

Estimating Raindrop Size Distributions and Vertical Motions using S-band & KAZR Vertically Pointing Radars

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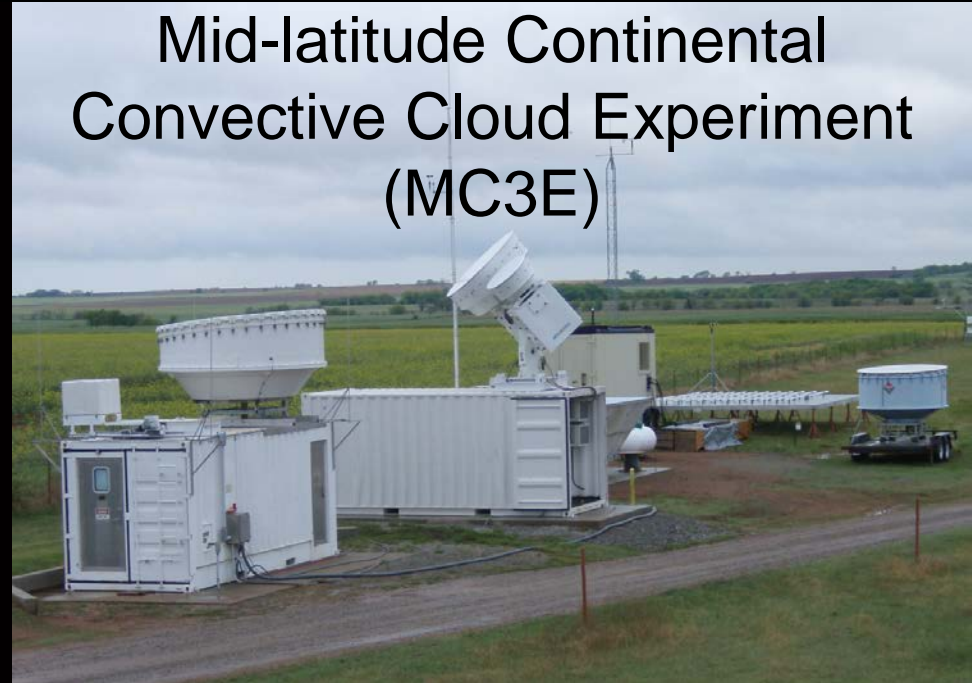
In partnership with

NOAA Earth System Research Laboratory (ESRL)



University of Colorado
Boulder

Mid-latitude Continental Convective Cloud Experiment (MC3E)



Support for this work:

DOE ASR Grant: DE-SC0007080

NASA PMM Grant: NNX13AF89G

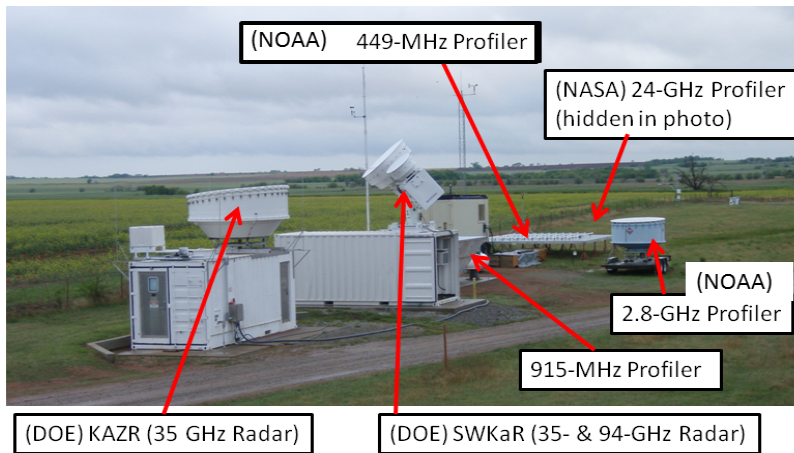


Research Objectives

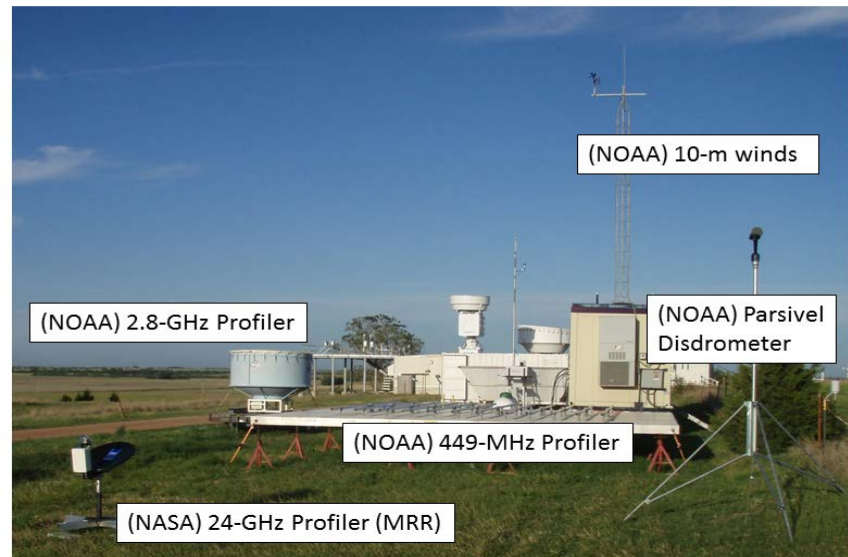
- Goal
 - Estimate profiles of vertical air motion and raindrop size distributions (DSDs) using two non-synchronous and non-beam matched vertically pointing profilers
- Approach
 - Exploit the different backscattering signatures at Ka-band (KAZR) and S-band
 - ***KAZR – non-Rayleigh (also, non-Bragg)***
 - ***S-band – Rayleigh***
- Key Results
 - Air motion & DSD retrievals in rain
 - Retrievals independent of radar calibration
 - N_w and rain rate dependent on S-band calibration

MC3E Profiling Radar Deployment

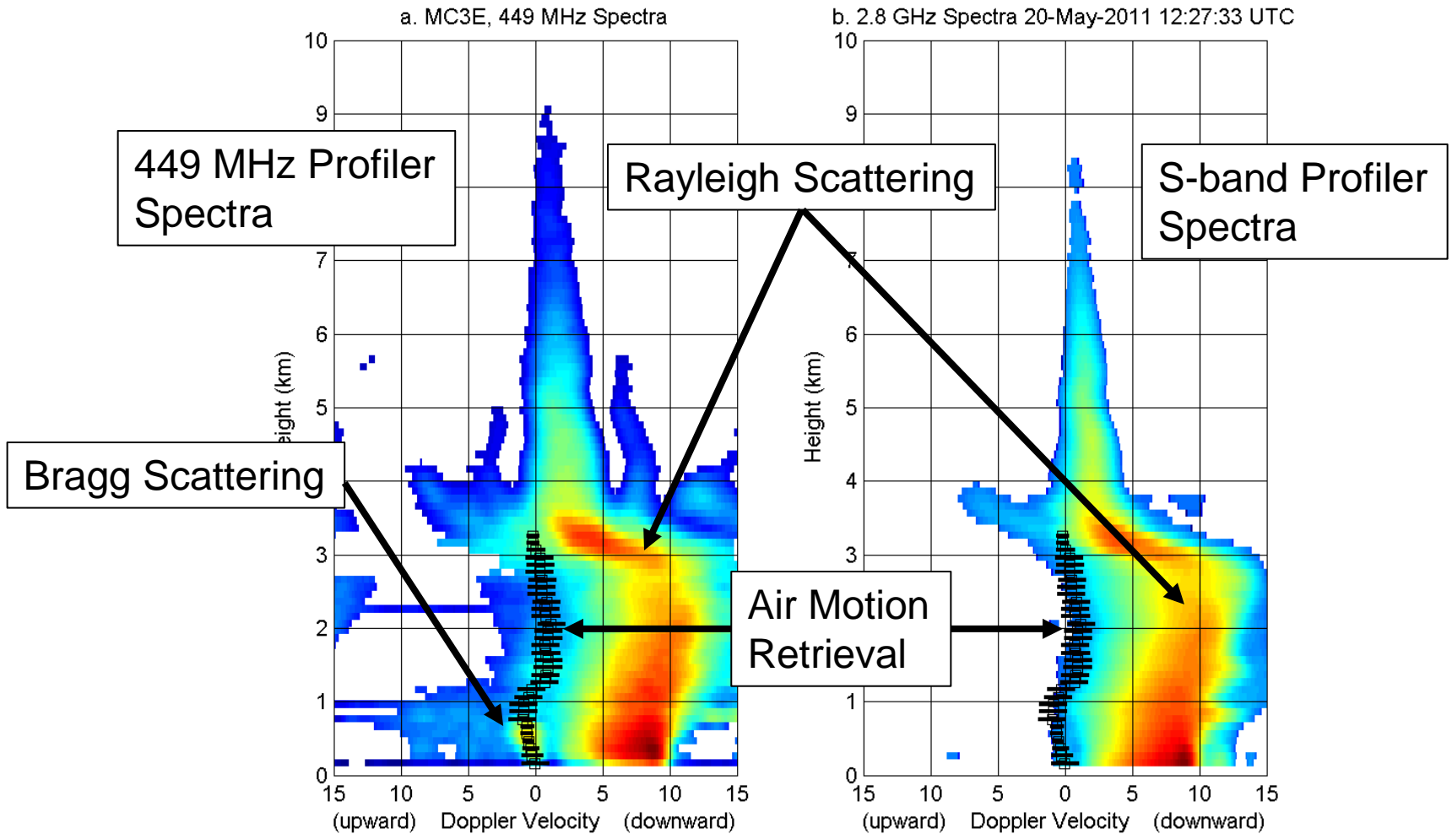
Radars deployed in Mid-latitude Continental Convective Cloud Experiment (MC3E)
22 April – 6 June 2011

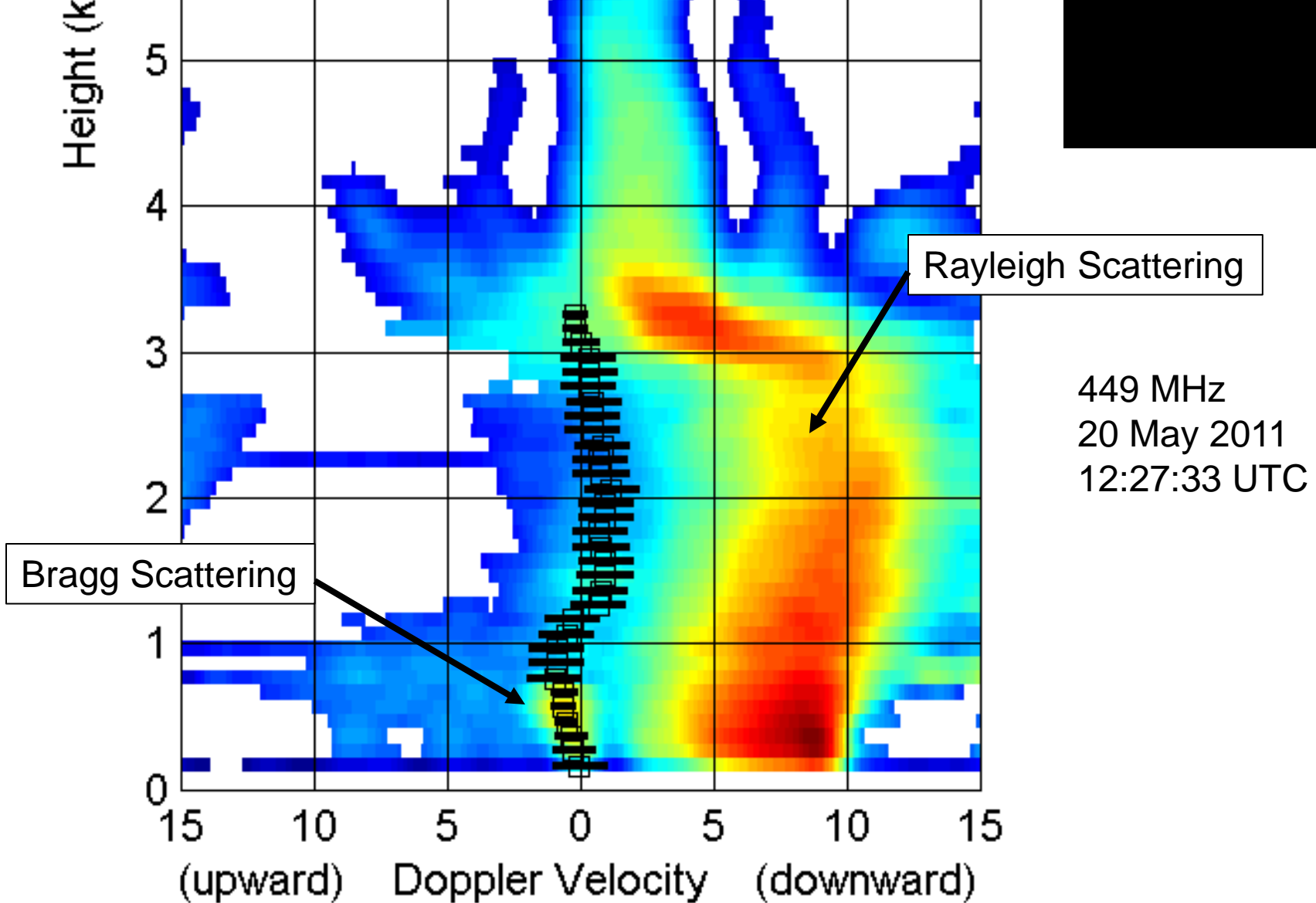


Radars deployed in Mid-latitude Continental Convective Cloud Experiment (MC3E)
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Dual Frequency Air Motion Retrieval





1-Minute Dwell – Pros & Cons

Profiles from KAZR and S-band radars are:

- *not simultaneous*
- *not matched beams*

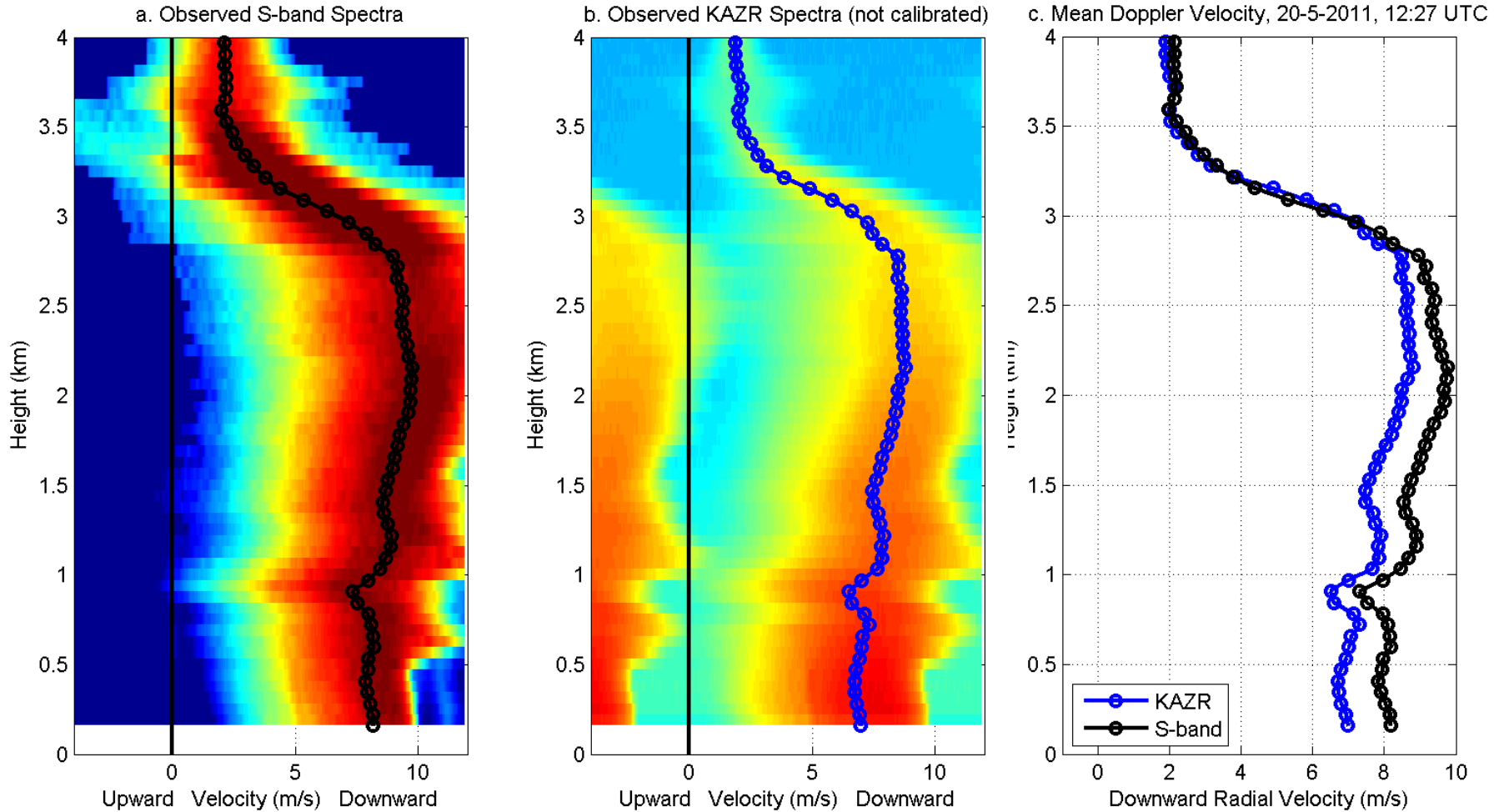
Average spectra for 1-minute

- *Represent larger spatial domain*
- *Cannot represent the turbulence within pulse volume*

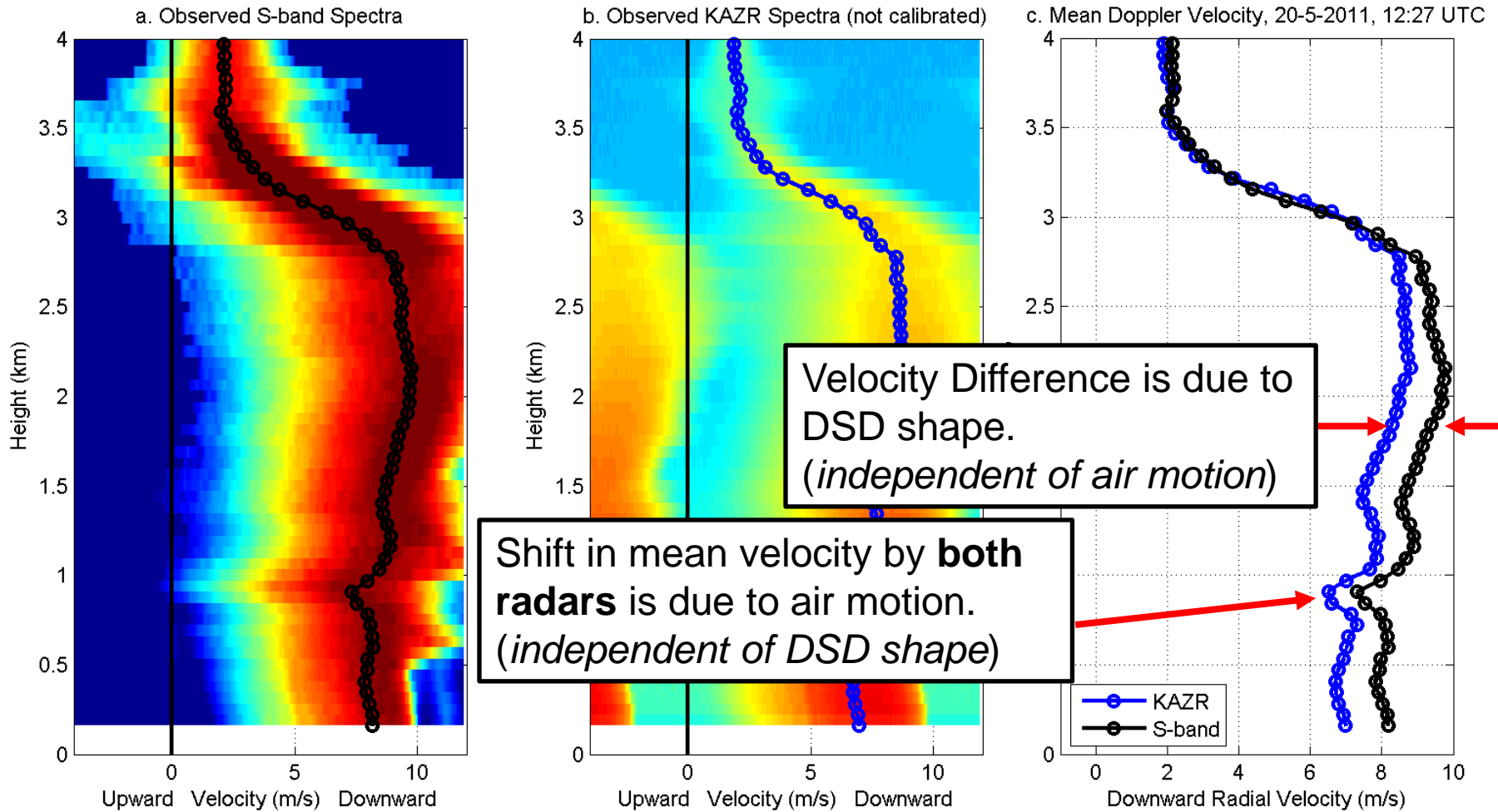
Number of profiles per 1-minute dwell:

- *KAZR – 17 profiles per minute*
- *S-band – 7 profiles per minute*

Observed Doppler Velocity Spectra



Observed Doppler Velocity Spectra



Mean Doppler Velocity

DSD (scaled PDF): $N(D; N_w, D_m, \mu) = N_w f(D; D_m, \mu)$

'Intensity'

'quasi PDF'

Radar Weighted Fall Velocity:

$$S_{hydro}(v; N_w, D_m, \mu) = N_w f(D; D_m, \mu) \sigma_{backscatter}(D) g(D, v)$$

Diameter-to-fall conversion

Mean Hydrometer Fall Velocity:

$$V_{hydro}(D_m, \mu) = \frac{\int S_{hydro}(v; D_m, \mu) v dv}{\int S_{hydro}(v; D_m, \mu) dv}$$

Measured Velocity (Doppler Velocity):

$$V_{measured} = \frac{\int_{v_{min}}^{v_{max}} S(v) v dv}{\int_{v_{min}}^{v_{max}} S(v) dv} = V_{hydro}(D_m, \mu) - W$$

Difference in Doppler Velocity (DDV)

Mean Doppler Velocities: $V_{measured}^{Sband} = V_{hydro}^{Sband}(D_m, \mu) - W$

$$V_{measured}^{KAZR} = V_{hydro}^{KAZR}(D_m, \mu) - W$$

Difference in Doppler Velocities (DDV):

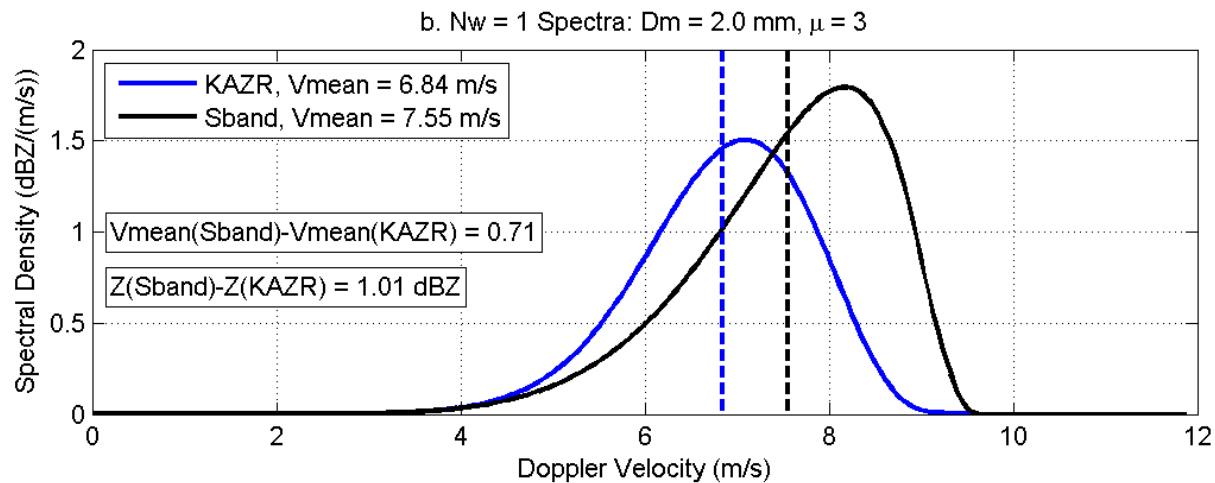
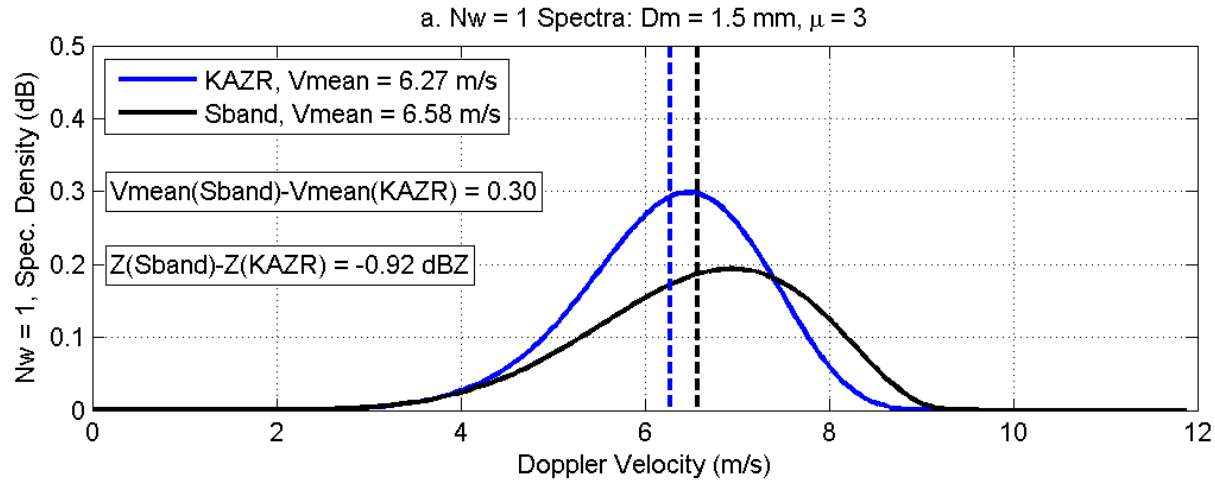
$$DDV = V_{measured}^{Sband} - V_{measured}^{KAZR}$$

$$DDV = V_{Hydro}^{Sband}(D_m, \mu) - V_{Hydro}^{KAZR}(D_m, \mu)$$

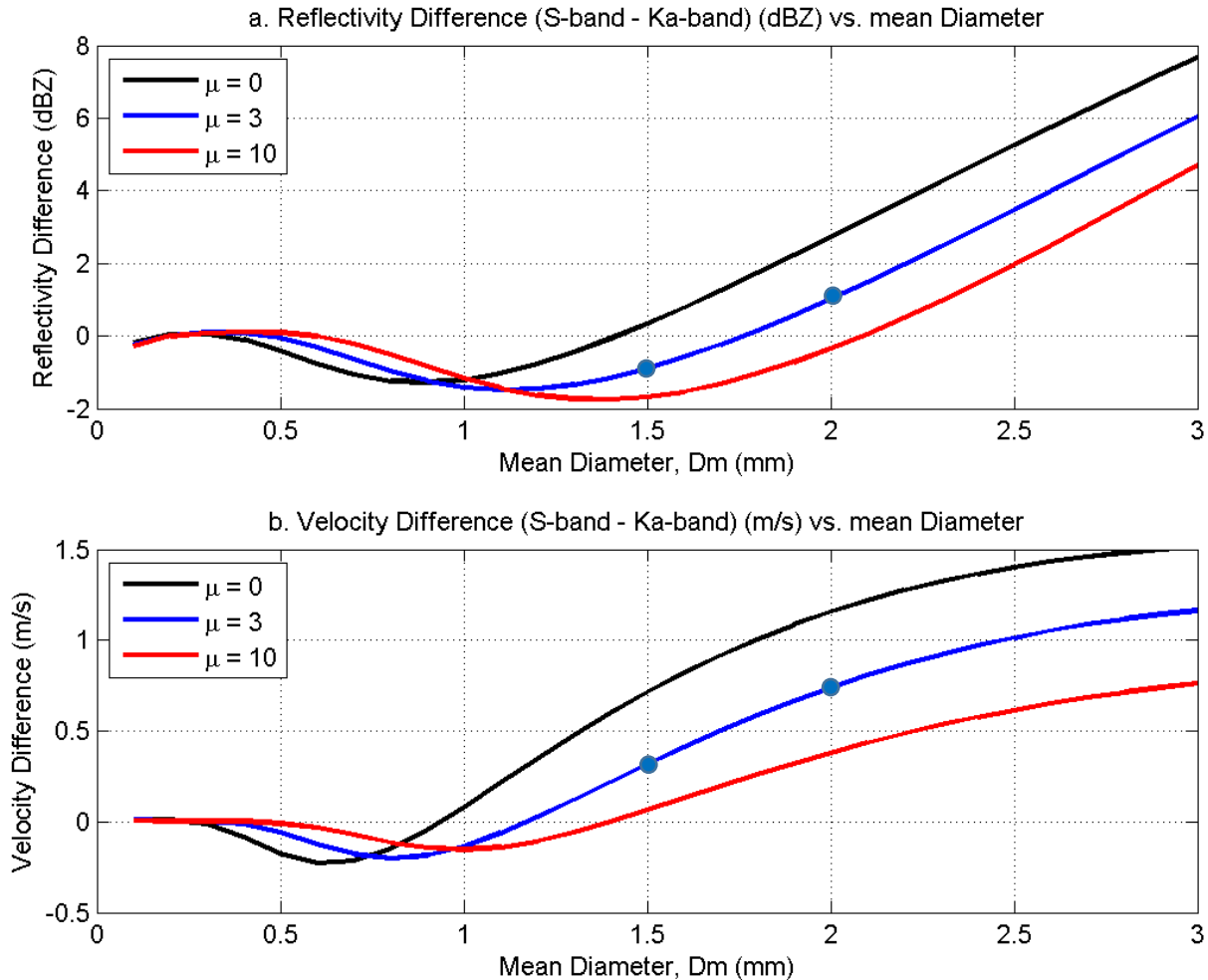
Bottom line:

Difference in Doppler velocity (DDV) is independent of air motion and only dependent on the shape of the DSD.

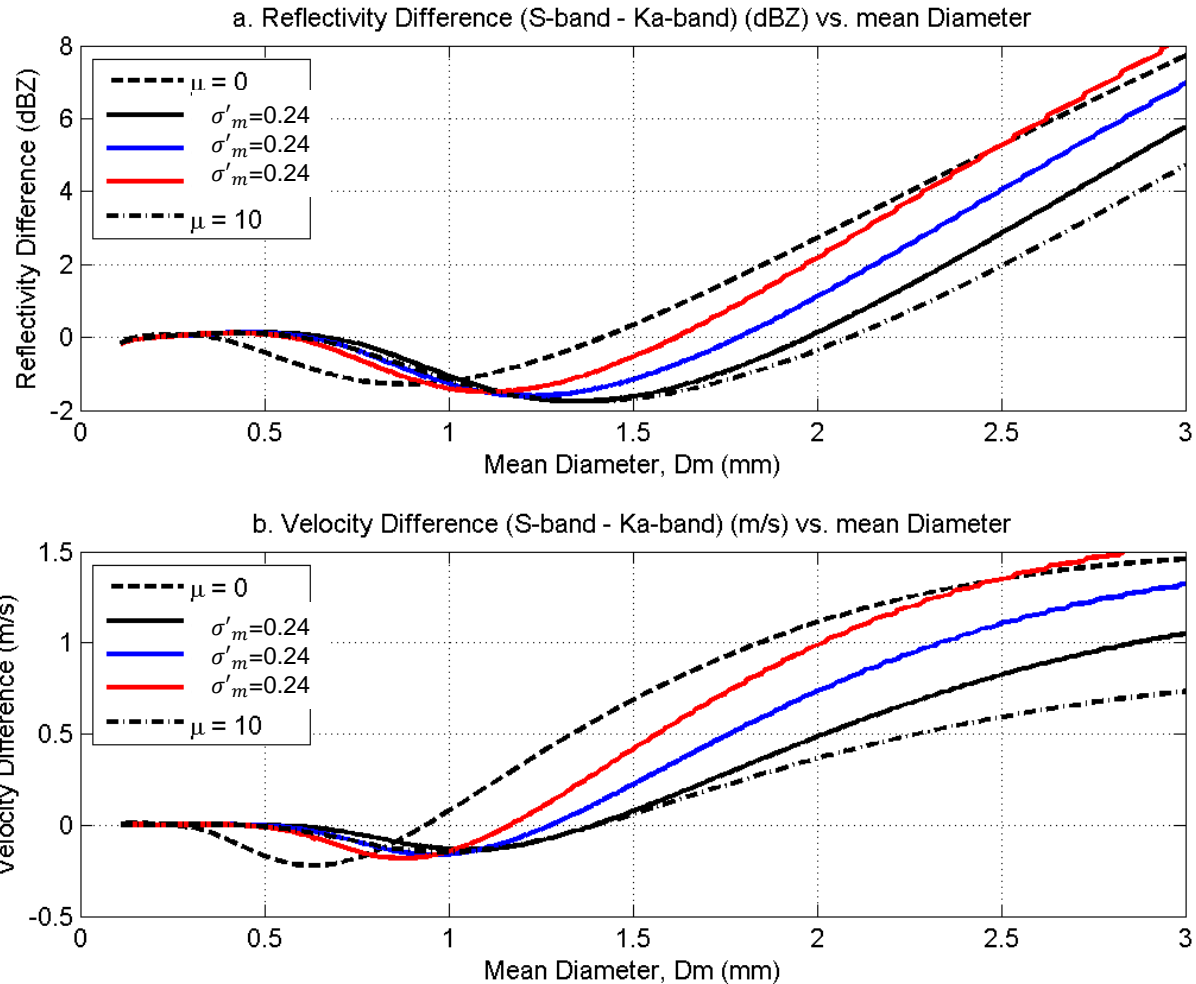
Simulated Doppler Spectra



DFR and DDV vs. Mean Diameter



DFR & DDV with Norm. Breadth



Retrieval Sequence

Two Measurements:

KAZR Doppler Velocity

Sband Doppler Velocity

Three Unknowns:

Air motion (W)

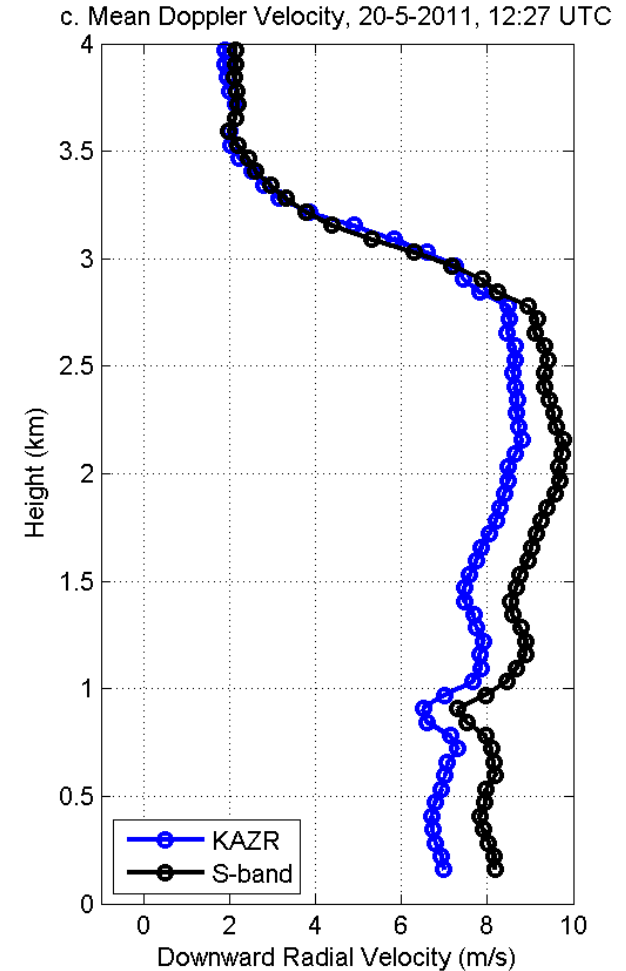
Mean Diameter (D_m)

Breadth Parameter (σ'_m)

Assumptions:

Zero air motion at lowest range gate

Breadth Parameter constant with ht



Retrieval Sequence

Two Measurements:

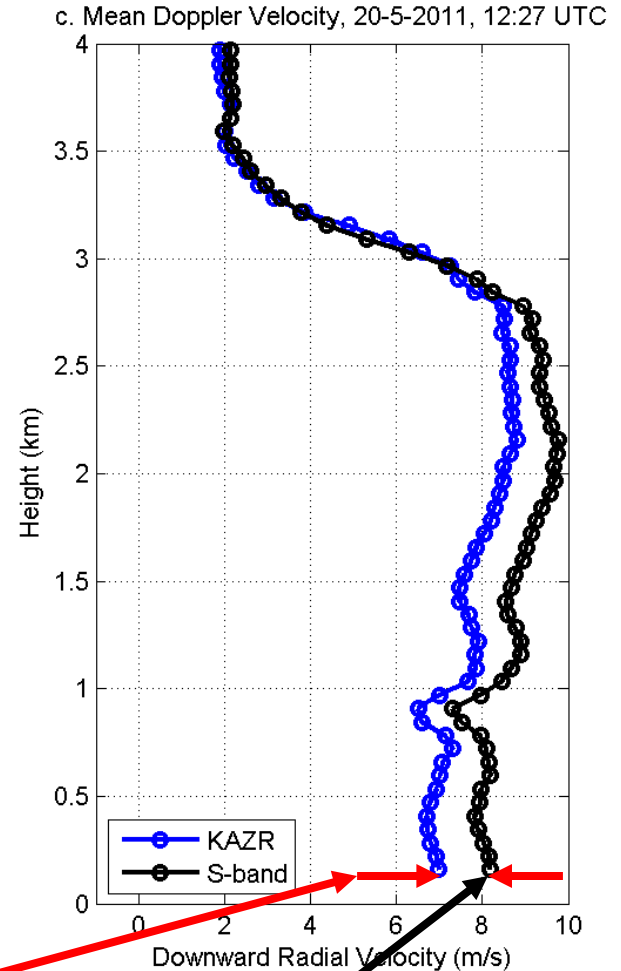
KAZR Doppler Velocity
Sband Doppler Velocity

Three Unknowns:

Air motion (W)
Mean Diameter (D_m)
Breadth Parameter (σ'_m)

Assumptions:

Zero air motion at lowest range gate
Breadth Parameter constant with ht

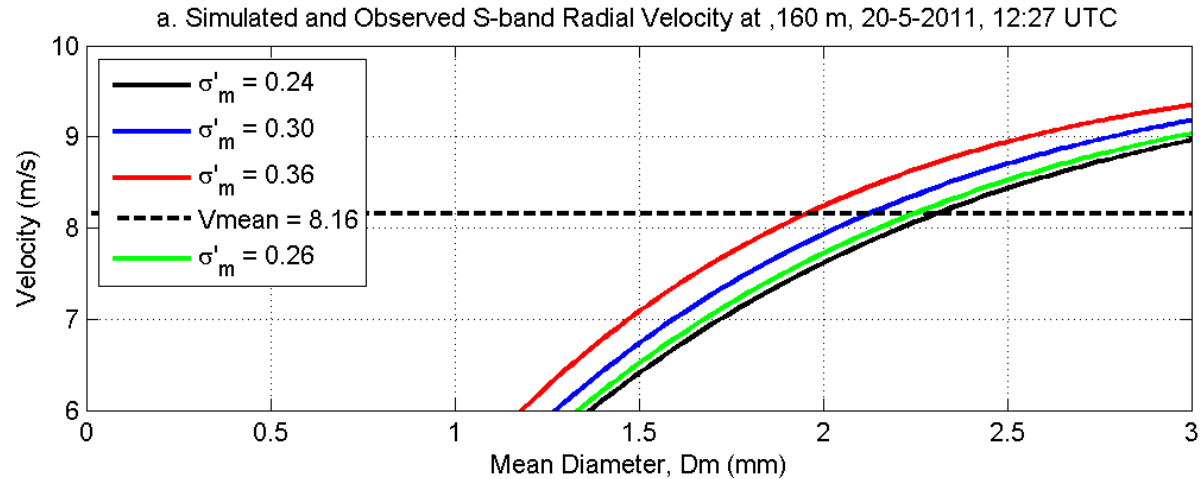


$$DDV = 0.79 \text{ m/s}$$

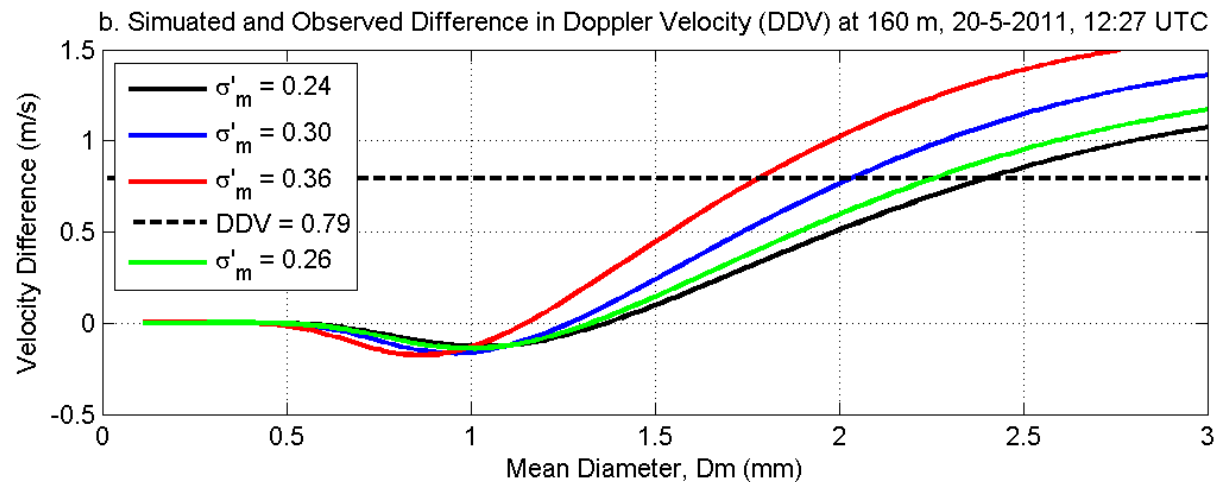
$$V_{measured}^{Sband} = 8.1 \text{ m/s}$$

Step #1: Lowest range gate (160 m)

$$V_{measured}^{Sband} = 8.16 \text{ m/s}$$

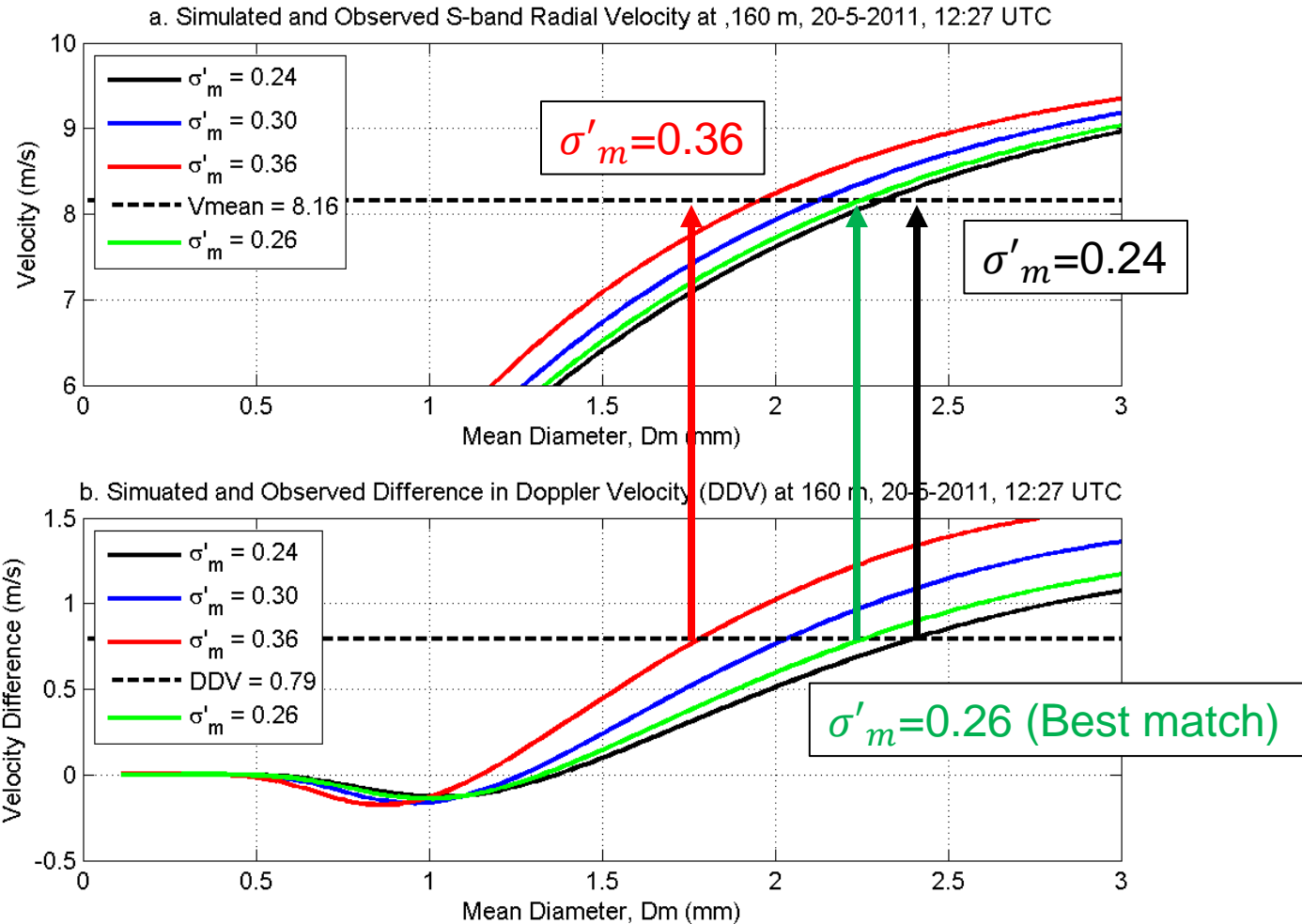


$$DDV = 0.79 \text{ m/s}$$



Step #1: Lowest range gate (160 m)

$V_{measured}^{Sband} = 8.16 \text{ m/s}$



DDV = 0.79 m/s

Retrieval Sequence

Two Measurements:

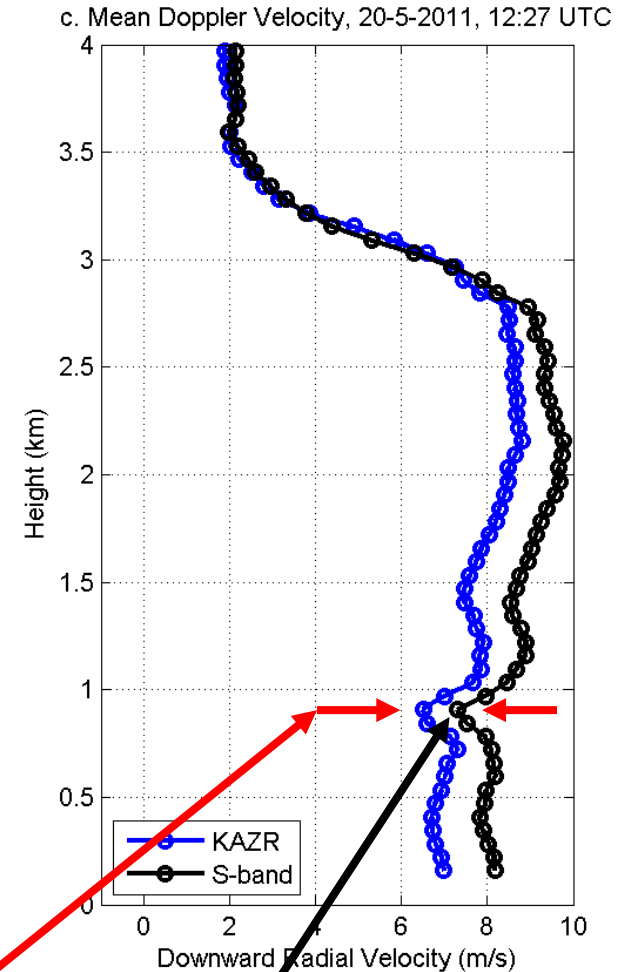
- KAZR Doppler Velocity
- Sband Doppler Velocity

Three Unknowns:

- Air motion (W)
- Mean Diameter (D_m)
- Breadth Parameter (σ'_m)

Assumptions:

- Zero air motion at lowest range gate
- Breadth Parameter constant with ht

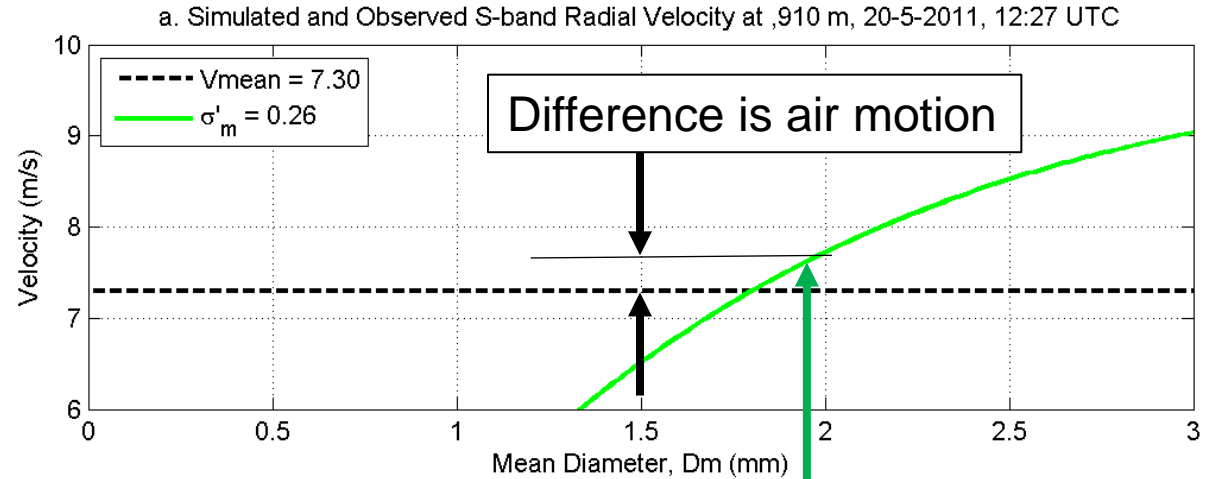


DDV = 0.56 m/s

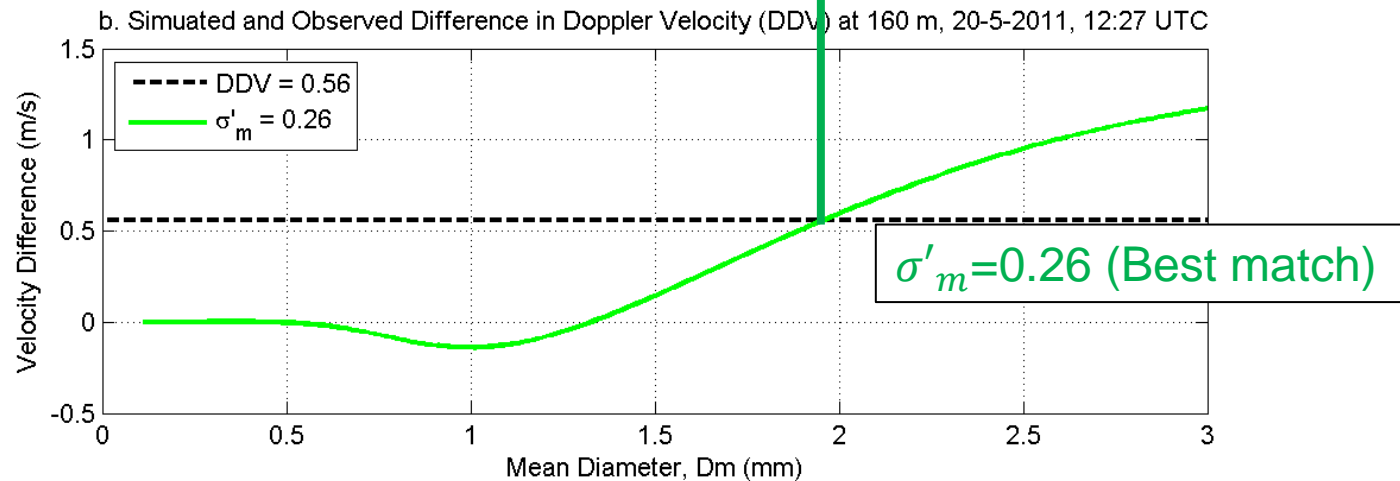
$V_{measured}^{Sband} = 7.3 \text{ m/s}$

Step #1: Lowest range gate

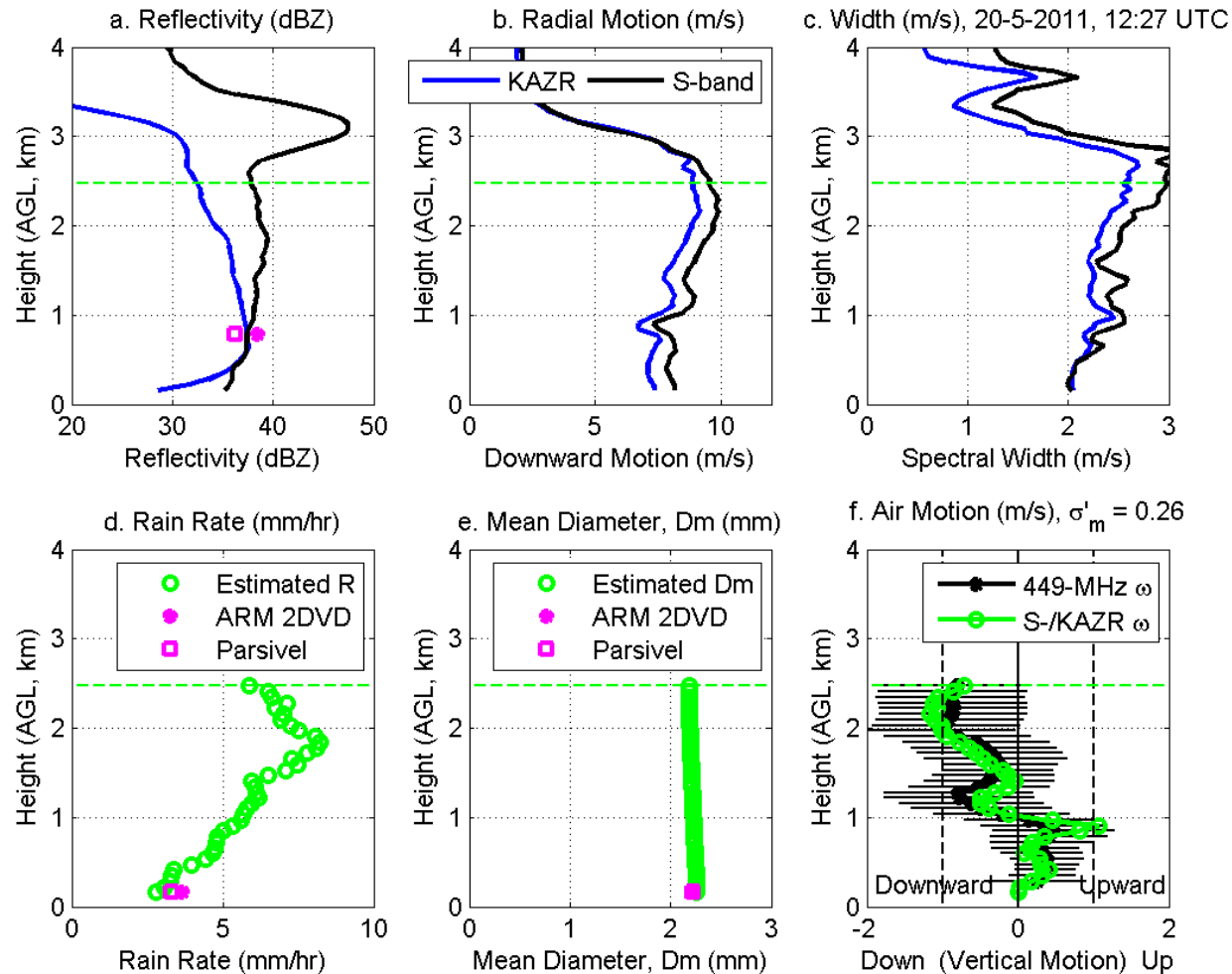
$$V_{measured}^{Sband} = 7.30 \text{ m/s}$$



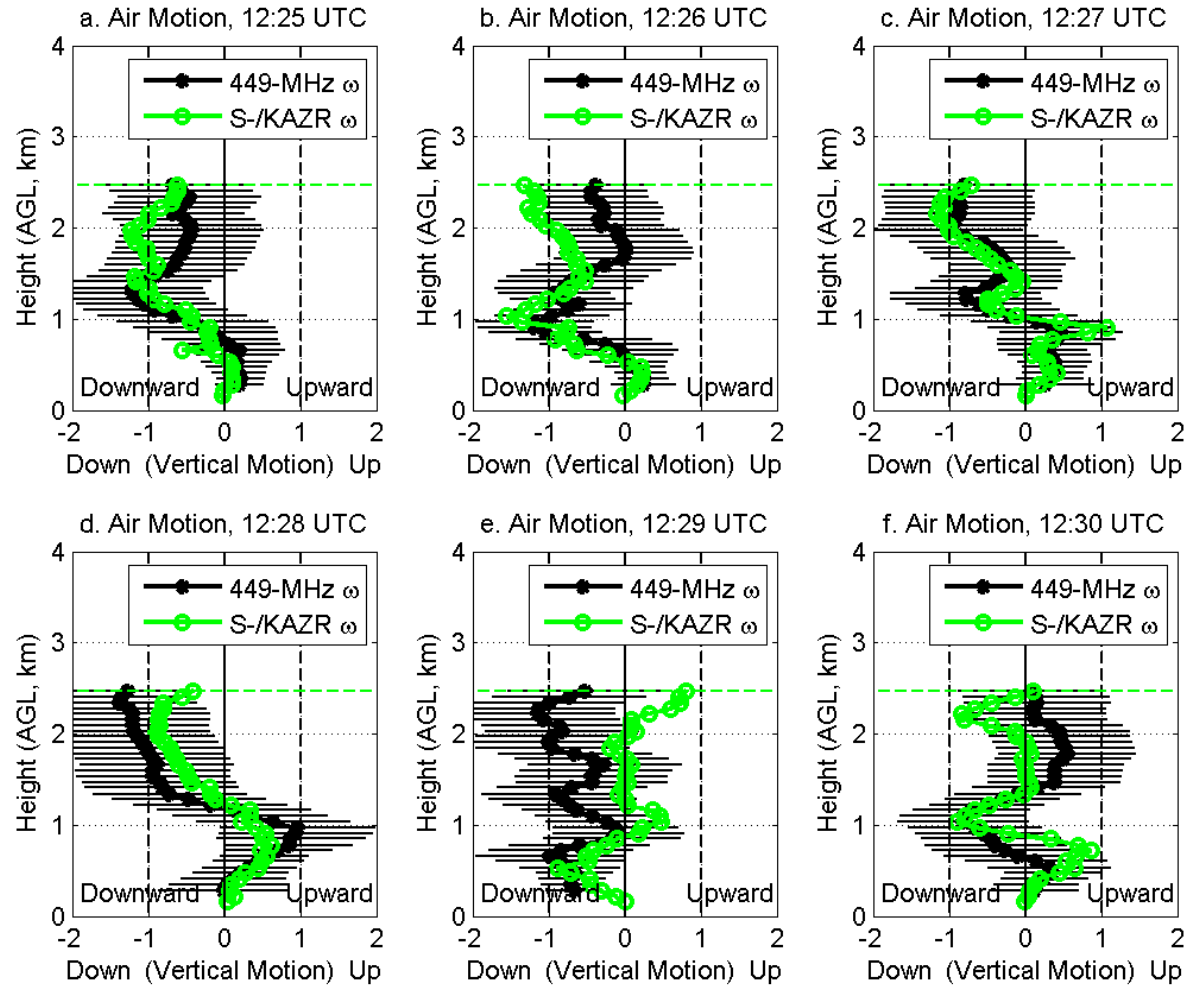
$$DDV = 0.56 \text{ m/s}$$



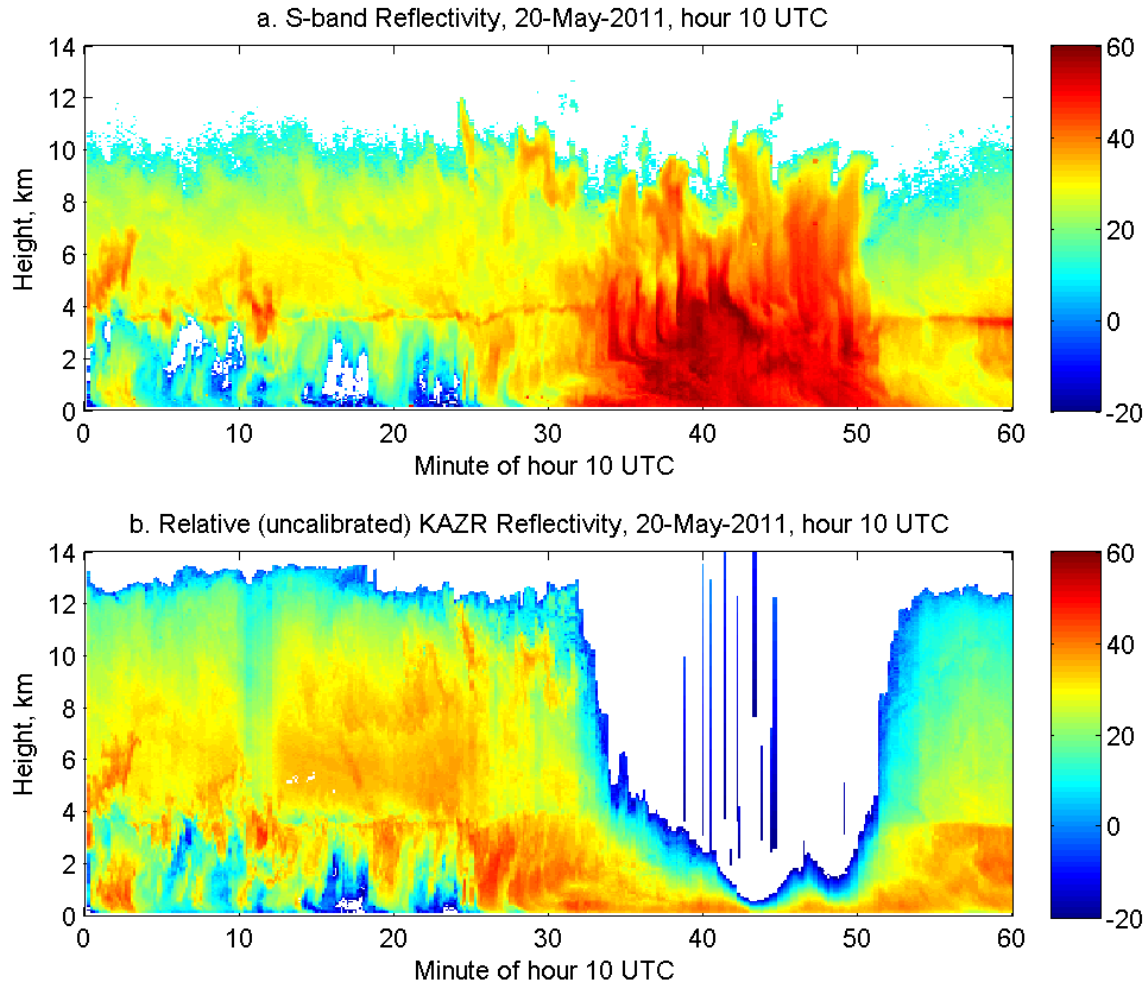
Retrieval at 12:27 UTC



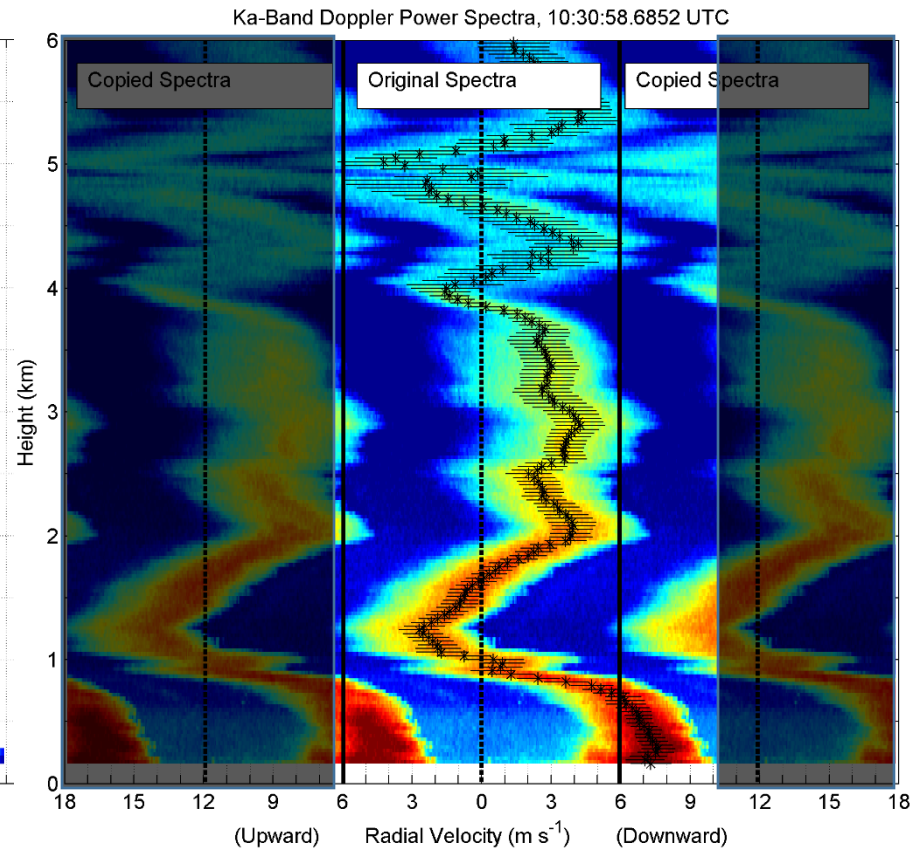
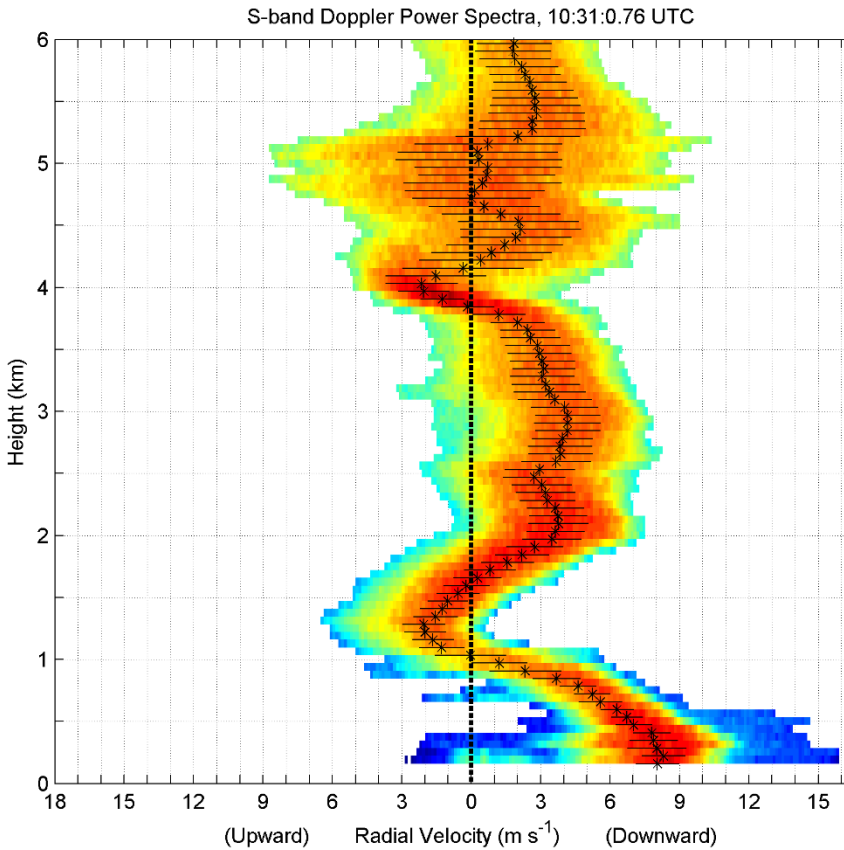
Air motions: 12:25 to 12:30 UTC



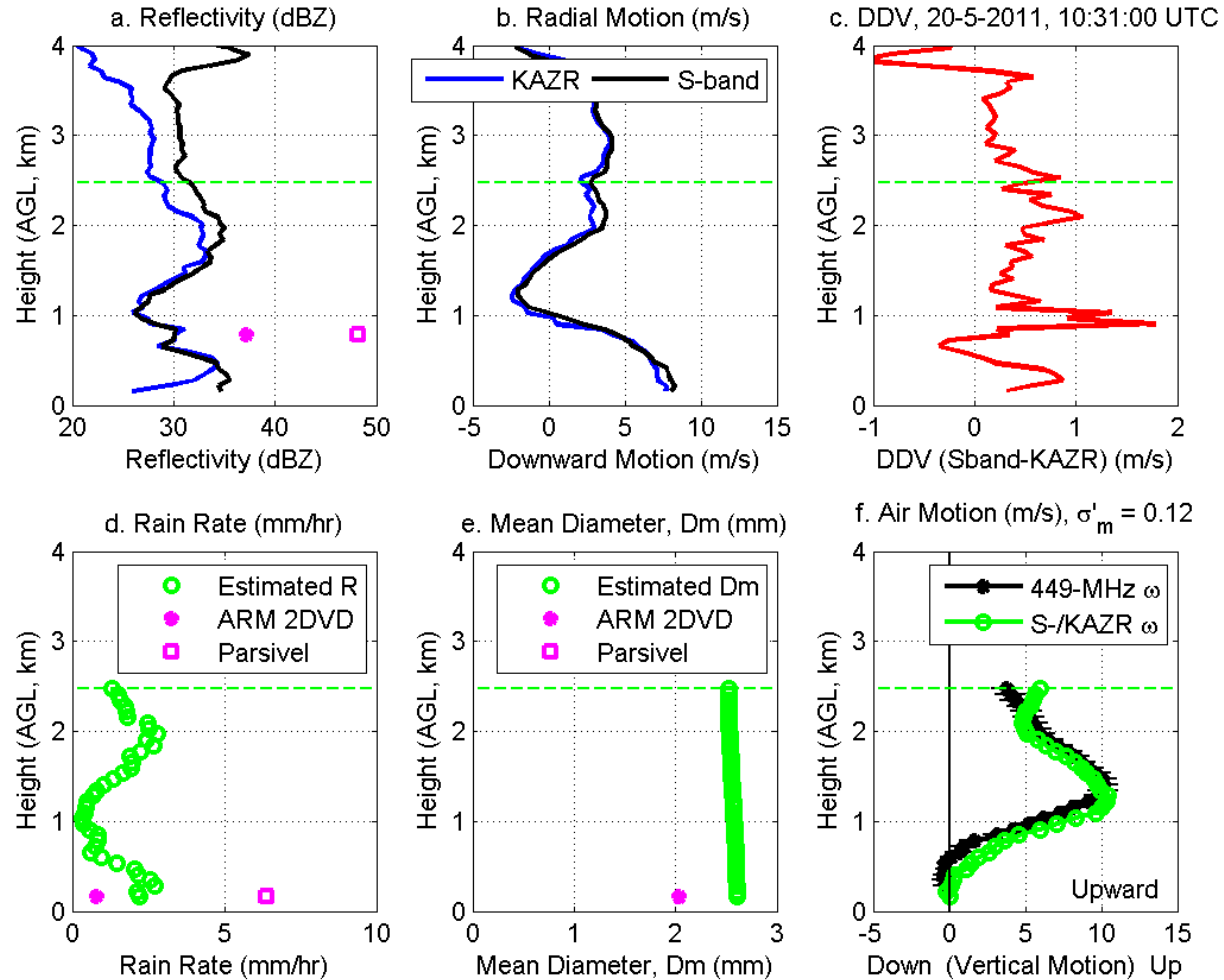
Time-height Cross-Section Z



Spectra at 10:31 UTC



Convective profile, 10:31:00 UTC



Next Steps

1. Convective Rain in rain portion only
Use profiles every 10 seconds
2. UAZR instead of S-band?
FASTER analysis suggests UAZR & S-band moments are very similar (Scott G. & Tami)
3. Produce a PI Product using 2 years of KAZR / UAZR observations at SGP

Backup slides

Huntsville, 2DVD: 21,000 minutes

If we **assume a gamma shape DSD**, there is a relationship between $\sigma_m - D_m - \mu$
(Assume the $D_{max} = \infty$)

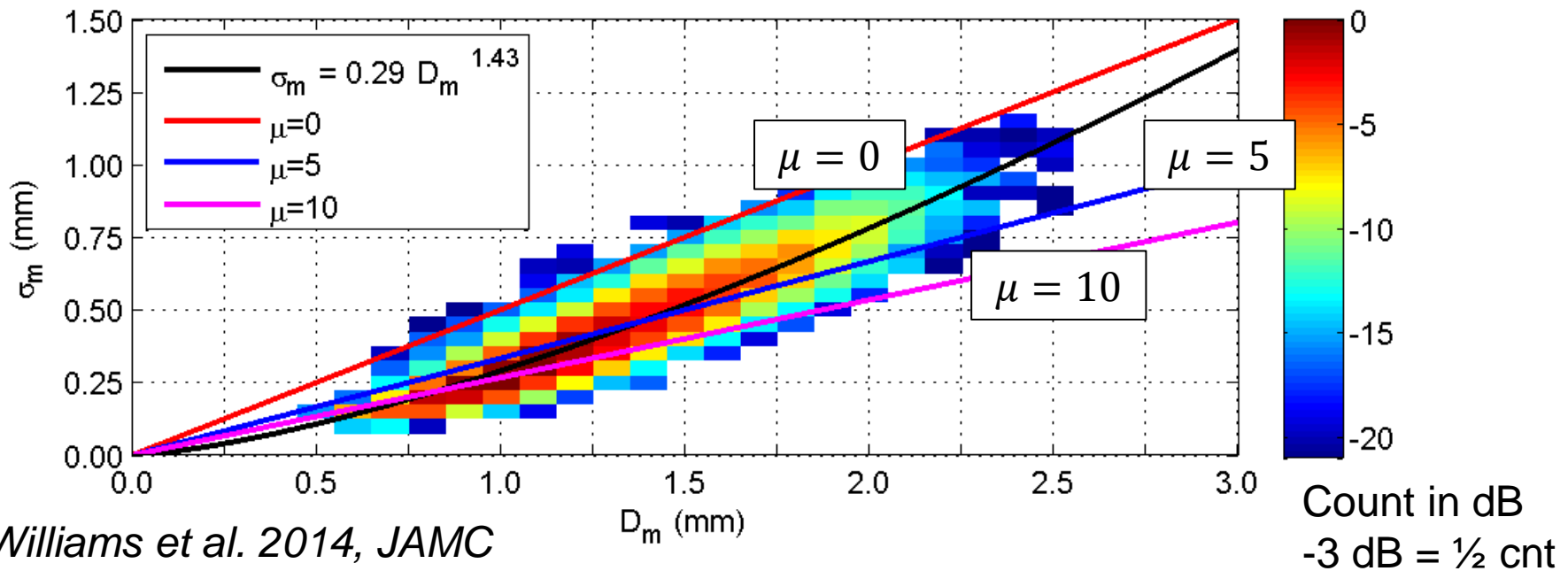
1. Can estimate σ_m from D_m and μ

$$\sigma_m^2 = \frac{D_m^2}{\mu + 4}$$

2. Can estimate μ from D_m and σ_m

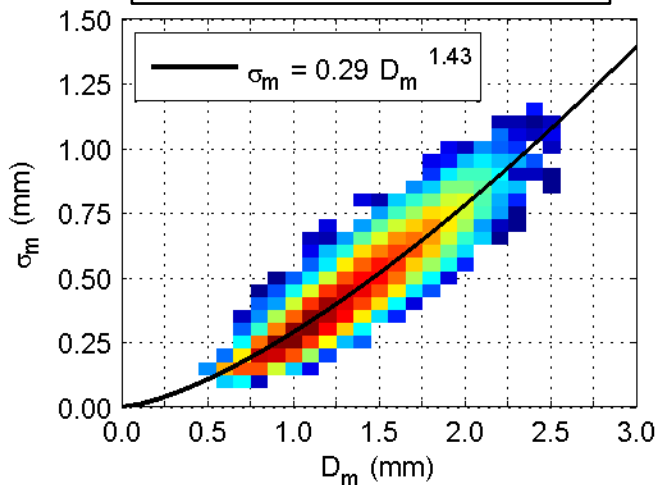
$$\mu = \frac{D_m^2}{\sigma_m^2} - 4$$

a. Huntsville σ_m vs. D_m

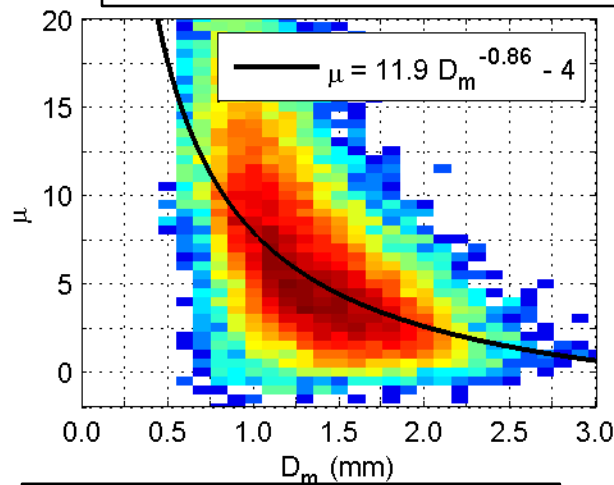


Huntsville 2DVD: 21,000 minutes

Observed σ_m vs. D_m

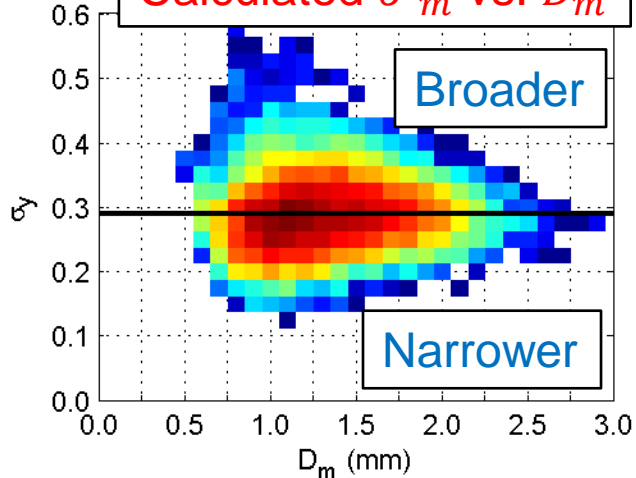


Calculated μ vs. D_m (assume a gamma DSD)

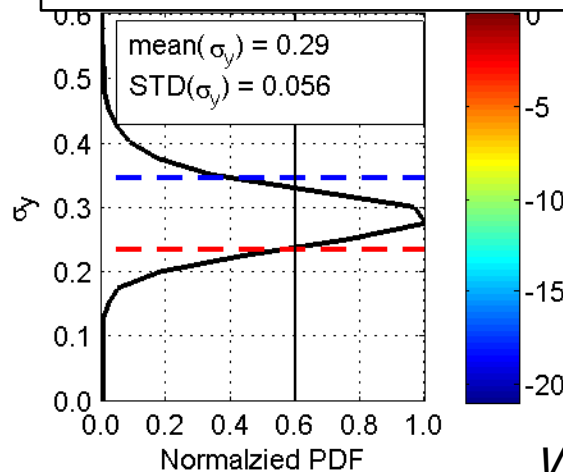


Key attribute:
 σ'_m and D_m
are uncorrelated

Calculated σ'_m vs. D_m



Normalized PDF of σ'_m



74% of observations
are within +/- 1 STD
(a normal distribution
would have 68%)

Difference in Doppler Velocity (DDV)

Mean Doppler Velocities: $V_{measured}^{Sband} = V_{hydro}^{Sband}(D_m, \sigma'_m) - W$

$$V_{measured}^{KAZR} = V_{hydro}^{KAZR}(D_m, \sigma'_m) - W$$

Difference in Doppler Velocities (DDV):

$$DDV = V_{measured}^{Sband} - V_{measured}^{KAZR}$$

$$DDV = V_{Hydro}^{Sband}(D_m, \sigma'_m) - V_{Hydro}^{KAZR}(D_m, \sigma'_m)$$

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