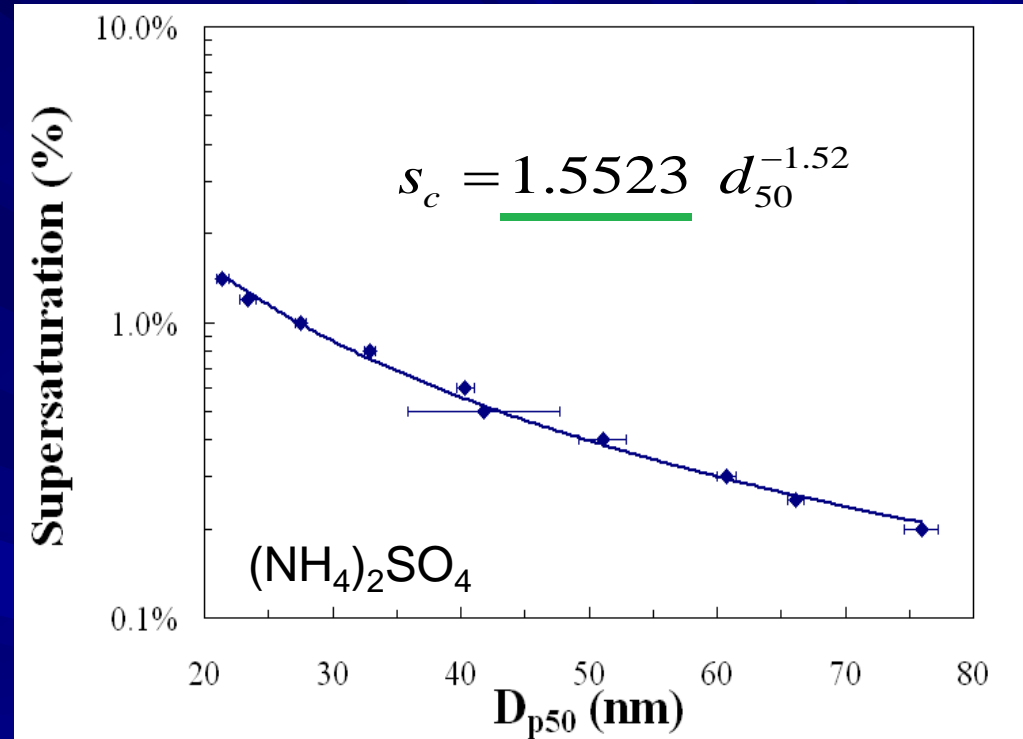
Particle Counter, 3010



Count CN

# Parameterizing the CCN activity data using methods based on Köhler-theory

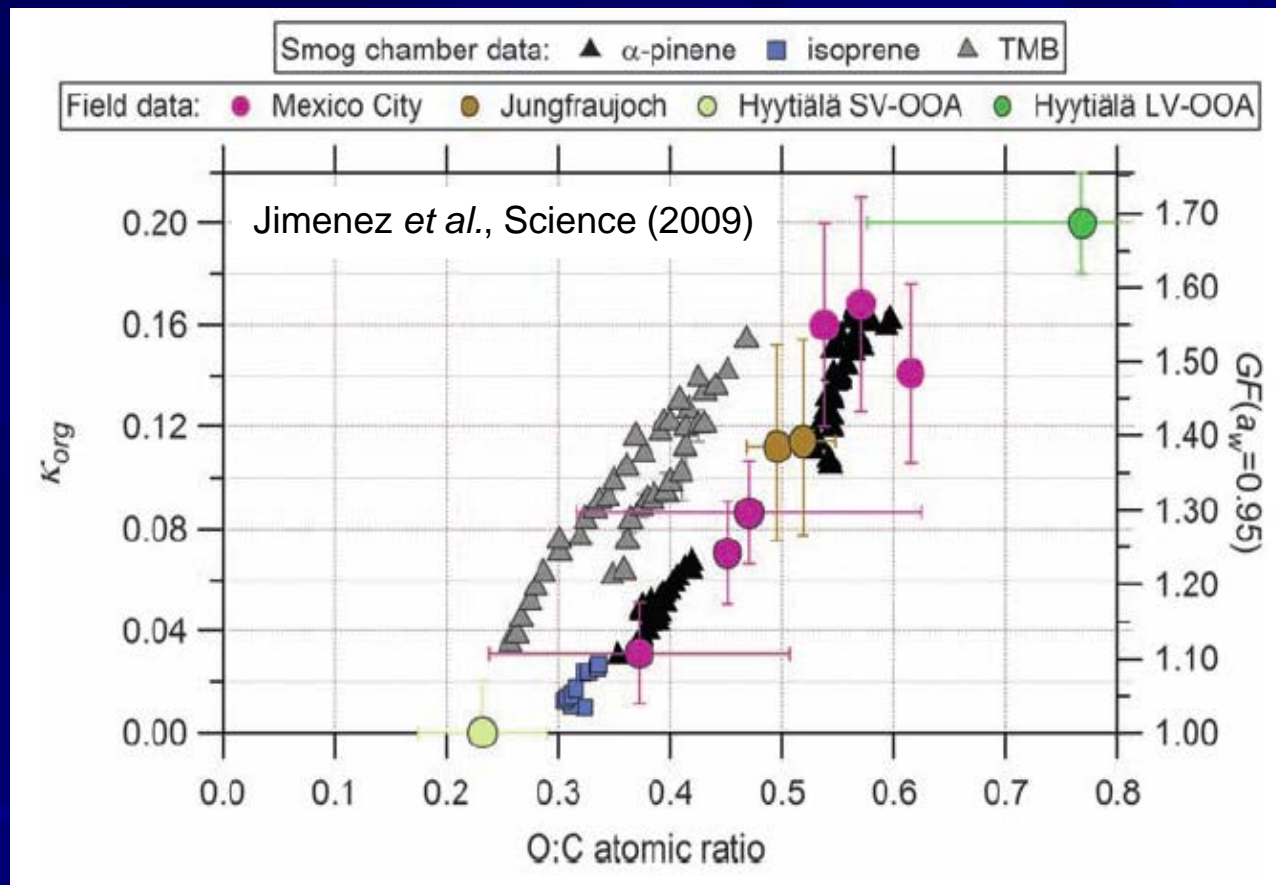
- Determine  $d_{50}$  dependence on supersaturation.
- Fit the measurements to a power law expression.
- Relate fitted coefficients to aerosol properties (e.g. hygroscopicity parameter  $\kappa$ ) by applying theory:



$$S_c = \omega d_{50}^{-3/2} = \left[ \frac{4A^3}{27\kappa} \right]^{1/2} d_{50}^{-3/2}$$

...  $\kappa$  can also be related to an average molecular weight of the solute in the aerosol (Padró et al., ACP, 2007).

# Understanding & parameterizing CCN activity... ... of organic aerosol



$K_{org}$  depends on oxidation state and precursor.

O:C is related to the water-soluble fraction of organics,

$$K_{org} \sim \epsilon_{sol} K_{sol}$$

Can most of the above be explained as variation in  $\epsilon_{sol}$  ?  
Look at the  $\kappa$  of water-soluble organics...



# The link between $\kappa_{org}$ , O:C and WSOC

- Aged organics in Mexico City aerosol from MILAGRO (Padró et al, 2010).

$$\kappa_{sol} = 0.28 \pm 0.06, \text{ regardless of location and time !}$$

- Organic SOA from biogenic VOCs

$\alpha$ -pinene, monoterpene, isoprene oxidation.

$$\kappa_{sol} \sim 0.28 \text{ (Engelhart et al., ACP, 2009, 2011)}$$

$\beta$ -caryophyllene (Asa-Awuku et al., ACP, 2009).

$$\kappa_{sol} \sim 0.26$$

- SOA from Anthropogenic VOCs (Asa-Awuku et al., ACP, 2010)  
terpinolene, cycloheptene, 1-methylcycloheptene ozonolysis

$$\kappa_{sol} \sim 0.26-0.33$$

- Biomass burning samples (Asa-Awuku et al., 2008)

$$\kappa_{sol} \sim 0.33$$

# The link between $\kappa_{\text{org}}$ , O:C and WSOC

Many "aged" soluble organics (SOA) from a wide variety of sources have a remarkably similar hygroscopicity.

**Speciation** across samples **varies considerably**, but their **cumulative effects** on CCN activity are about the same.

Changes in surface tension partially compensates for shifts in average molar volume to give the constant  $\kappa_{\text{sol}}$

What matters is the fraction of soluble organic - which is consistent with  $\kappa_{\text{org}}$  correlating with O:C.

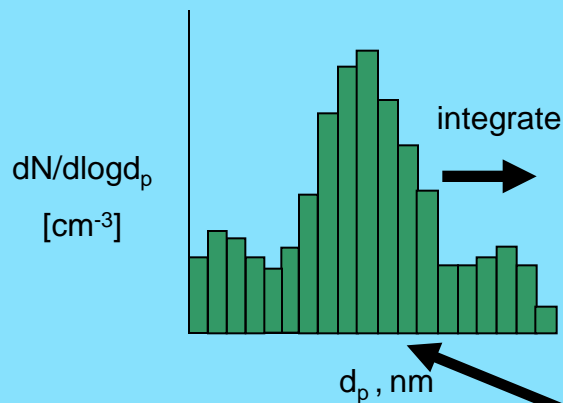
$$\kappa_{\text{org}} = (0.25 \pm 0.05) \varepsilon_{\text{sol}}$$

**Complexity sometimes simplifies things for us.**

# Testing CCN activation theory: CCN "Closure" studies

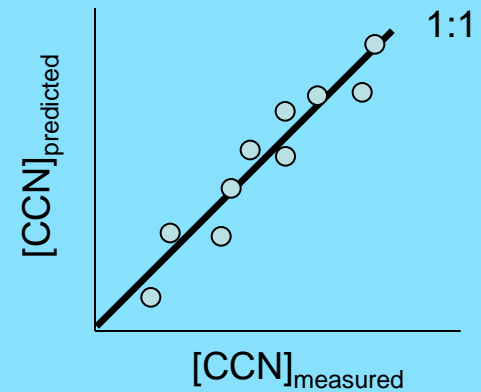
Compare measurements of CCN to predictions using Köhler activation theory and  $\kappa$  description

Aerosol Size Distribution



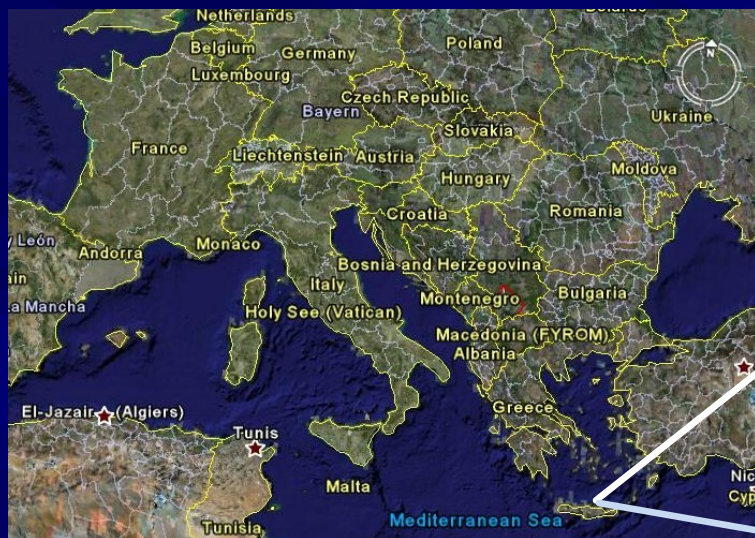
$[\text{CCN}]_{\text{predicted}}$

CCN Closure



Use theory to predict the particles that can act as CCN based on measured chemical composition and CCN instrument supersaturation.

# Finokalia Aerosol Measurement Campaign (FAME-07) - Summer 2007



**DMT CCN counter**  
*Supersaturation*  
*range: 0.2-1.0%*

**TSI 3080 SMPS**  
*Size range: 20-460*  
*nm*

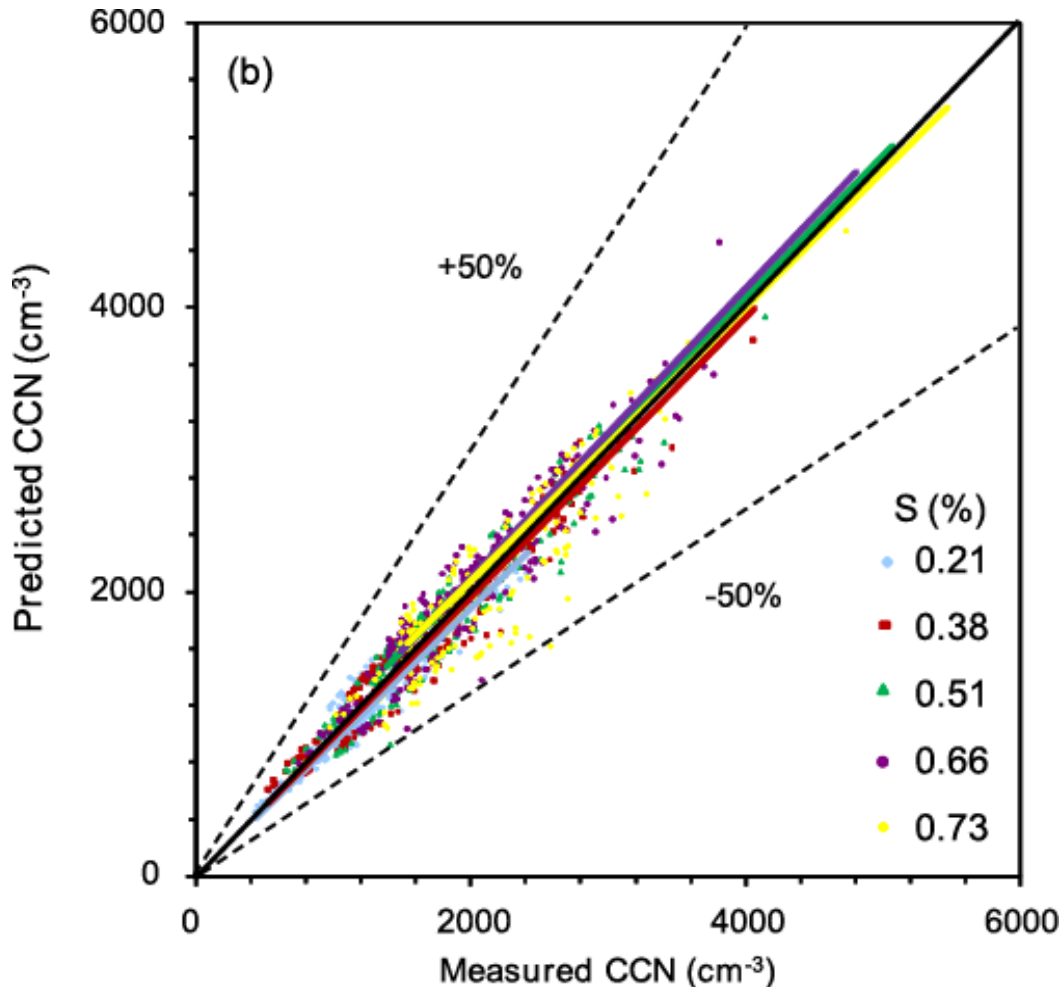
**Low-vol impactor**  
*Ionic composition*  
*measured via IC*

**WSOC/EC/OC also**  
*measured*



(Bougiatioti et al., ACP, 2009)

# Finokalia Aerosol Measurement Campaign (FAME-07) - CCN closure



2% overprediction  
(on average).

Introducing  
comprehensive  
composition into  
CCN calculation  
gives excellent CCN  
closure.

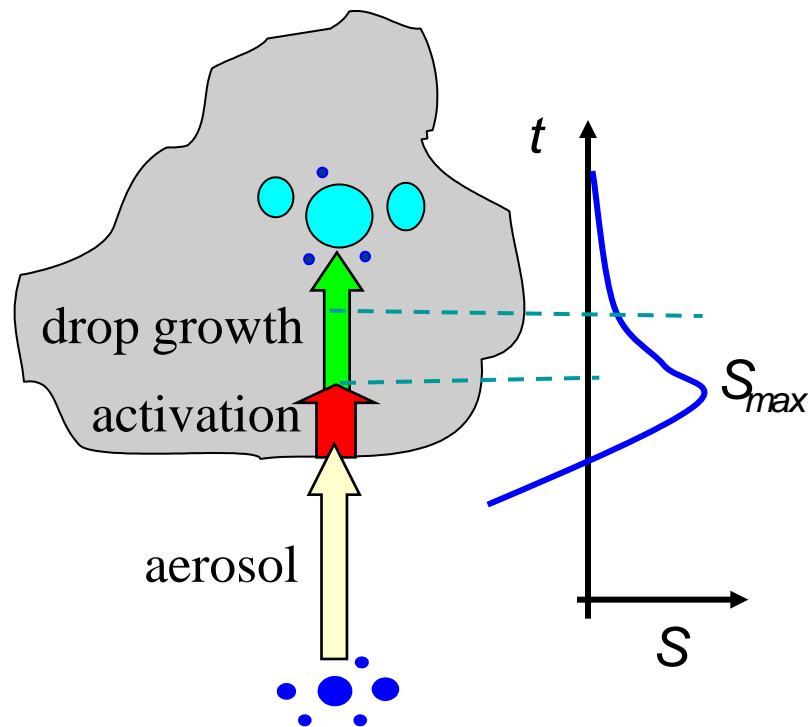
Köhler (CCN  
activation) theory  
*really* works.

(Bougiatioti et al., ACP, 2009)

# CCN activation requires knowledge of cloud RH...

**Approach:** use the “simple story of droplet formation”

**Basic ideas:** Solve conservation laws for energy and the water vapor condensing on aerosol particles in cloudy updrafts.



**Steps are:**

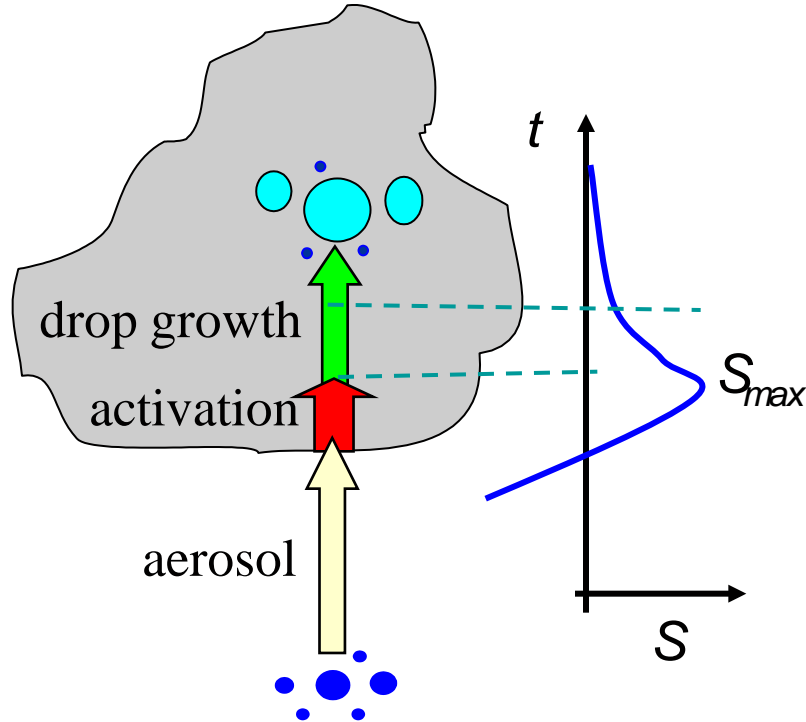
- Air parcel cools
- Eventually exceeds dew point
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**A “classical” nucleation/growth problem**

# Liquid Phase Clouds

**Approach:** use the “simple story” (1D parcel theory)

**Basic ideas:** Solve conservation laws for energy and the water vapor condensing on aerosol particles in cloudy updrafts.



**Parameterization goals:**

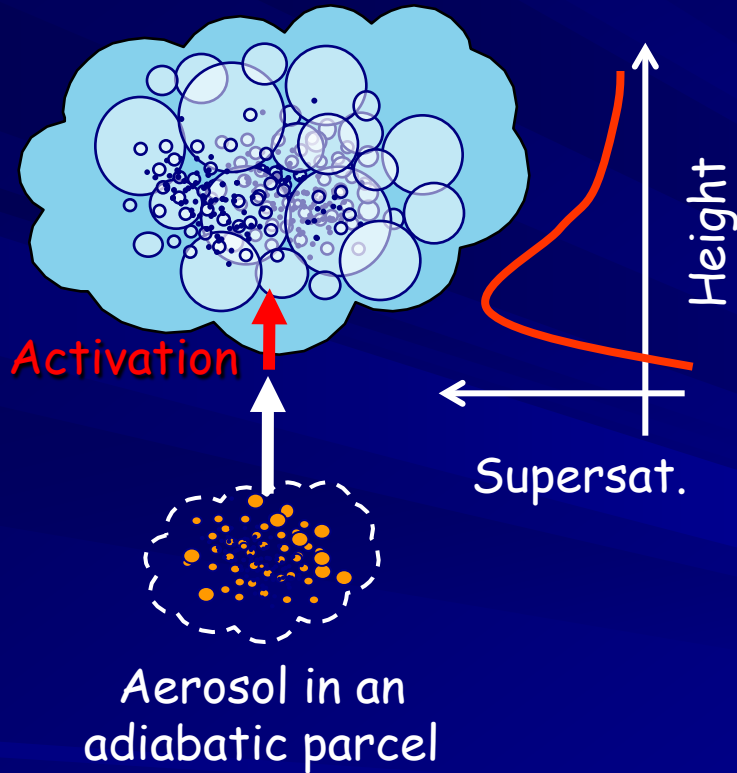
Determine the number of droplets  $N_d$  that can activate at the parcel maximum supersaturation,  $S_{max}$ .

**This is a two step process:**

1. Obtain parcel  $S_{max}$
2. Determine  $N_d$  by counting Cloud Condensational Nuclei (CCN) with  $s_c < S_{max}$
3. CCN are determined from an appropriate theory (Köhler, Adsorption activation, etc).

# Cloud Droplet Formation in GCMs

## State of the art



### Mechanistic Parameterizations:

Twomey (1959); Abdul-Razzak et al., (1998); Nenes and Seinfeld, (2003); Fountoukis and Nenes, (2005); Ming et al., (2006), and others.

**Input:**  $P, T$ , vertical wind, particle size distribution, composition.

**Output:** Cloud properties (droplet number, size distribution).

**How:** Solve/apply **one algebraic equation** (instead of ODE's).

**Basic Assumption:** Adiabaticity

### Comprehensive review & intercomparison:

Ghan, Abdul-Razzak, Nenes et al., *Rev. Geoph.*, in review



# Are these parameterizations "good enough"?

Evaluate them with in-situ data from airborne platforms



CIRPAS Twin Otter



Observed Aerosol size  
distribution & composition

Observed Cloud updraft  
Velocity (PDF)

Predicted Drop Number  
(Parameterization)

Compare

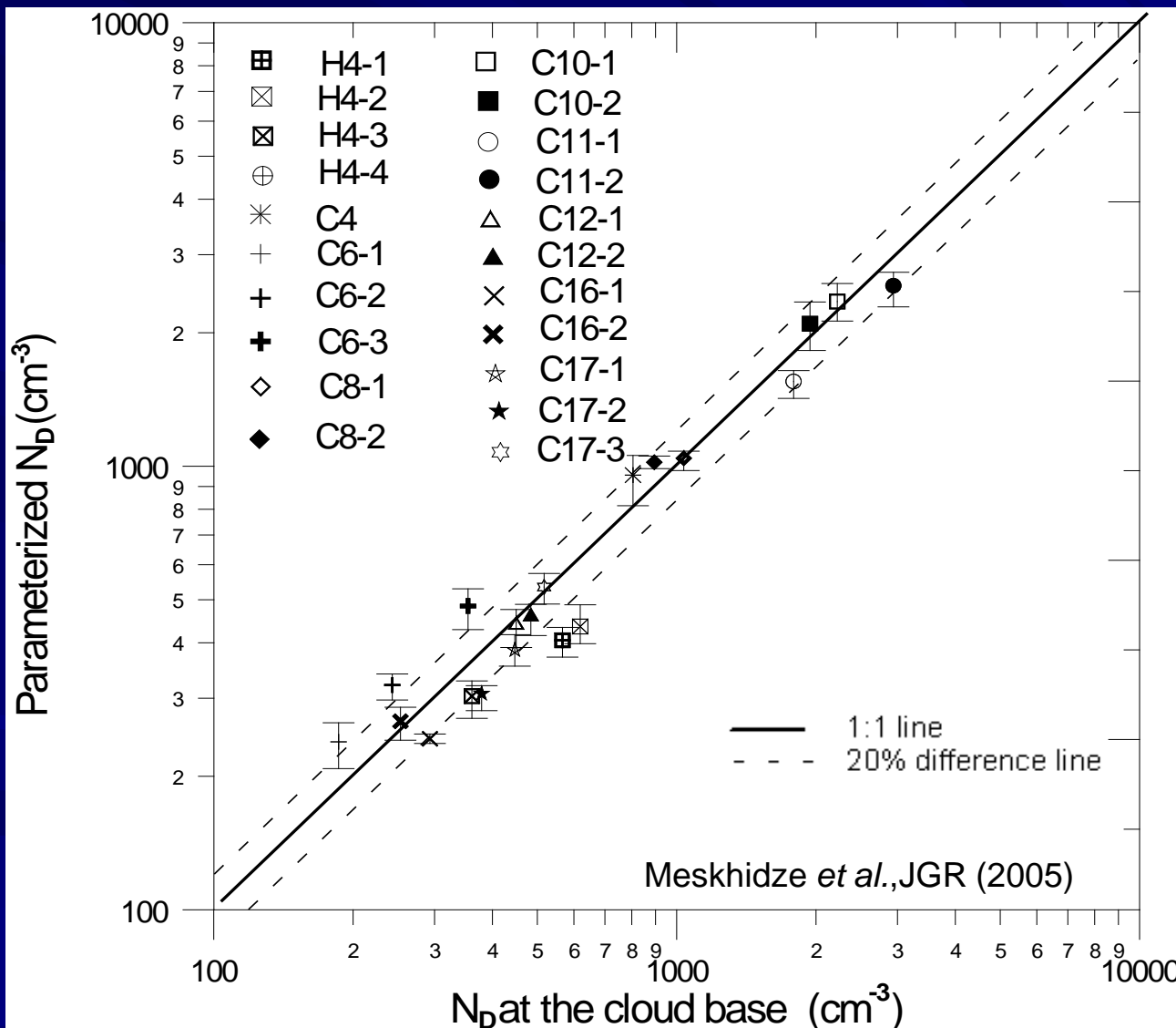
Observed Drop Number  
Concentration



# CRYSTAL-FACE (2002) "Adiabatic" Cumulus clouds



CIRPAS Twin Otter



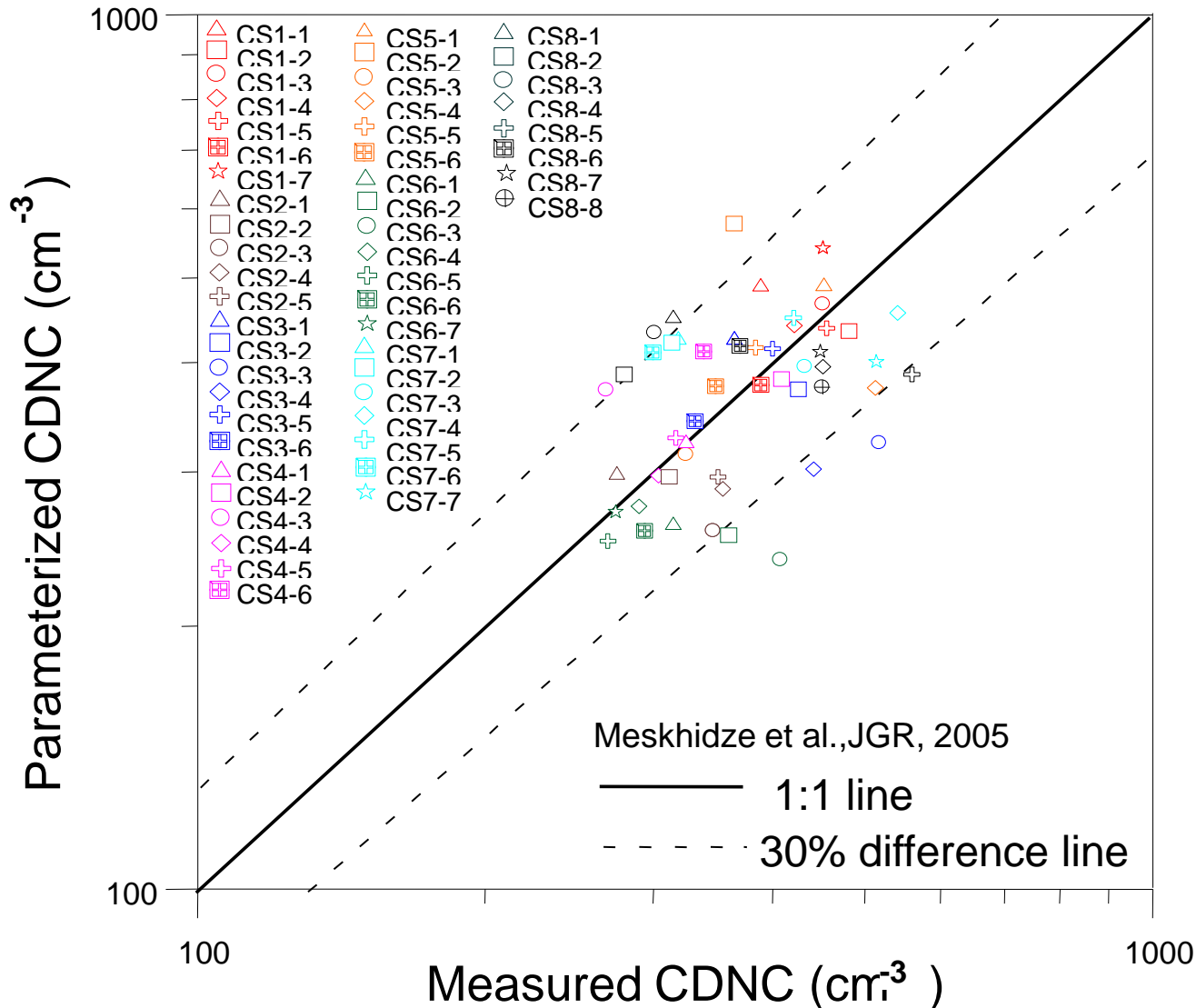
Parameterized  
agrees with  
observed cloud  
droplet number  
in "adiabatic-  
like" parcels.

Agreement to  
within a few %  
(on average)!

# CSTRIPE (2003) Marine Stratocumulus



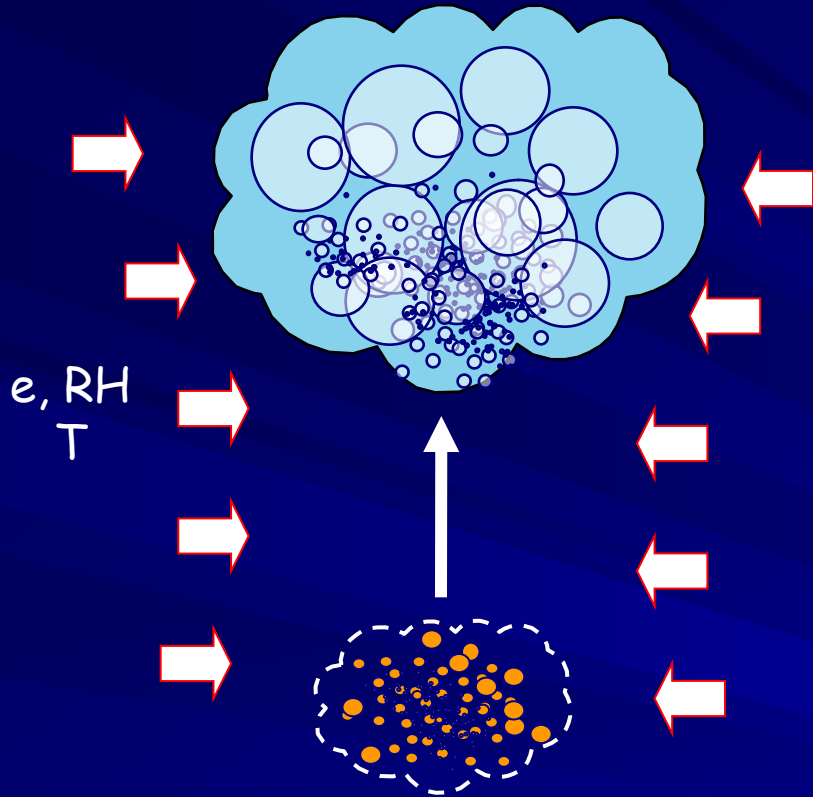
CIRPAS Twin Otter



Parameterized  
agrees with  
observed cloud  
droplet number  
in "adiabatic-  
like" parcels.

Agreement to  
within a few %  
(on average)!

# Ambient clouds are not usually adiabatic...



- Barahona and Nenes (2007): Droplet parameterization for clouds continuously entraining in dry air.
- Equations are similar to adiabatic activation - only that mixing of outside air is allowed.
- "Outside" air with  $(RH, T)$  is assumed to entrain at a rate of  $e$  (kg air / kg parcel / m ascent)

## Very important point finding:

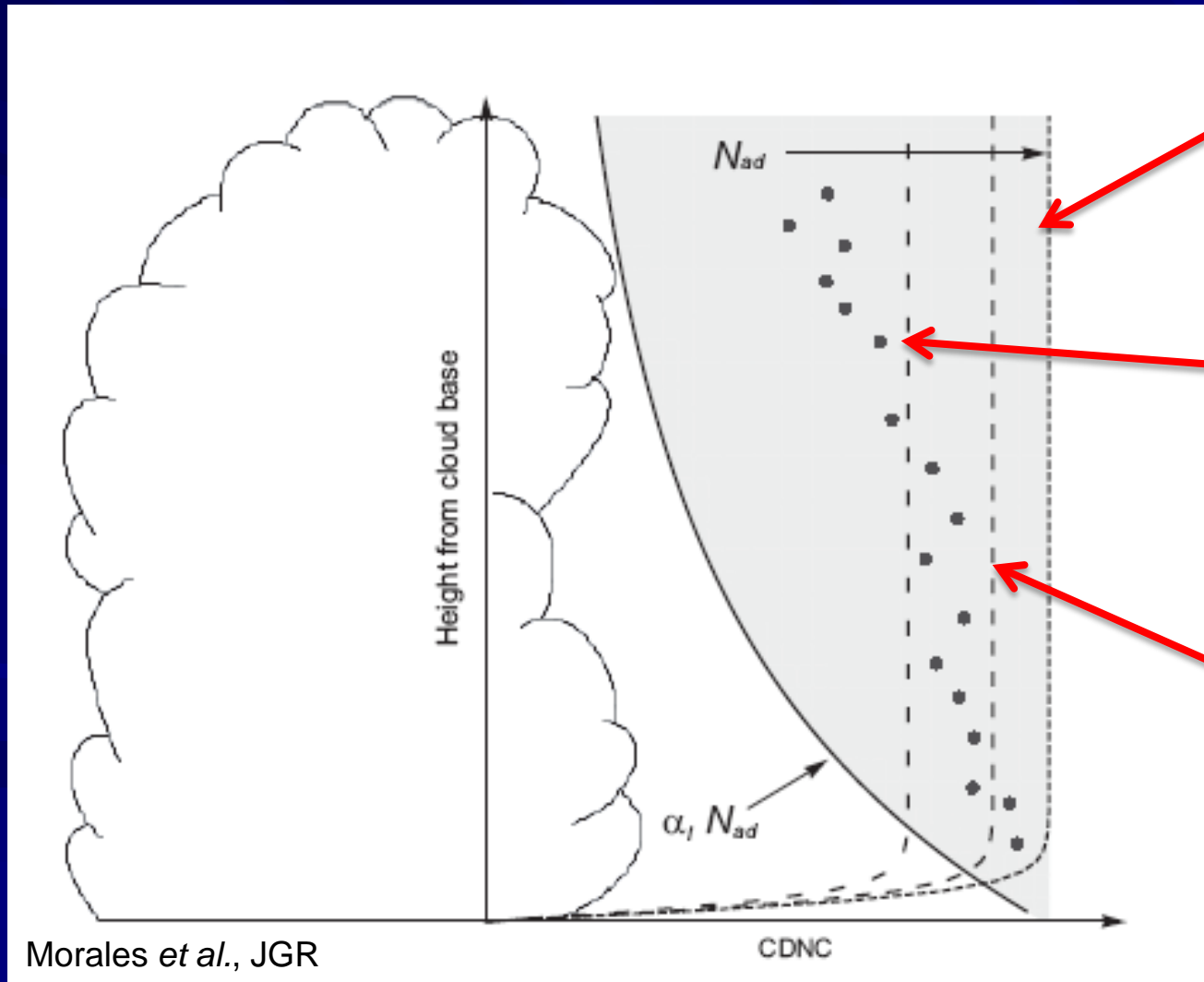
- Any adiabatic parameterization can be modified to consider entrainment - just replace  $w$  with  $w(1 - e/e_c)$  !

vertical  
velocity

entrainment rate that  
completely dissipates cloud

# Expressing entrainment effects on $N_d$

Approach:  $N_d$  predicted from the entraining parameterization represents cloud average. Link  $e, e_c$  to liquid water profile.



Adiabatic  $N_d$   
Overestimation

$N_d$  with  $1-e/e_c$   
diagnosed from  
the average  
dilution ratio  
( $LWC/LWC_{ad}$ )

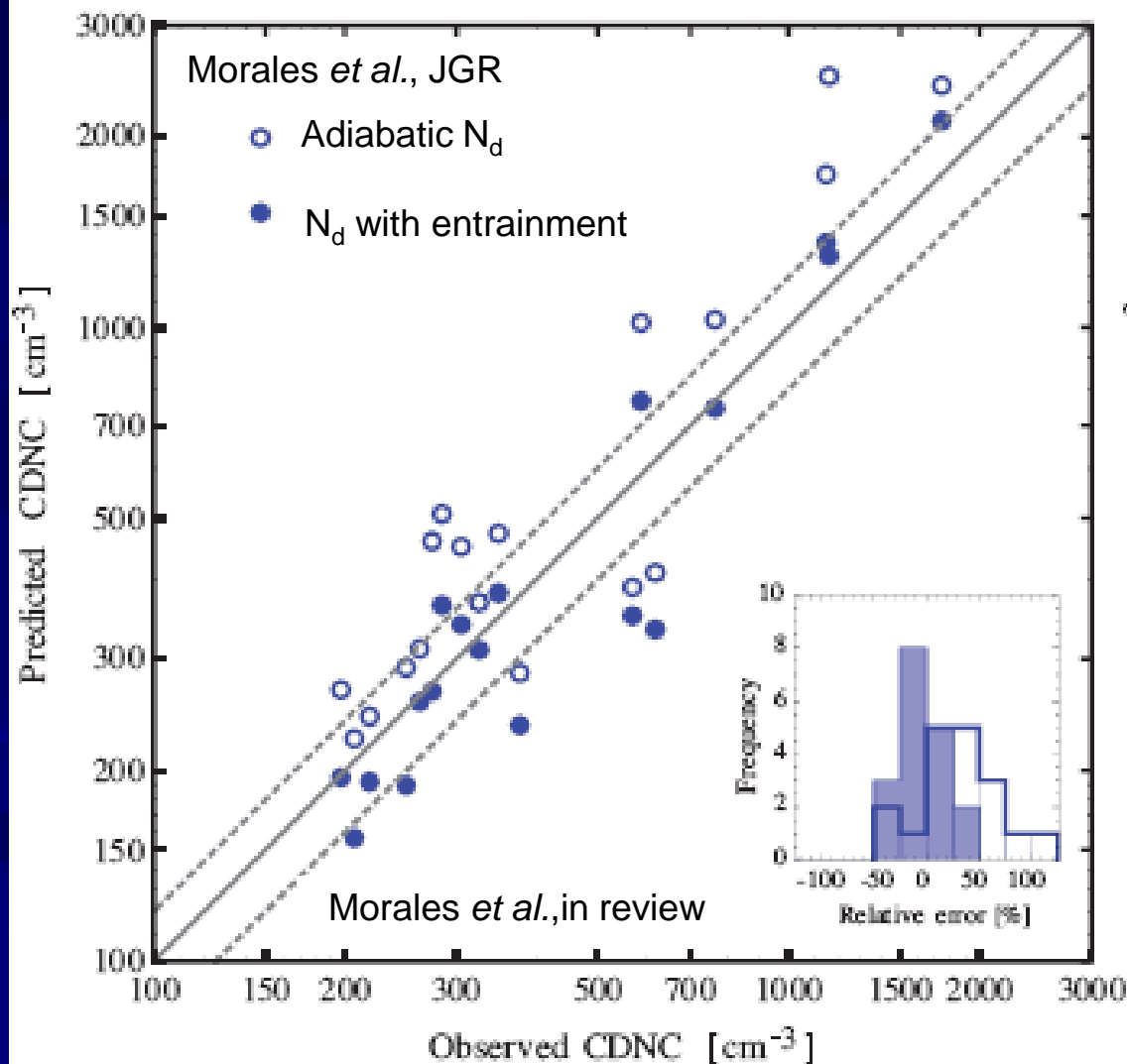
$N_d$  with constant  
entrainment rate  
diagnosed from  
average dilution  
ratio



# CRYSTAL-FACE (2002) Entraining Cumulus clouds



CIRPAS Twin Otter



**Adiabatic  $N_d$ :**  
45% overprediction

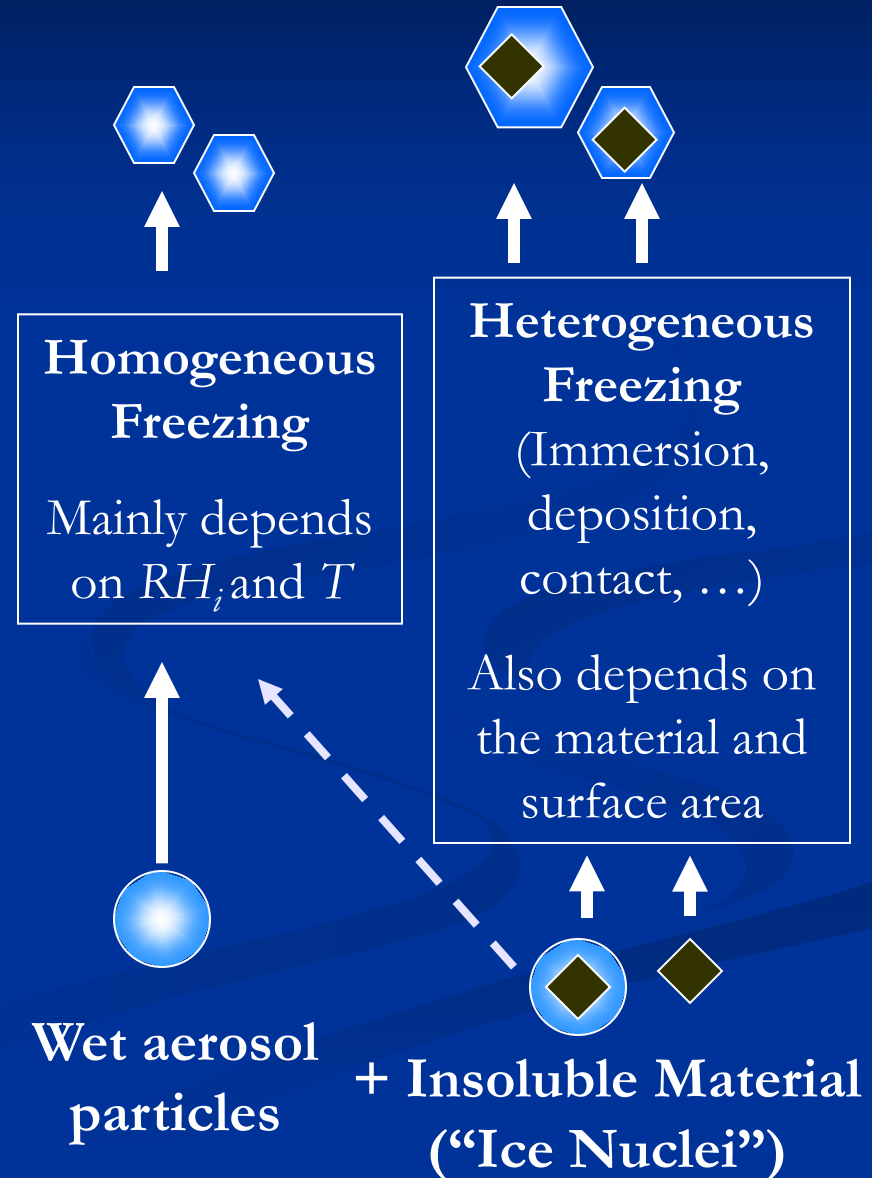
**$N_d$  with entrainment:**  
3.5% error when  
Column-average  
adiabaticity ratio  
( $LWC/LWC_{ad}$ ) used to  
diagnose  $1-e/e_c$

**$N_d$  with pure  
heterogeneous mixing**  
45% underprediction

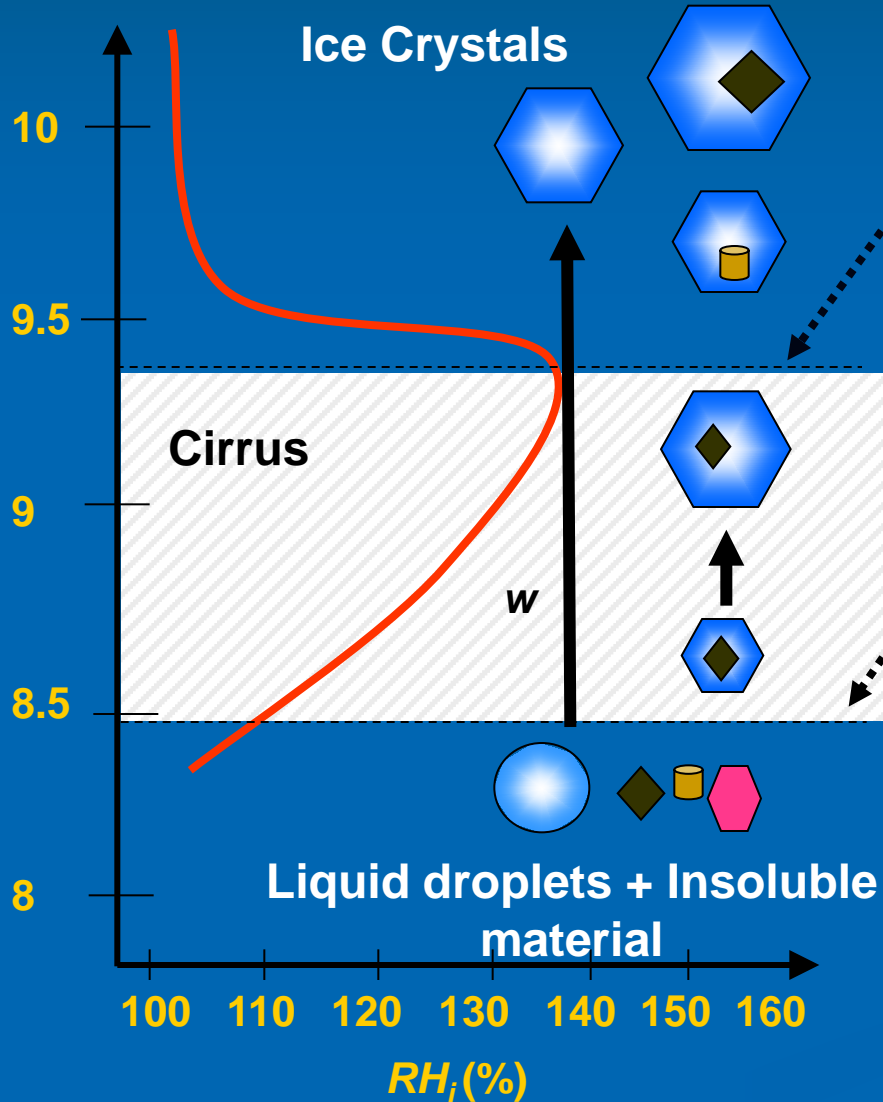
# Cirrus (Ice) Clouds

*Multiple mechanisms for ice formation can be active.*

<http://www.alanbauer.com>



# Cirrus (Ice) Clouds



Conceptual steps are:

Homogeneous freezing of droplets

Crystal growth, fresh IN continue to freeze and deplete vapor

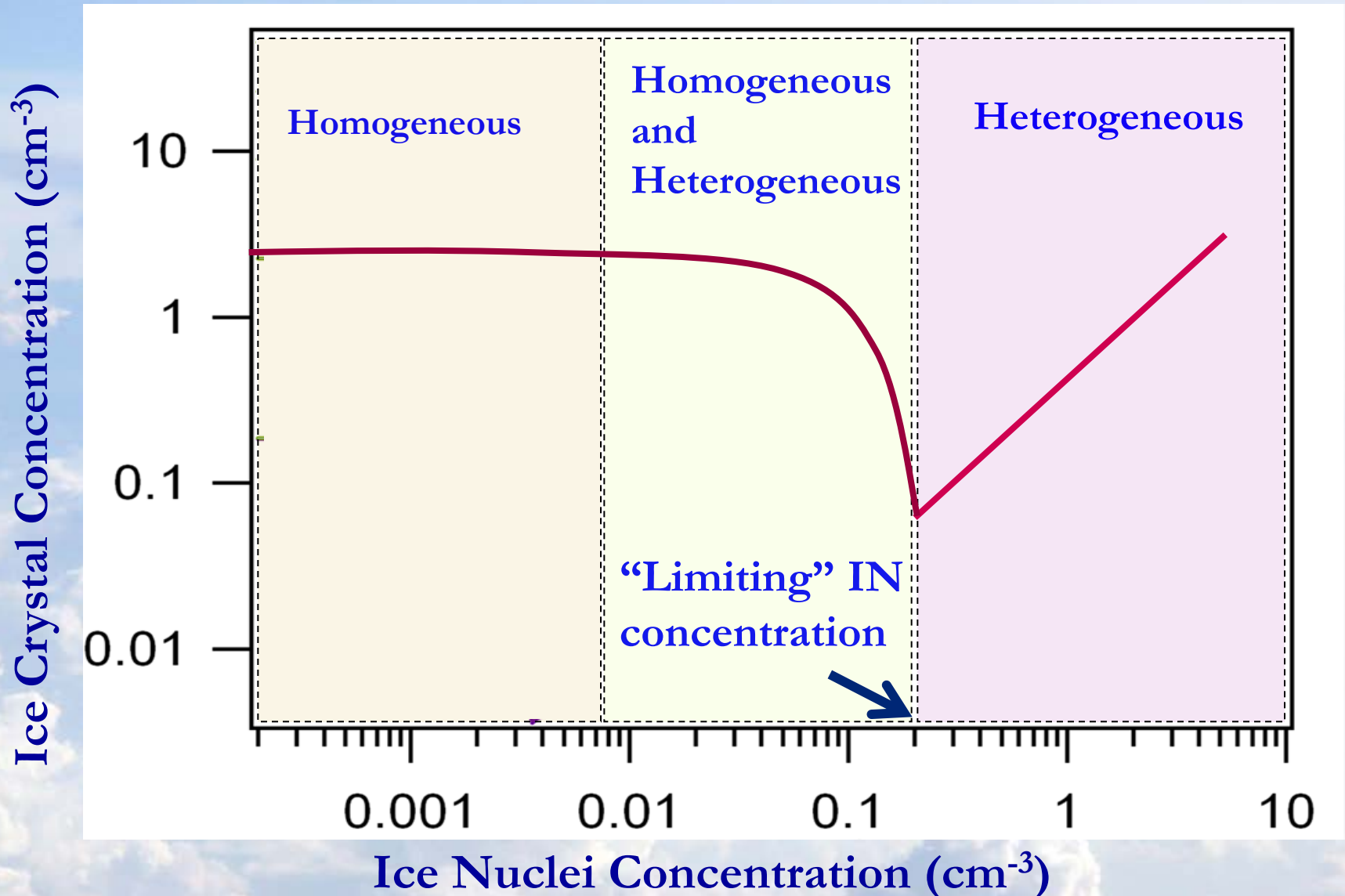
Heterogeneous IN freezing begin forming ice

Expansion cooling and ice supersaturation development

Soluble and insoluble aerosol initial distribution



# Source of strong nonlinearity: IN effects on Ice Crystal Concentration



# Cirrus Formation in Global Climate Models: Current State of the Art

Approach	Advantages	Disadvantages
<b>Empirical</b>	Very fast Representative values	Limited Coverage Cannot be used to assess aerosol effects
<b>Off-line solutions</b> (Liu and Penner, 2005)	Fast Physically-based	Consider only a limited range of conditions
<b>Analytical-Numerical</b> (e.g., Kärcher, et al., 2006)	Most of the physics included.	Simplistic description of IN (Single freezing threshold”).

**Analytical models based on cloud formation equations are needed!**

# Ice Parameterization Development

## Solving the parcel equations...

$$\frac{dS_i}{dt} = -\frac{M_a p}{M_w p_i^o} \frac{dw_i}{dt} - (1 + S_i) \left[ \frac{\Delta H_s M_w}{RT^2} \frac{dT}{dt} - \frac{g M_a}{RT} V \right]$$

Global water vapor balance

$$\frac{dT}{dt} = -\frac{gV}{c_p} - \frac{\Delta H_s}{c_p} \frac{dw_i}{dt}$$

Energy balance

$$\frac{dw_i}{dt} = \frac{\rho_i}{\rho_a} \frac{\pi}{2} \int \dots \int_x D_c^2 \frac{dD_c}{dt} n_c(D_c, D_{IN}, m_{1, \dots, nx}, t) dD_c dD_{IN} dm_{1, \dots, nx}$$

Ice water vapor condensation

$$\frac{\partial n_c(D_c, D_o)}{\partial t} = -\frac{\partial}{\partial D_c} \left( n_c(D_c, D_o) \frac{dD_c}{dt} \right) + n_o(D_o, S_i) v_o J(t) \exp \left( -\frac{\pi}{6} \int_0^t D_o^3 J(t) dt \right)$$

Ice crystal size distribution evolution = nucleation + growth

$$\frac{dD_c}{dt} = \frac{(S_i - S_{i,eq})}{\Gamma_1 D_c + \Gamma_2}$$

Ice crystal growth

... lots of math and scaling...

Barahona and Nenes, *JGR*, 2008; *ACP*, 2009ab

# Analytical Parameterization for Cirrus Ice Formation and Growth

The analytical solution of the parcel equations :

Ice  
Crystal  
Concentration



$$\frac{N_{het}(s_{max})}{N^*} = \frac{1}{\sqrt{\Delta s_{char}^*}} \frac{(1 + s_{max})}{s_{max}} e^{\frac{2}{\lambda s_{max}}}$$

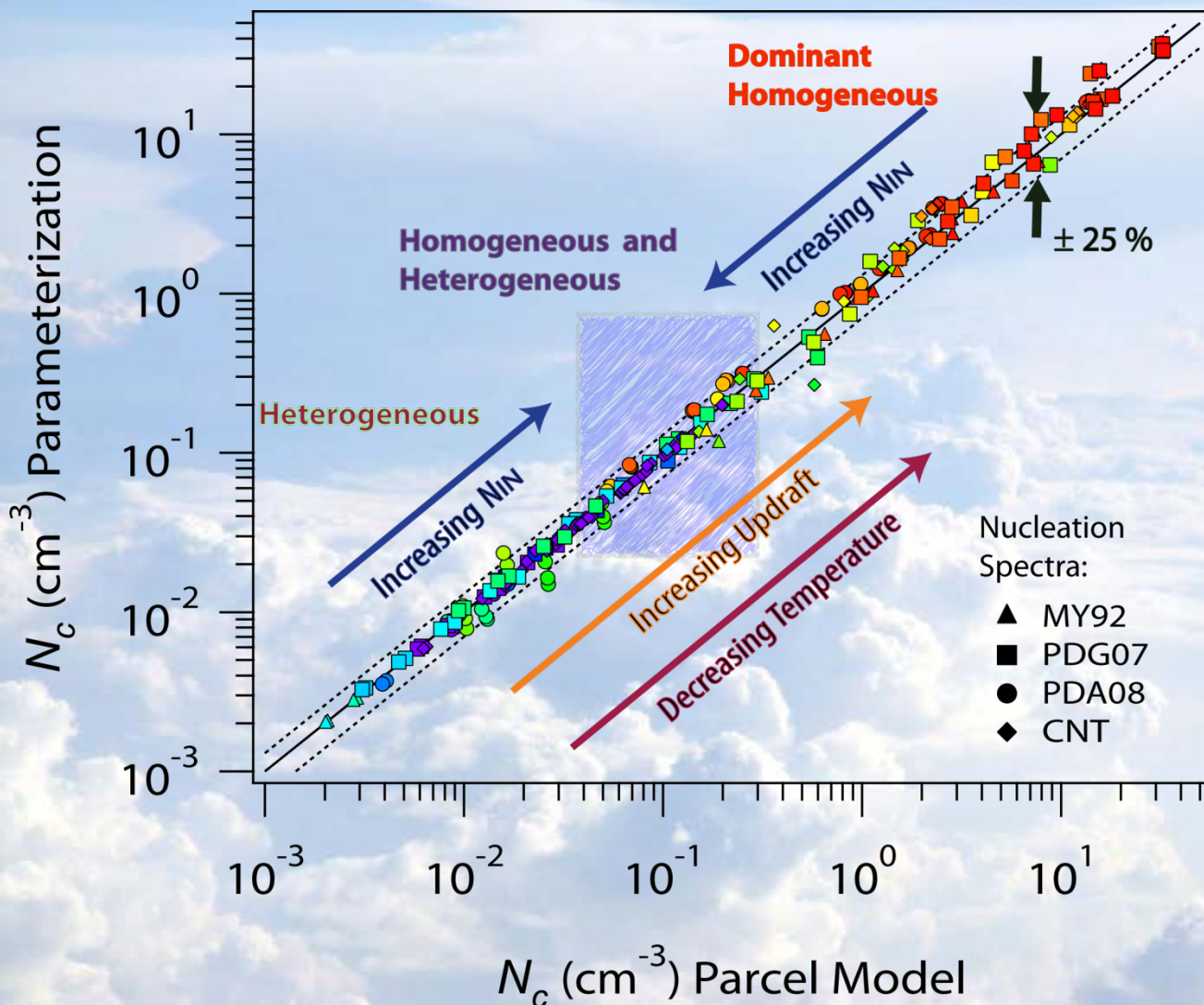
Condensation  
integral



Barahona and Nenes, *ACP*, 2008,2009ab.

- Simple and physically based. Completely theoretical and analytical (i.e., robust). **Very fast!**
- Accounts for homogeneous and heterogeneous freezing
- Works with a general definition of heterogeneous freezing:
  - Can take into account the contribution from several freezing modes and aerosol species (i.e., ranges of freezing thresholds).
  - Allows direct incorporation of theoretical and empirical data into large scale models.

# Cirrus parameterization evaluation: Compare Against Numerical Solution



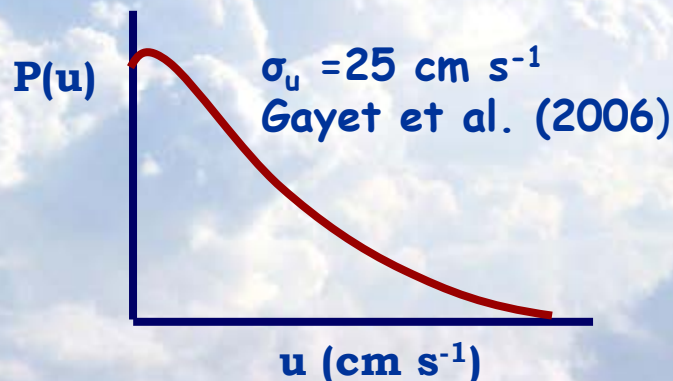
Average error over a broad range of conditions:  $5 \pm 12\%$ .

Orders of magnitude faster than the numerical solution

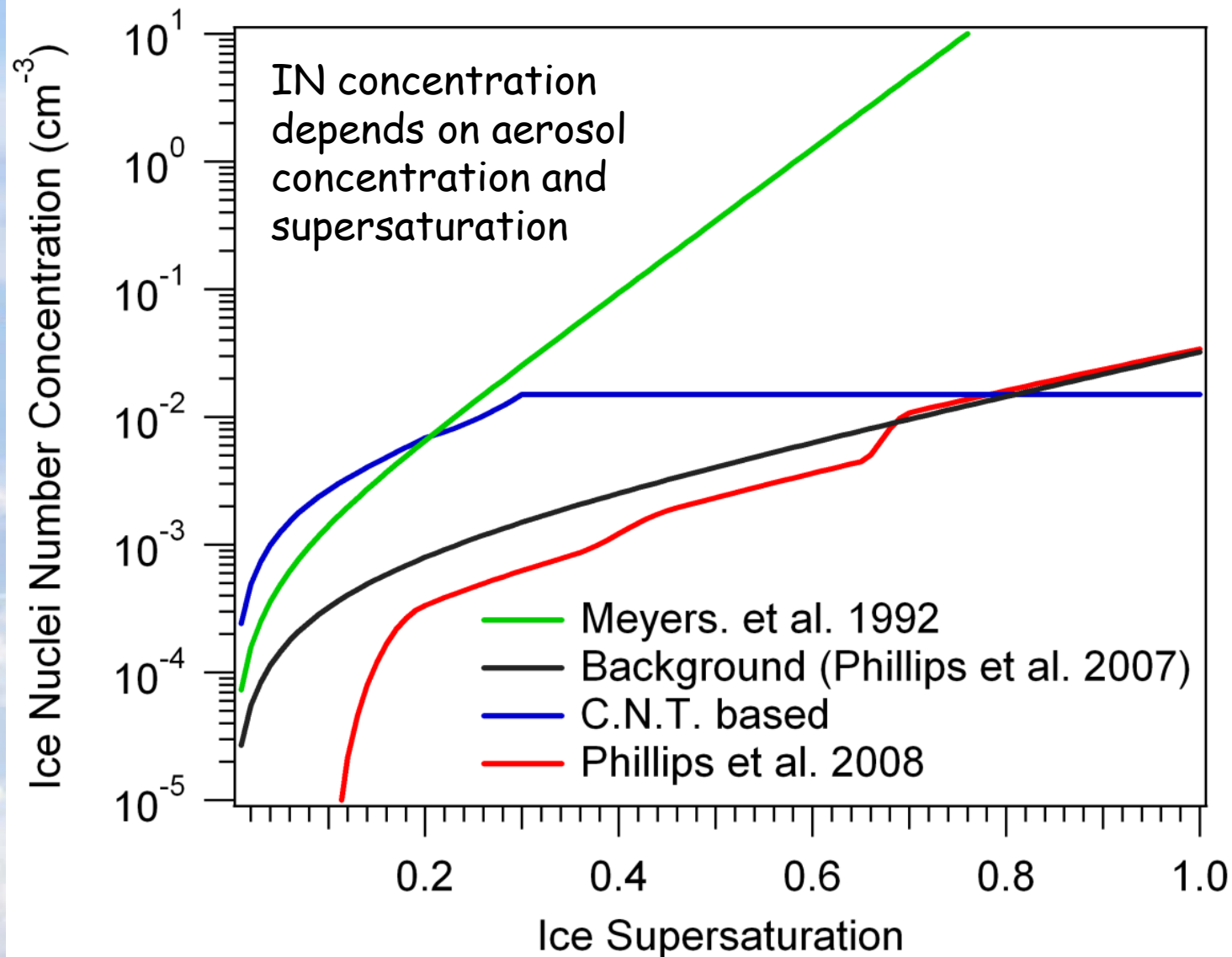
**In-situ datasets are much needed to evaluate these relationships.**

# Application: Sensitivity of global ice crystal concentration to IN

- NASA GMI Chemical and Transport Model.
- Aerosol model: Liu et al. (2005).
- Implementation:
  - Wind fields derived from GISS II' GCM
  - Dust and black carbon as IN precursors
  - Cirrus allowed for  $T < 235$  K. Time step 1h, resolution  $4^\circ \times 5^\circ$
- Dynamical forcing: Integrate over a Gaussian distribution of updraft velocities

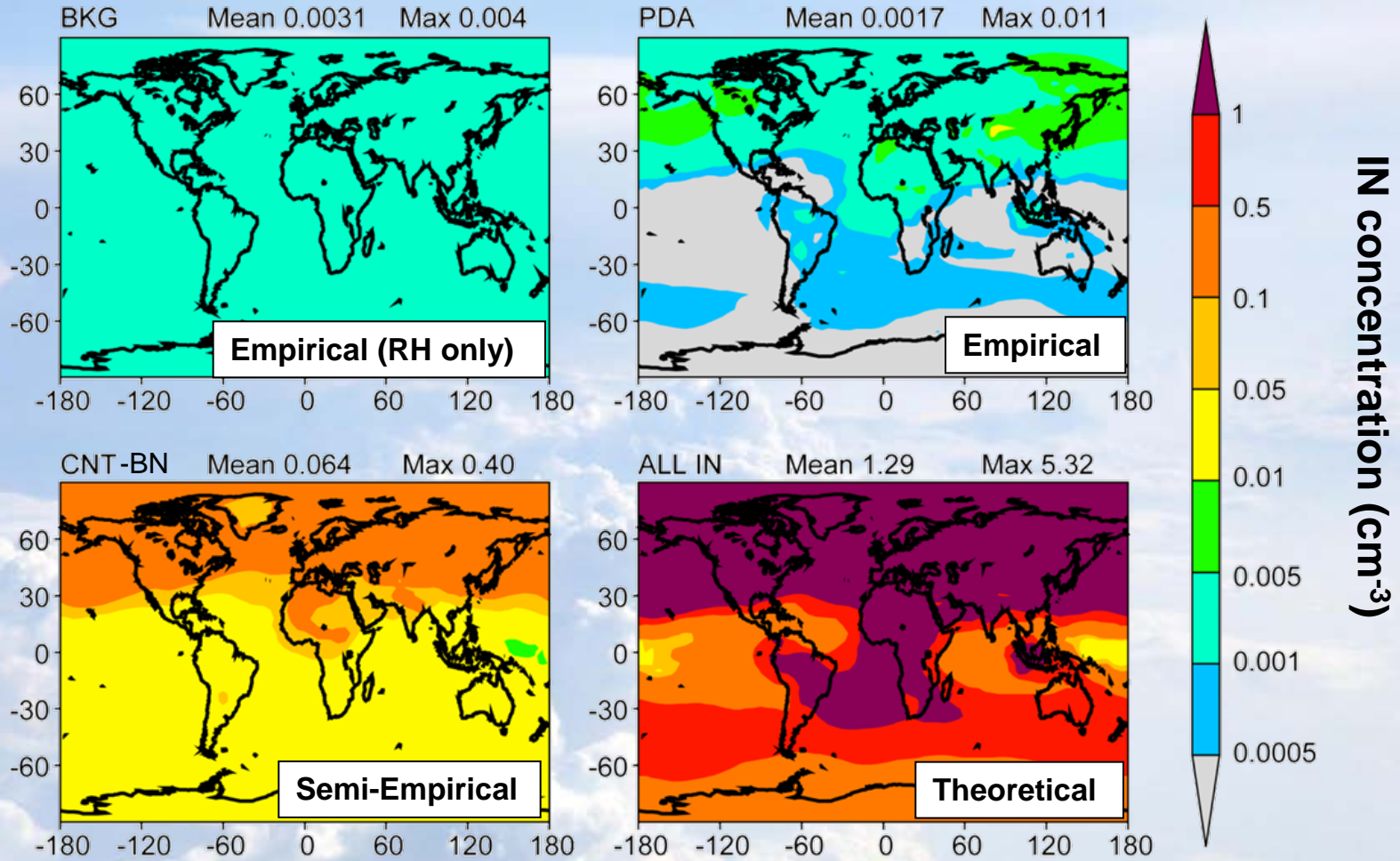


# Heterogeneous Freezing Spectra Considered



# Heterogeneous IN Concentrations

P = 281 hPa



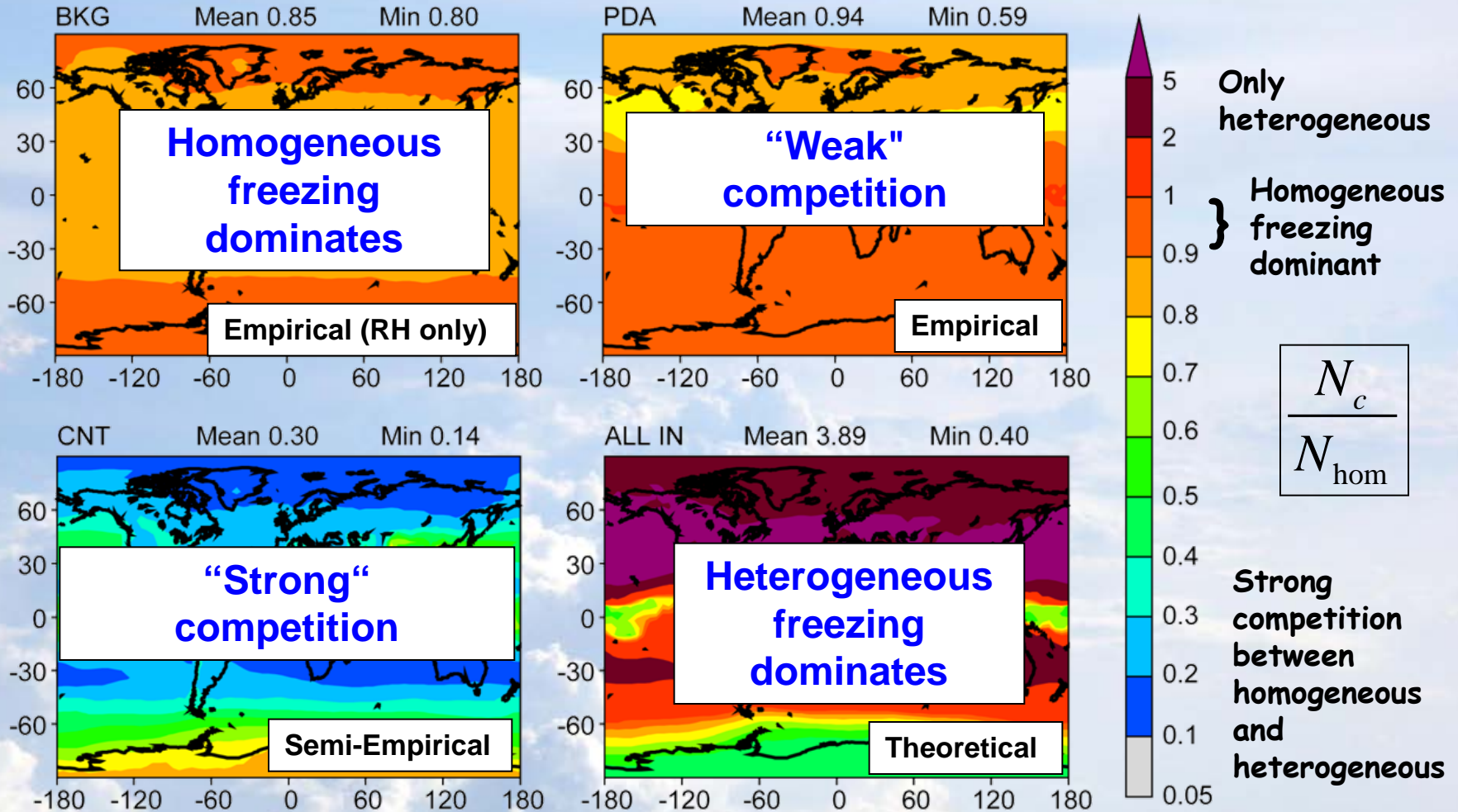
About three orders of magnitude difference in IN concentration  
Between IN parameterization expressions

Barahona, Rodriguez, and Nenes, JGR, 2010.



# IN impacts on Ice crystal number

P = 281 hPa



- A factor of 5-10 variation in global mean ice crystal concentration. Most significant in Northern Hemisphere

# Fast & Comprehensive Physics: Take-home messages

- Physically-based representations of droplet and ice formation in GCMs is now becoming sophisticated... but still very fast.
- With simplified aerosol composition treatment, activation parameterizations can do a good job of predicting  $N_d$  in ambient clouds.
- A simple treatment of entrainment/mixing of air seems to capture  $N_d$  in diabatic clouds (on average).
- Ice formation in cirrus can now be comprehensively treated, using either observational data or heterogeneous nucleation theory for IN predictions.
- These expressions need to be continuously evaluated with model/in-situ data (especially ice) but are very promising for linking aerosol with clouds.



**THANK YOU !!**

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