

Lagrangian studies of ice nucleation and growth in mixed-phase stratiform clouds

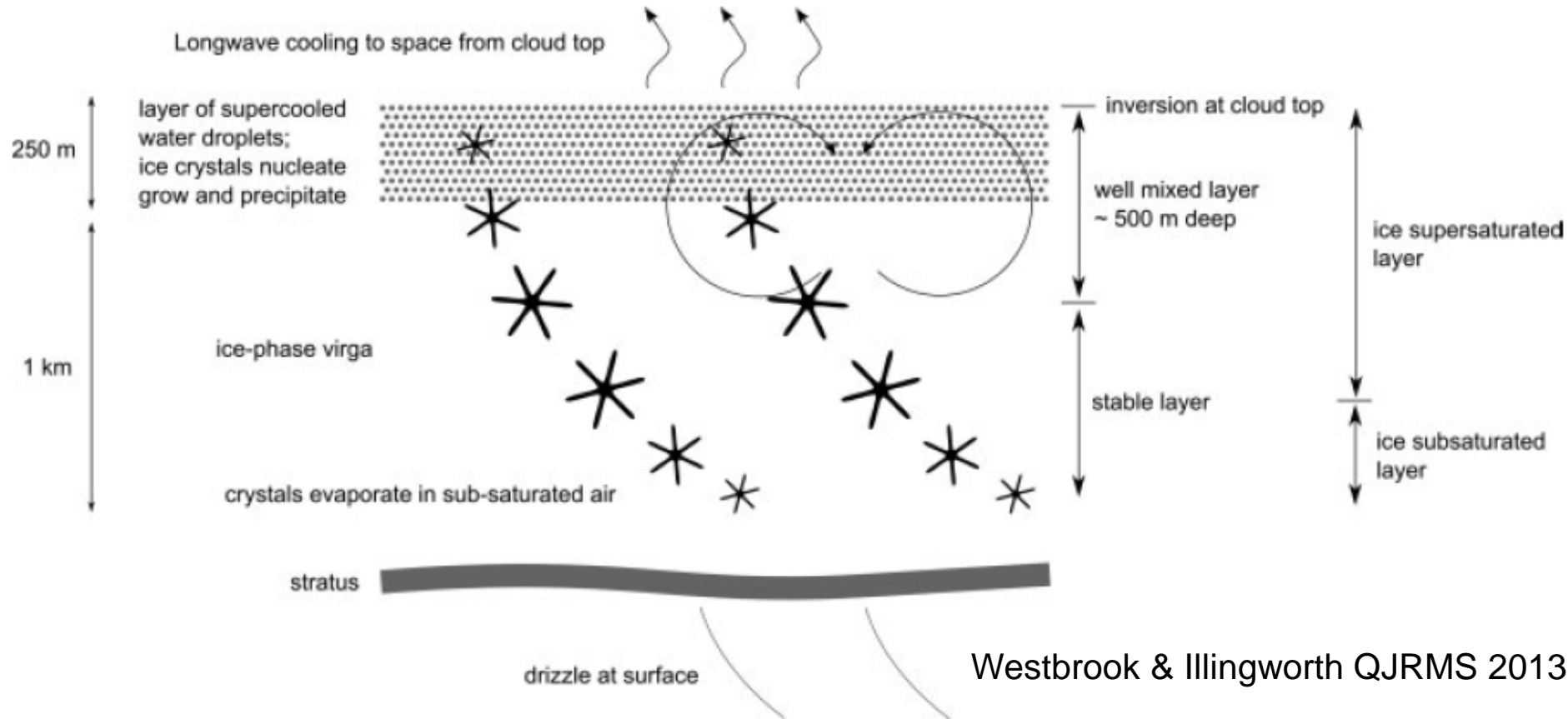
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Acknowledgements: DOE ASR

Mixed-phase stratiform clouds...



Arctic stratus & altocumulus clouds tend to be thin, long-lived, weakly precipitating ice, and radiatively important...

Question 1: Where do all the ice nuclei come from?

Question 2: How do the ice crystals get so big?

Simple model of ice nucleation and growth...

Objective: How simple can it be and still capture the essential physics?

1. Steady ice nucleation rate throughout cloud: $n'_i = \phi n_w / \tau$
2. Quasi-steady growth, with ice crystals falling out of an updraft only as fast as they can grow by vapor deposition: $v = \frac{h}{2r_i} \frac{dr_i}{dt}$
3. Steady state: rate of ice crystal precipitation equal to rate of crystal nucleation

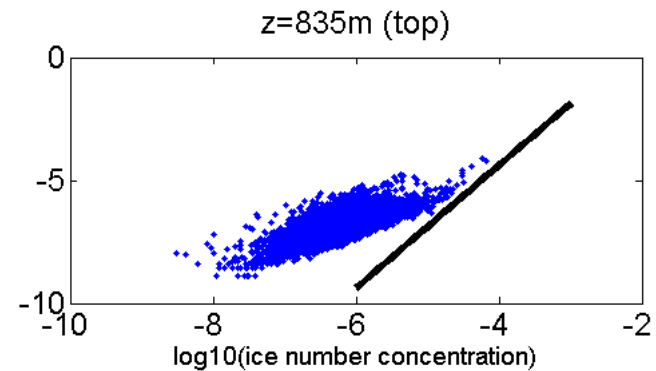
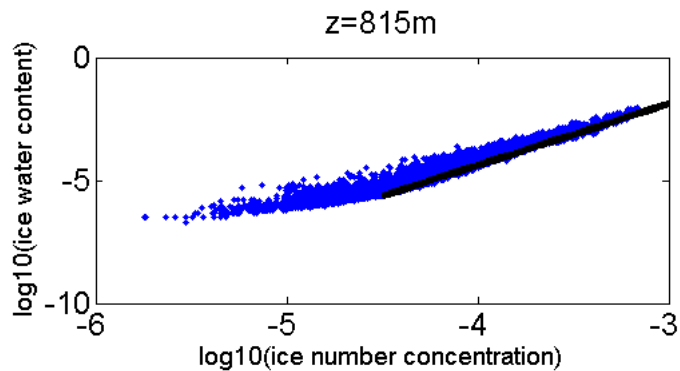
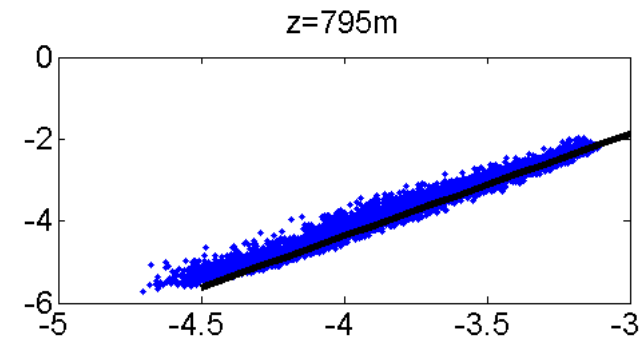
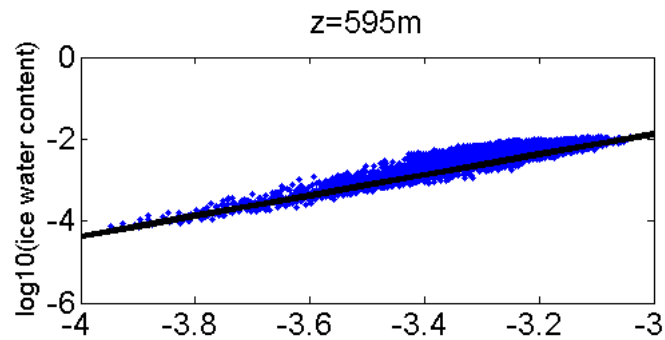
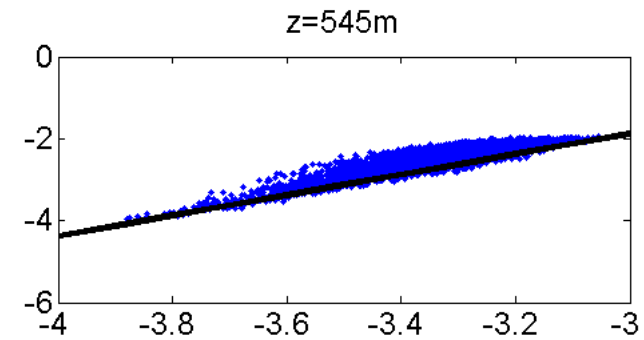
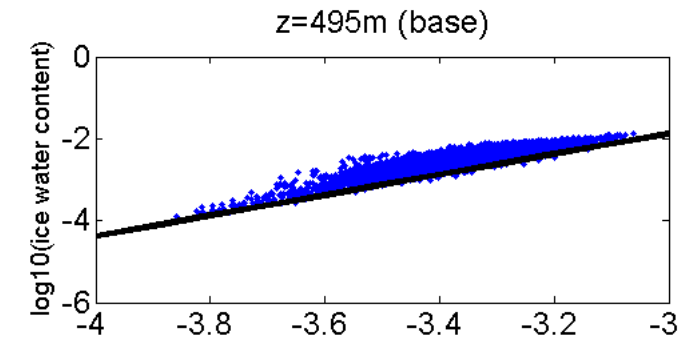
Using $IWC = n_i m_i$ simple model predicts

$$IWC = \frac{G' n_i^{5/2}}{n_i^{13/2}} \quad \text{with } G' = \frac{1}{6} \pi \rho_i (2CDs_i)^{3/2}$$

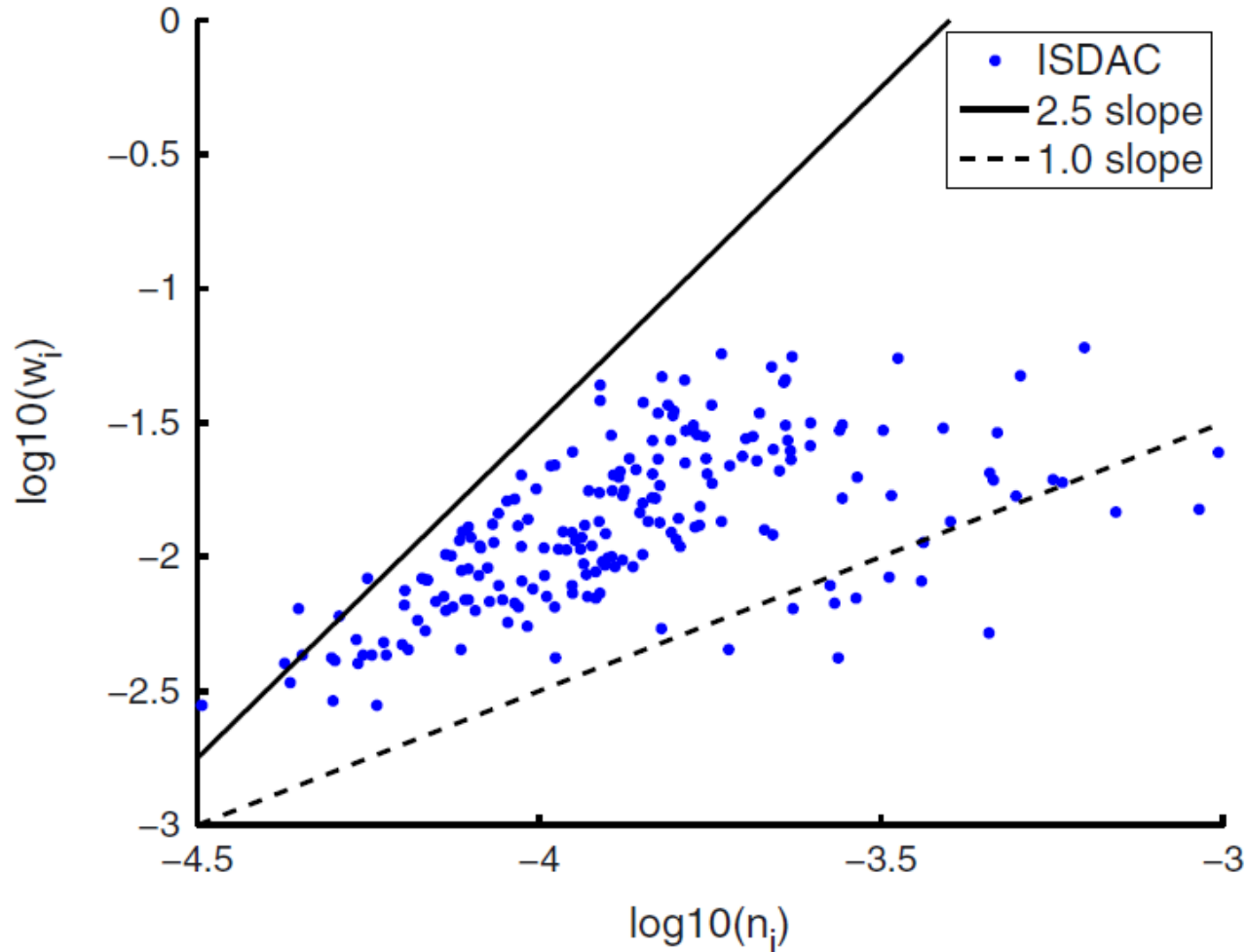
Note: 5/2 power law between ice mass and ice number...
with prefactor depending on ice nucleation rate

For more details, see: Yang, Ovchinnikov, and Shaw, *GRL*, **40**, 3756-3760 (2013)

IWC versus ice number concentration from LES...



IWC versus ice number for ISDAC observations...



For more details, see: Yang, Ovchinnikov, and Shaw, *GRL*, **40**, 3756-3760 (2013)

Questions leading to a Lagrangian view...

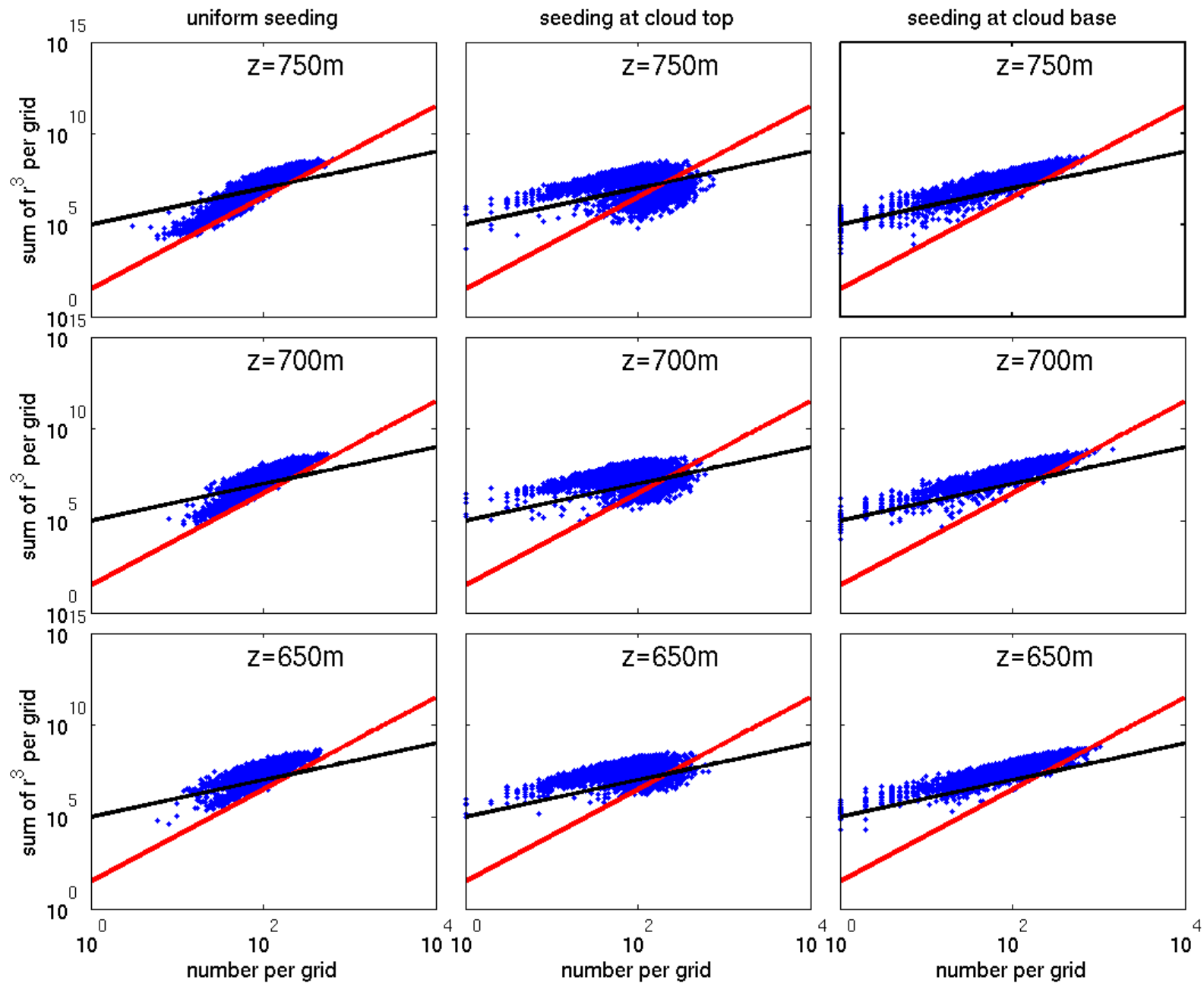
Questions about the 2.5 power law:

Is the volumetric, steady ice nucleation rate really necessary?

(e.g., what if ice nuclei are introduced from the cloud top or from the surface?)

Is the idealized, 1D concept of quasi-steady growth in an updraft observed in a fully 3D simulation?

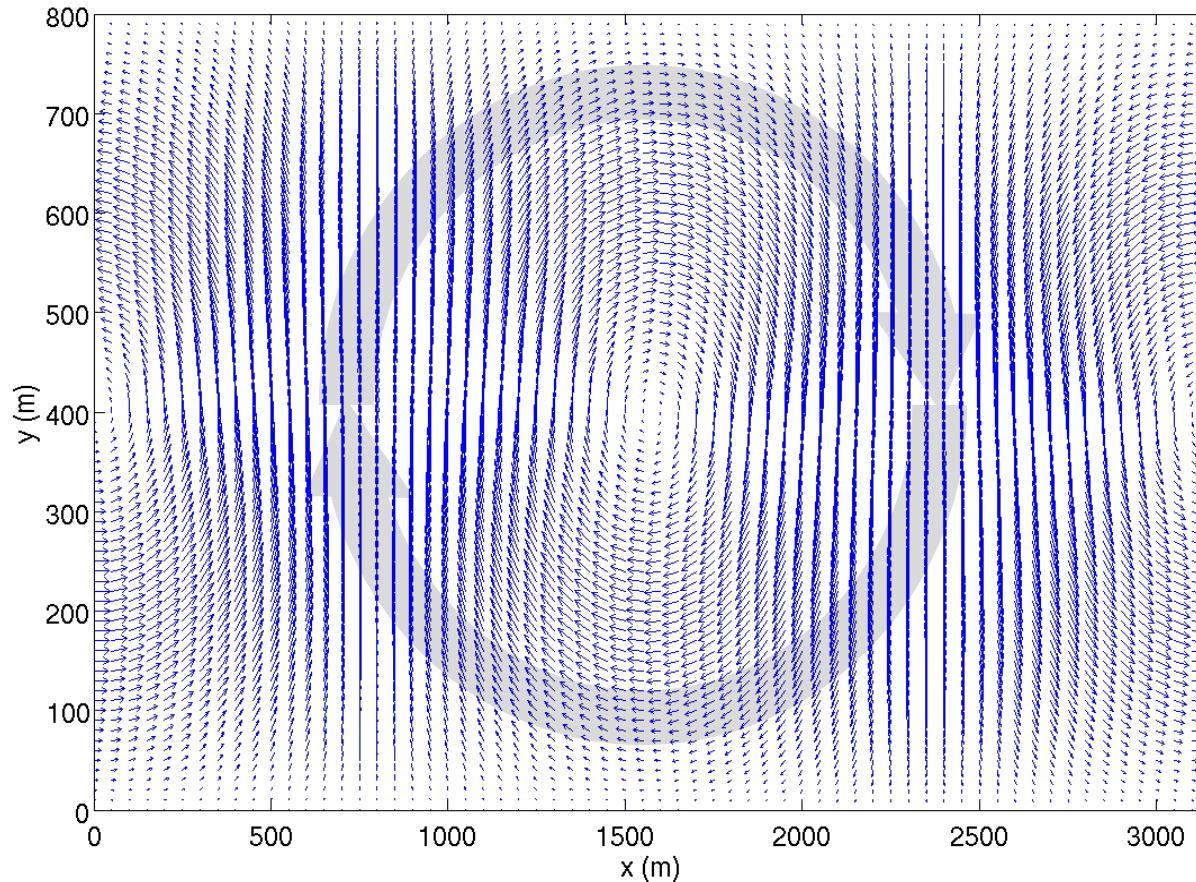
(related question... can the quasi-steady growth explain the presence of very large ice crystals that cannot form in a thin layer cloud without vertical velocities?)



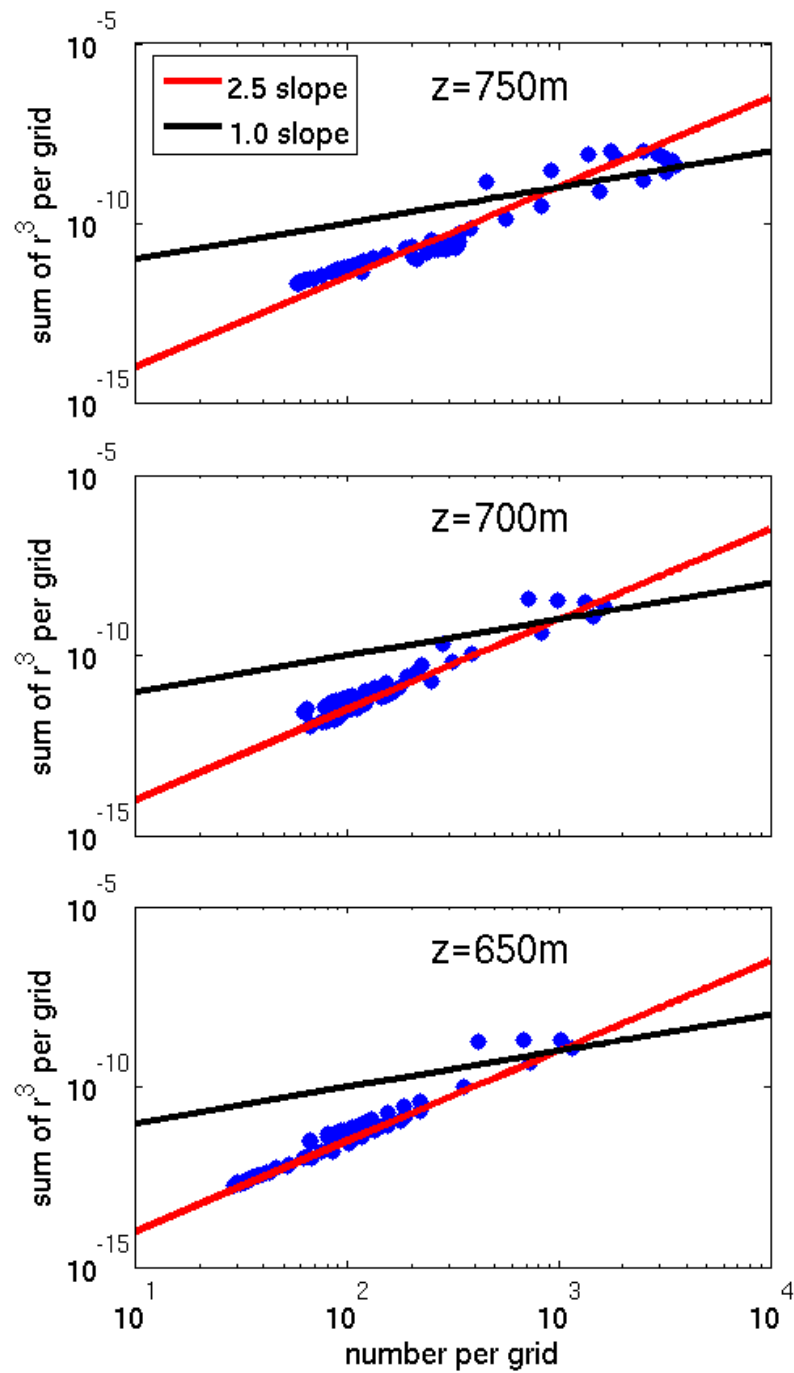
2D, time independent velocity field...

Maximum velocity: $u_0=v_0=2\text{m/s}$
Time independent

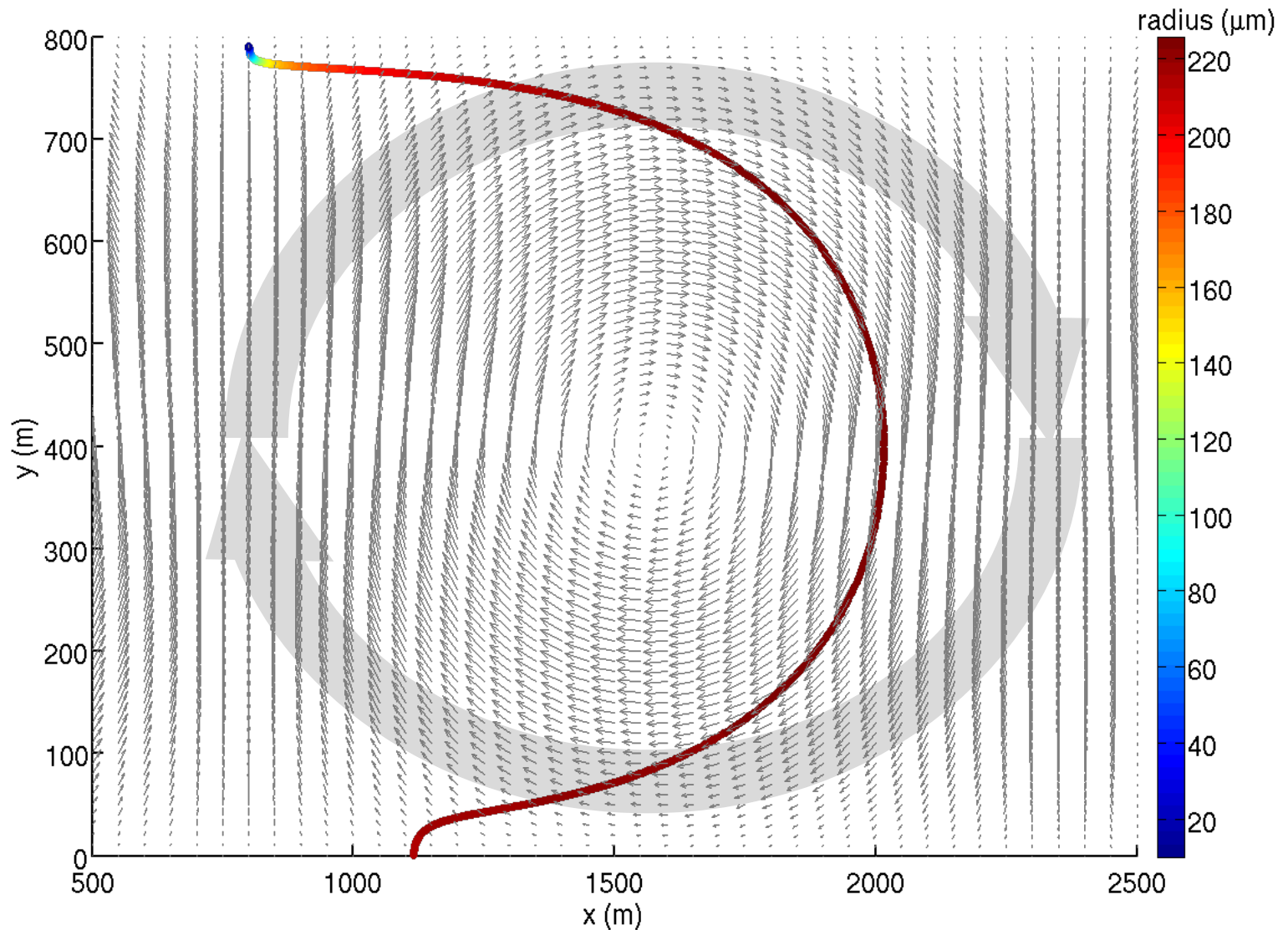
$$u = u_0 \sin(2\pi x/L) \cos(2\pi y/H)$$
$$v = -v_0 \cos(2\pi x/L) \sin(2\pi y/H)$$



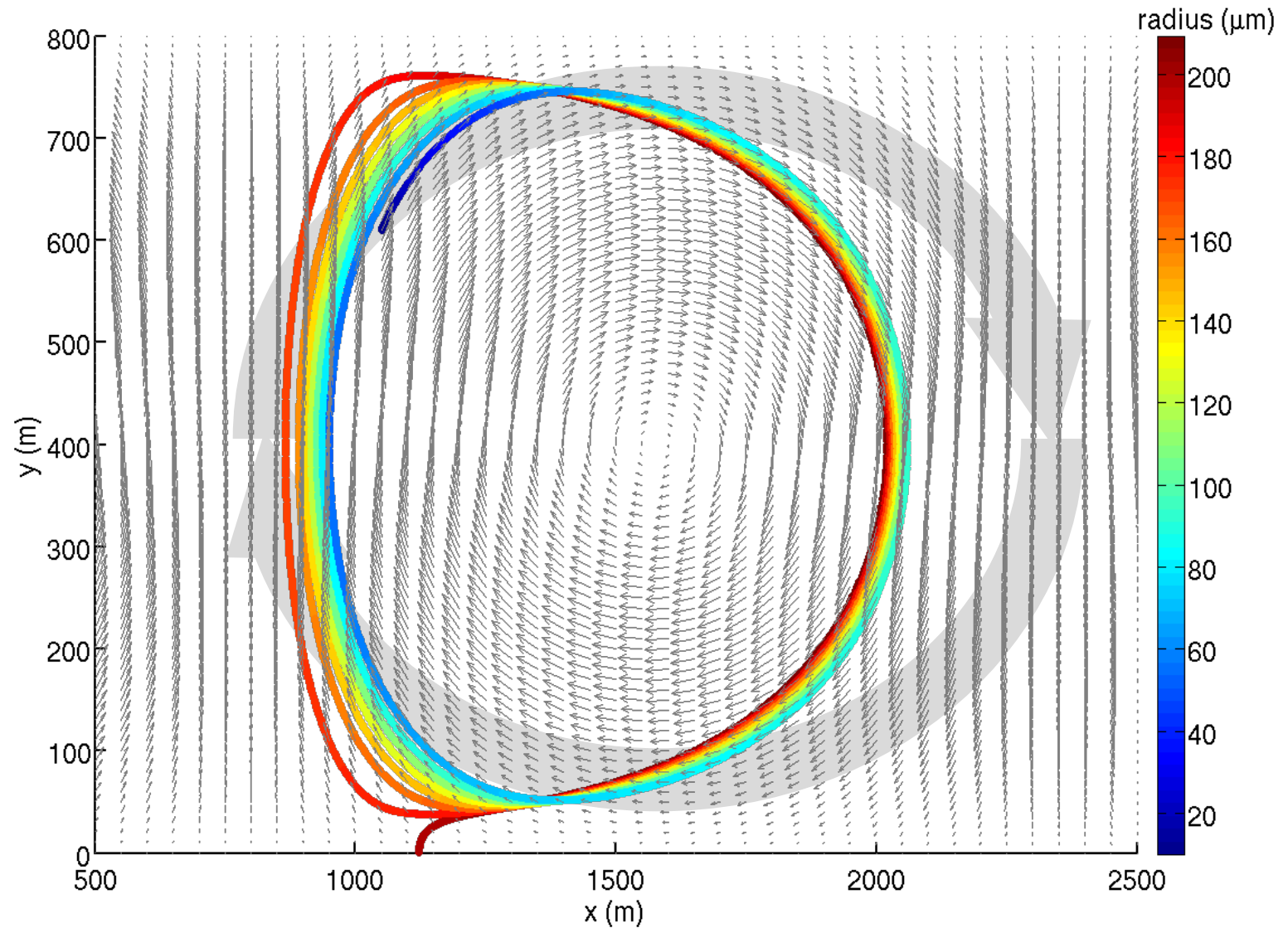
Inspired by Maxey and Corrsin (1986) and by Shipway and Hill (2012)



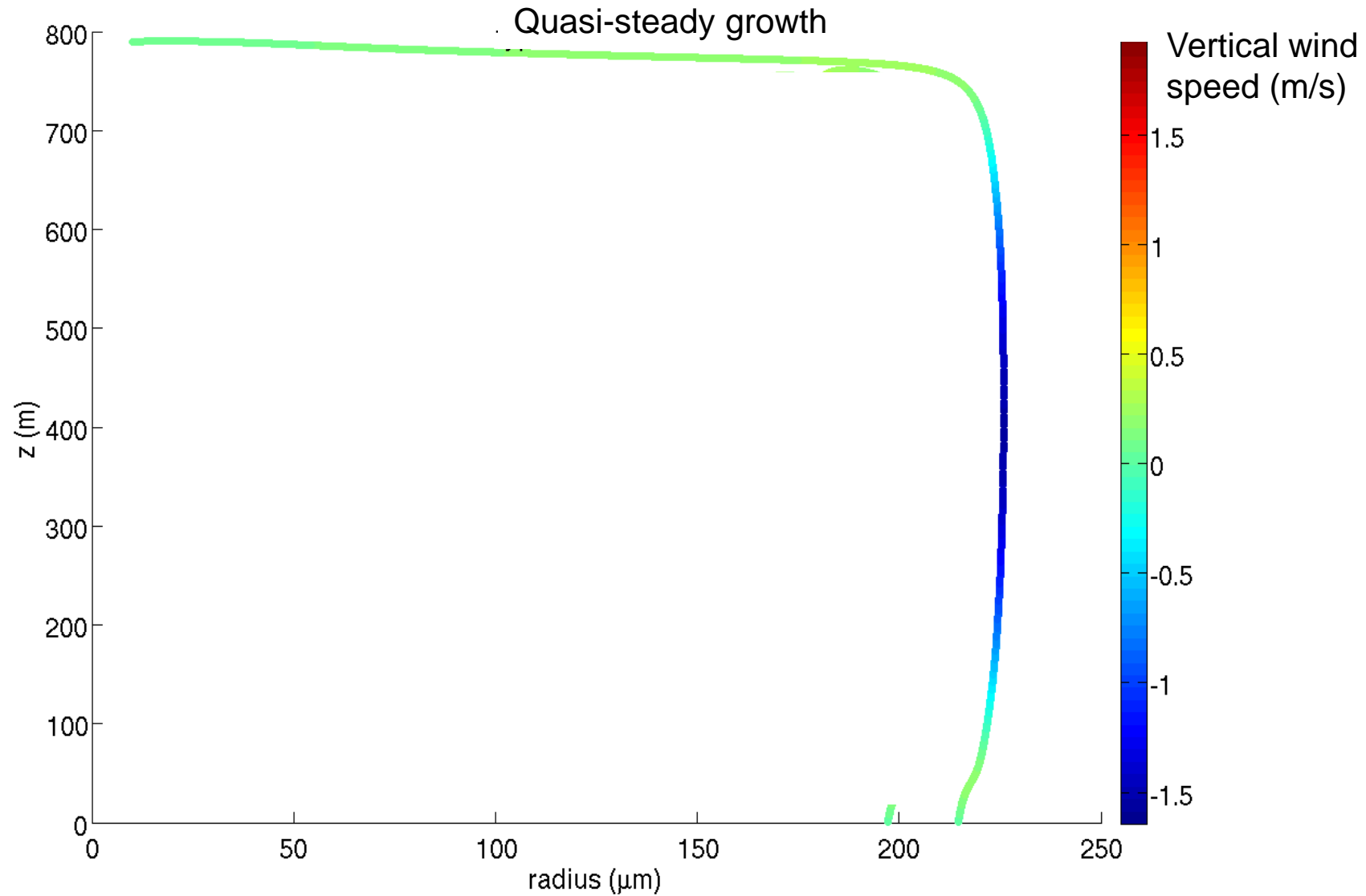
Lagrangian trajectories: quasi-steady growth...



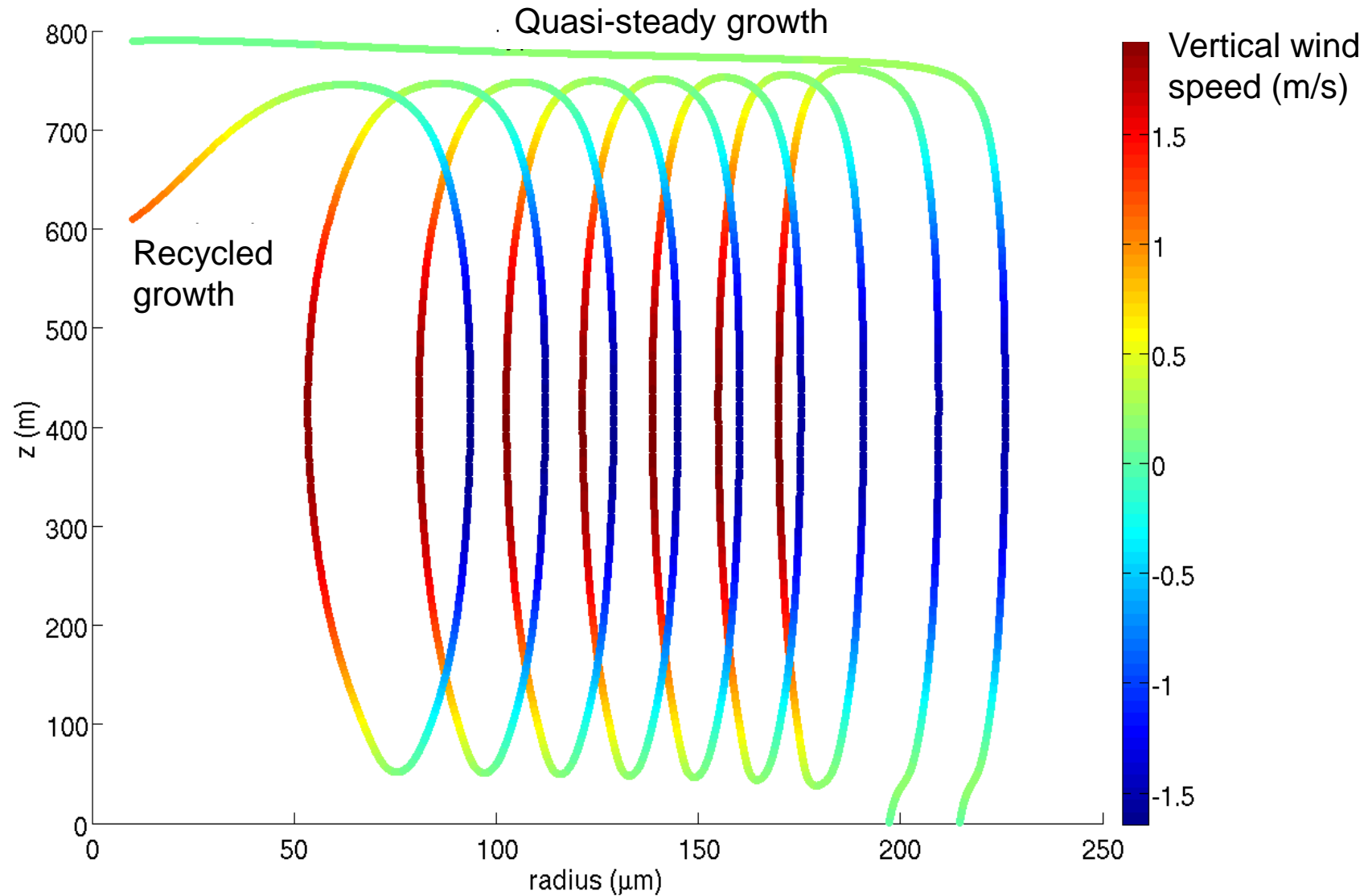
Lagrangian trajectories: recycled particles...



Trajectories in (r, z) coordinates...

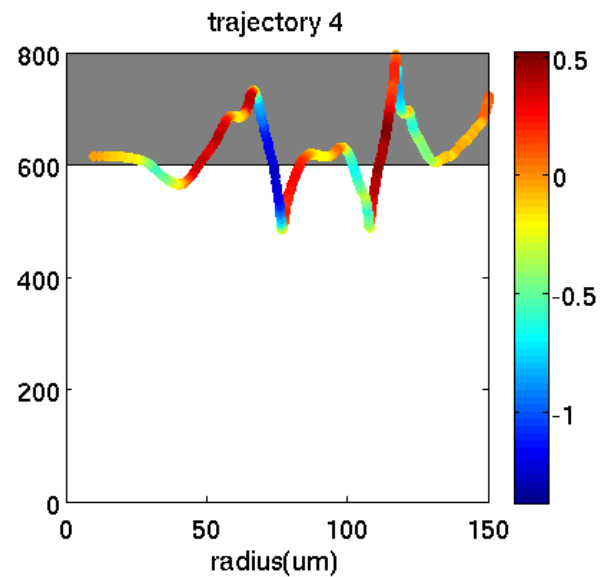
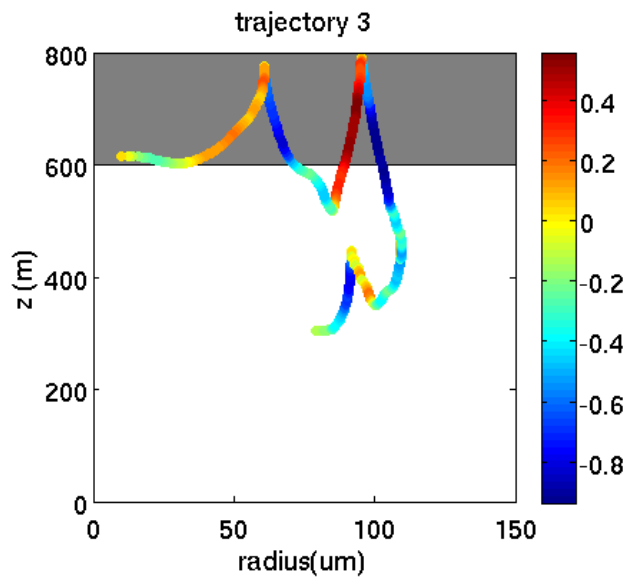
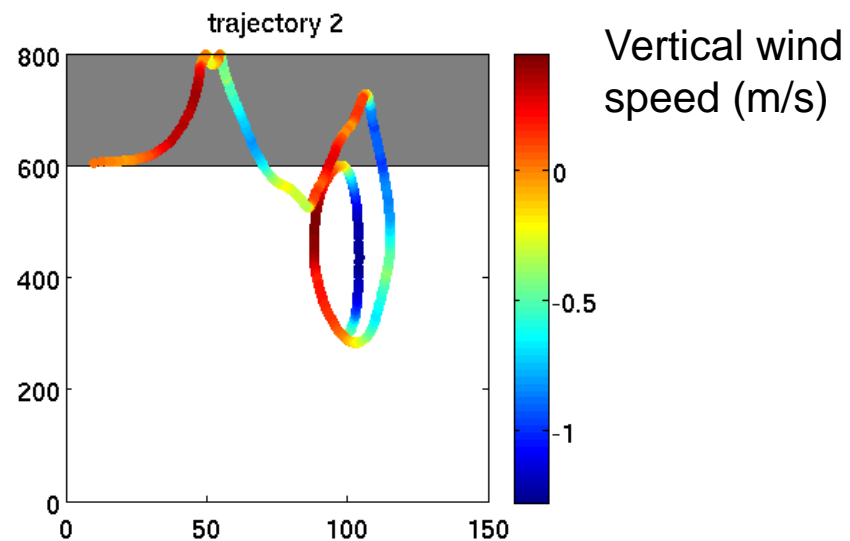
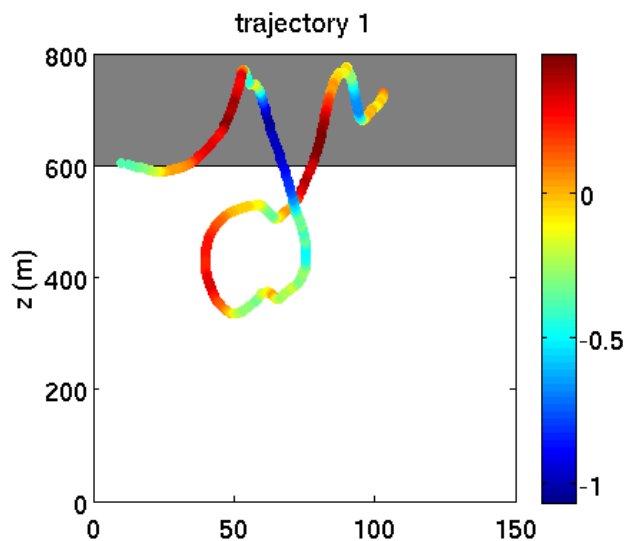


Trajectories in (r, z) coordinates...



(r, z) trajectories in the LES...

Shaded area:
Supercooled
liquid cloud



Summary...

A simple model including stochastic ice nucleation and ice growth

- **Quasi-steady** scenario in which crystals fall from the cloud only as fast as they can grow by deposition
- Power-law relationship between ice mass and number with **slope 2.5**
- Ice mass — ice number curve depends on the **nucleation rate**

Interpretation of model results and observations:

- LES with **IN source within liquid cloud** shows the predicted power law
- Ice crystals originating at **cloud top** or **cloud base** do not show the 2.5 power law
- Lagrangian tracks show surprising number of **long lifetime ice crystals**
- Idealized 2D cellular flow field allows us to study idealized trajectories
- Lagrangian trajectories show **quasi-steady growth**
- Lagrangian trajectories also show importance of **“recycled” ice crystals**
- LES trajectories show similar signatures for trajectories

For more details, see: Yang, Ovchinnikov, and Shaw, GRL, 40, 3756-3760 (2013)