

# Why does deep convection have different sensitivities to temperature perturbations in the lower and upper troposphere?

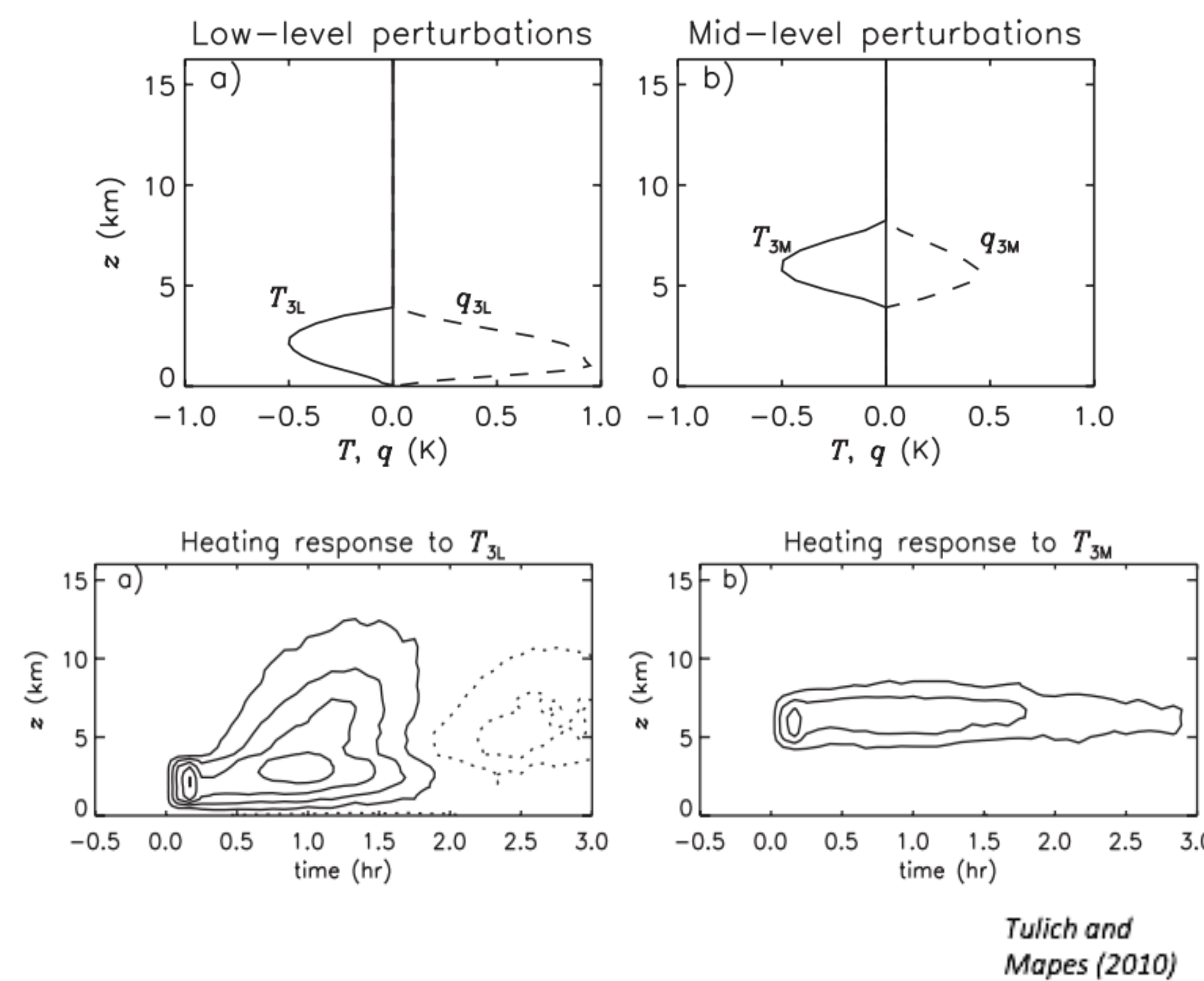


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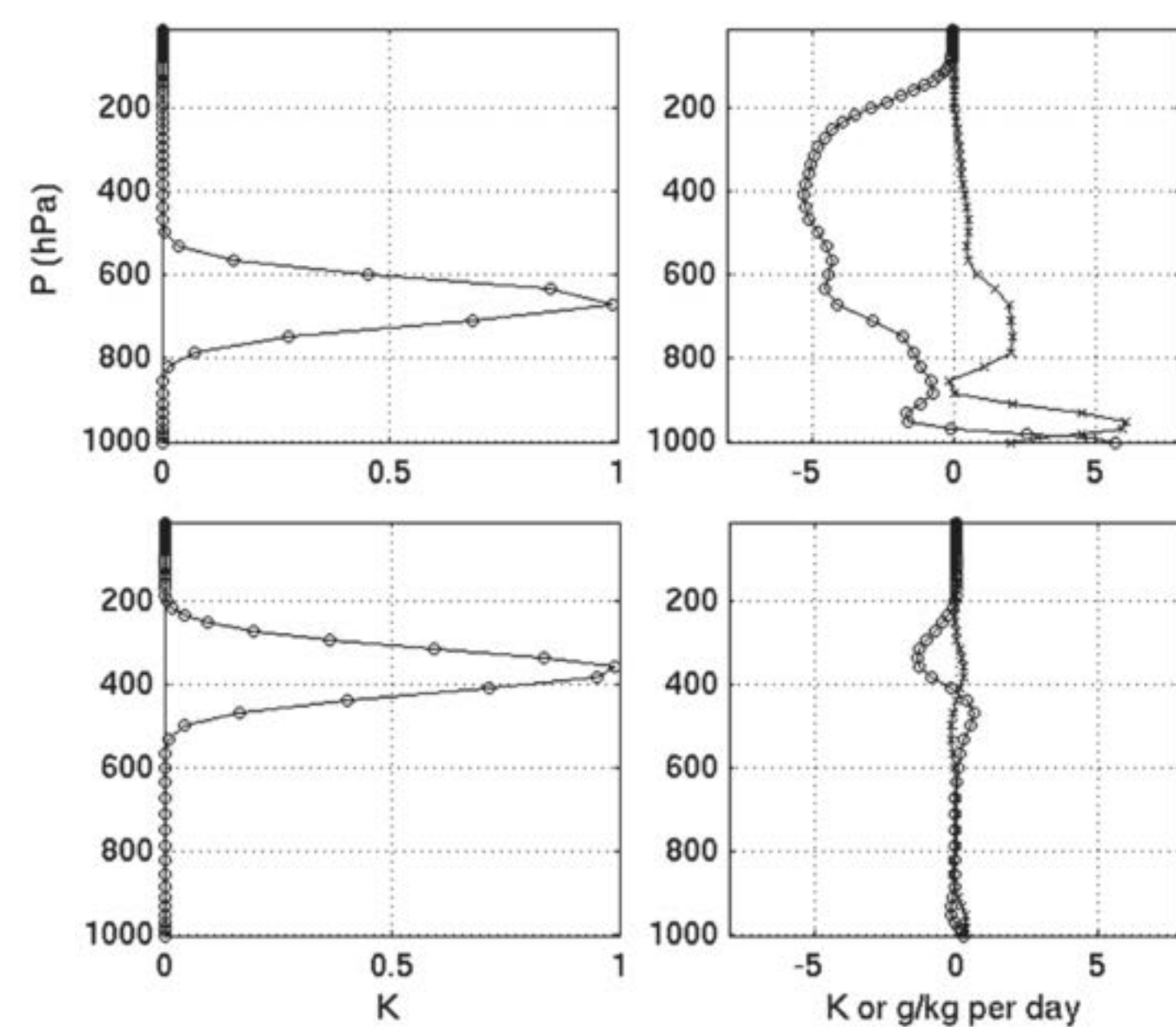
## Introduction

### Motivation

Previous studies have documented that deep convection responds more strongly to above-the-cloud-base temperature perturbations in the lower troposphere than to those in the upper troposphere (Tulich and Mapes 2010, Kuang 2010).



Tulich and Mapes (2010)



Kuang (2010)

### Implications

- Results in a “shallower” convective quasi-equilibrium rather than a full tropospheric quasi-equilibrium
- A stronger lower/middle troposphere convective response leads to wave potential energy generation and wave growth

A mechanistic understanding of what contributes to different sensitivities can help model convectively coupled waves better

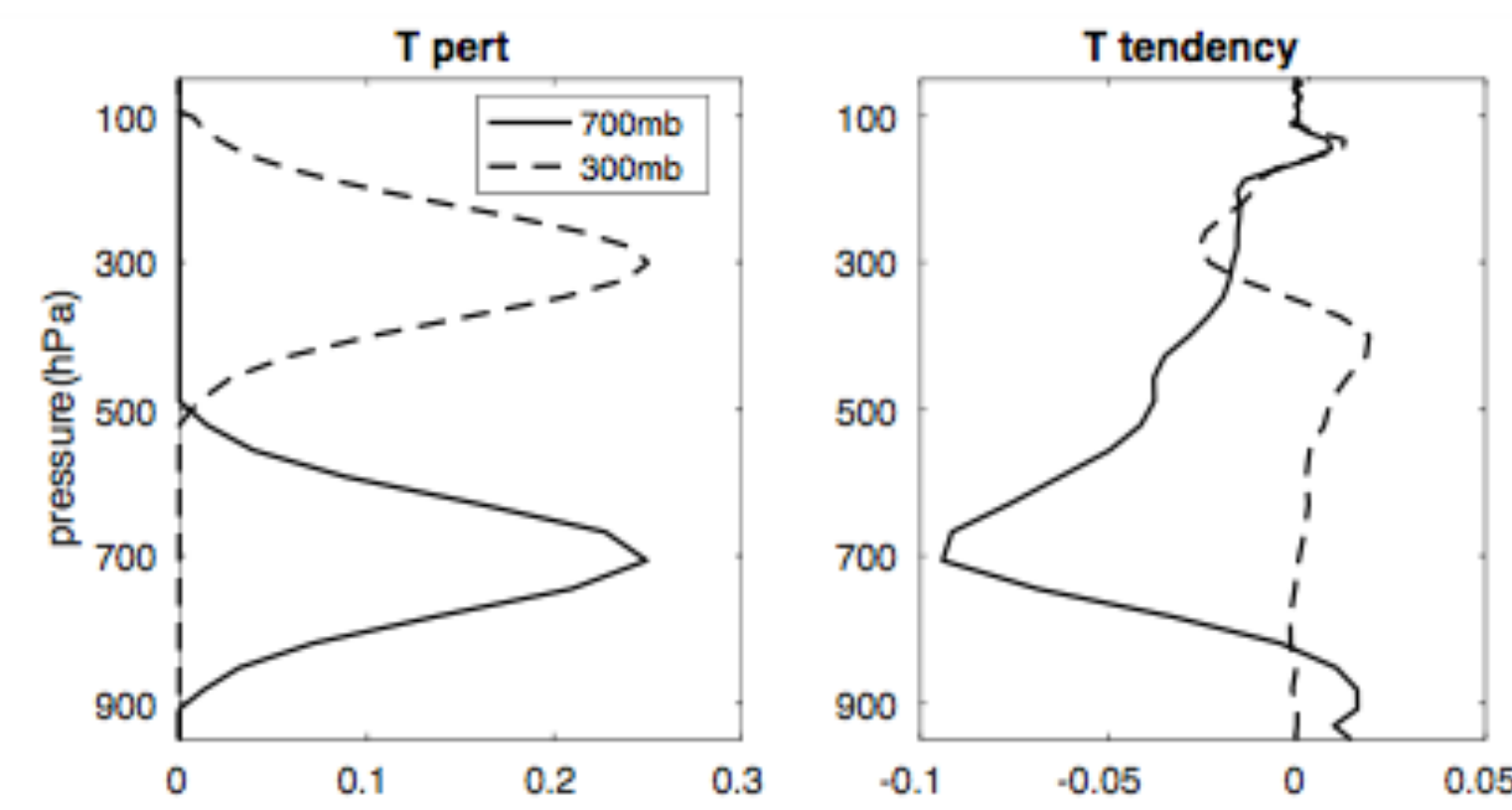
## Model setup

### Hypotheses

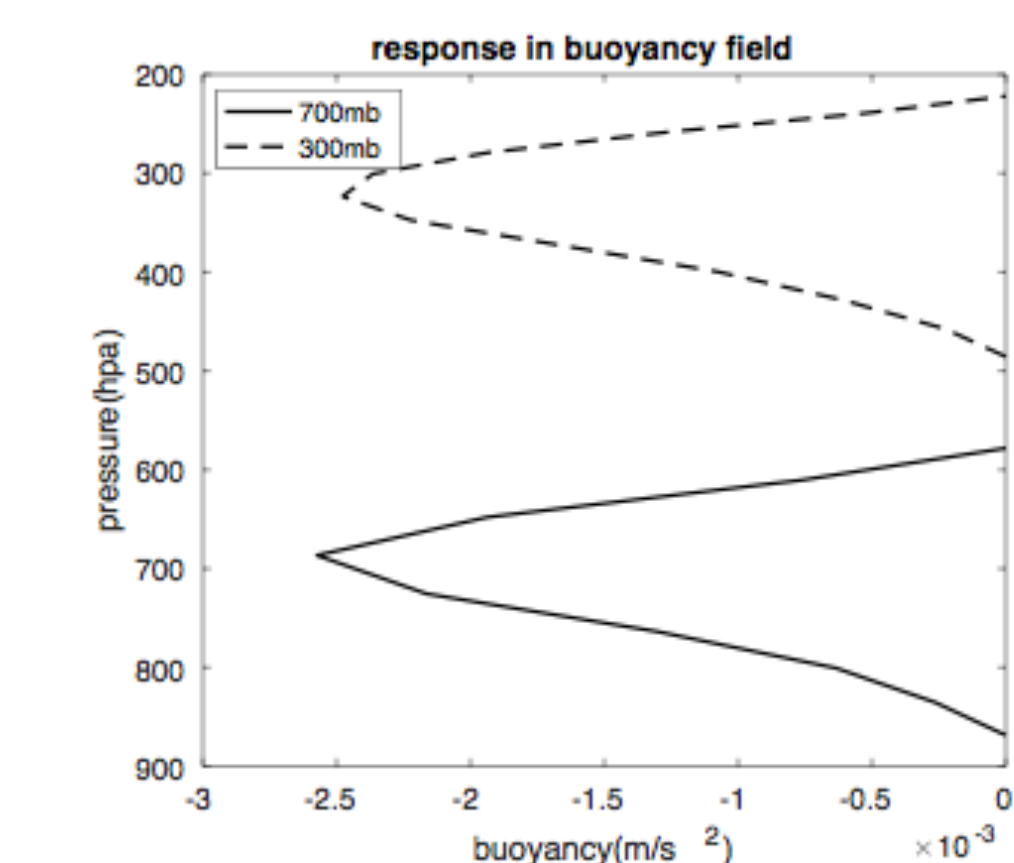
- Liquid water content is limited in the upper troposphere, so is evaporative cooling
- Near-neutral buoyancy in the lower troposphere
- Vertical velocity inertia, velocity increases with height

### Model Configurations

- RCE: Radiative Convective Equilibrium
- SAM: 500m horizontal resolution (128 x 128 km), 10s temporal resolution (2 hours)
- Introduce temperature perturbations at 700 hPa (lower tropo) and 300 hPa (upper tropo): +0.25 K Gaussian-shaped temperature perturbation with 75mb half width
- 100 ensemble runs, each has 8 particle per grid box (~30 million Lagrangian particles)



### Test Hypothesis 1: The amount of liquid water content



$$B = -g(\rho'/\rho) \approx g(T'/T - q_1)$$

T' is the same at the peak perturbation!

Peak buoyancy reduction between 700 hPa(-0.0027) and 300 hPa(-0.0026) is similar, whereas the difference in response is more than 3 times, **condensed water content should not be a controlling factor**

## Results

### Test Hypothesis 2 & 3: Relative importance between vertical velocity and buoyancy acceleration through “swapping”

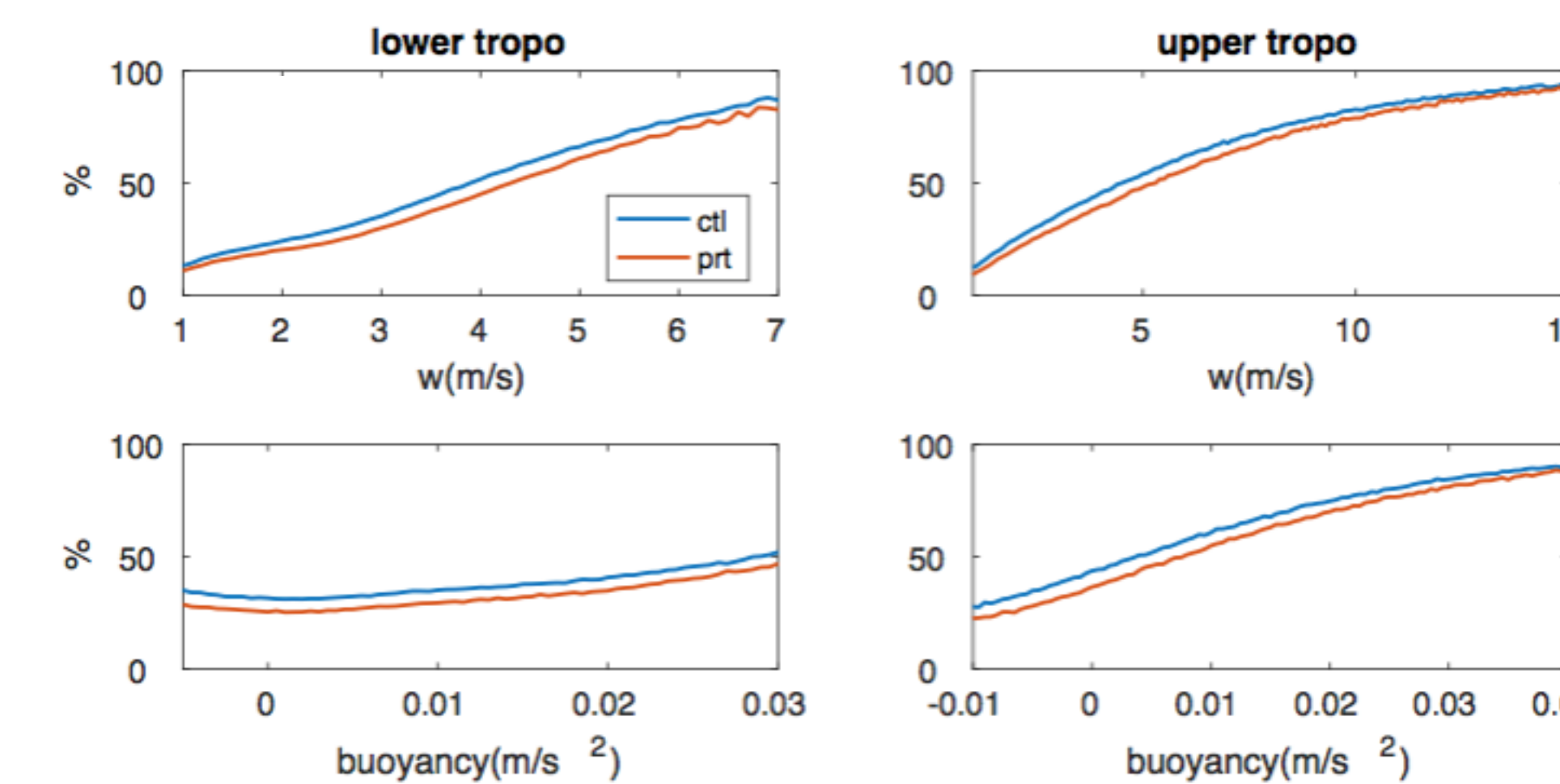
Lagrangian representation of updraft mass flux: counting the number of cloudy parcels that cross a particular interface within a certain time interval.

$$M = \frac{n\delta m}{XY\Delta t} \quad \delta m = \frac{1}{N} \sum_{k=1}^{N_z} \rho_k \Delta z XY$$

Selected two levels instead of a single interface, mass flux is calculated over the entire perturbation.

Upper level: 3000 m (700 hPa); 9400 m (300 hPa)  
Lower level: 1400 m (700 hPa); 7300 m (300 hPa)

From here we can calculate the percentage of particles that can successfully cross the perturbation layer, defined as crossing percentage.



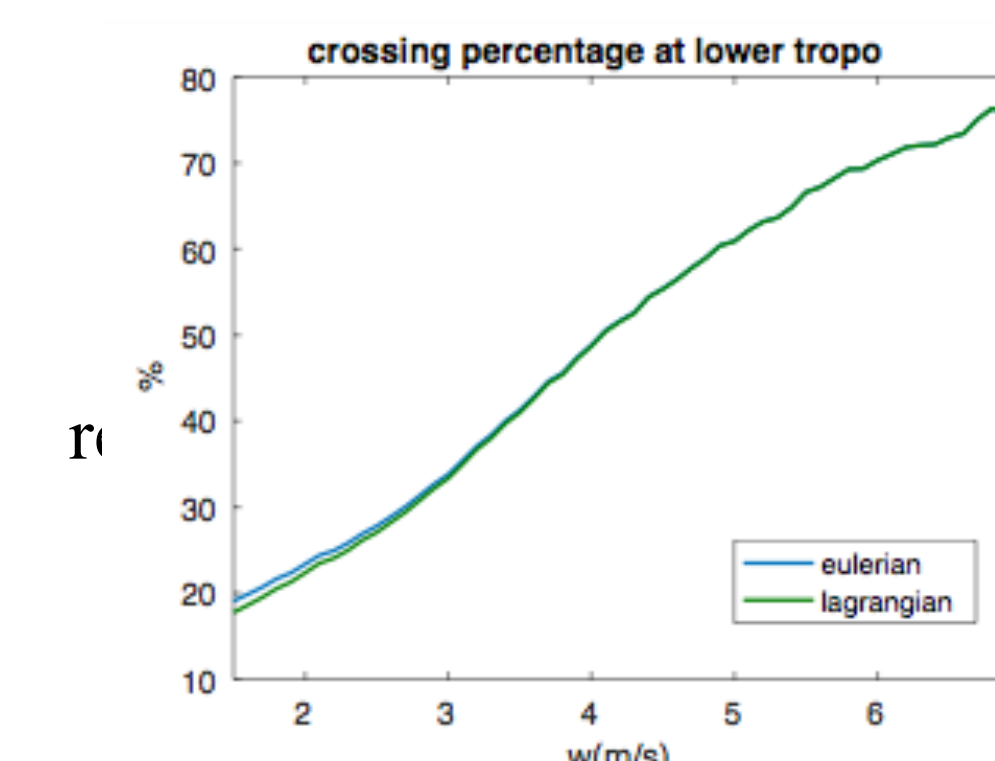
### Weaker dependence on initial buoyancy in the lower troposphere

Sub-grid scale diffusion term is small in the height range we consider, we can accurately compute how a parcel's vertical velocity and position evolve using buoyancy and vertical pressure gradient accelerations.

$$z(t) = z_{\text{bottom}} + \int_{t_{\text{bottom}}}^t w(t') dt' \quad (1)$$

$$\frac{1}{2} w^2(z) = \frac{1}{2} w^2(z_{\text{bottom}}) + \int_{z_{\text{bottom}}}^z F(x(z'), y(z'), z') dz' \quad (2)$$

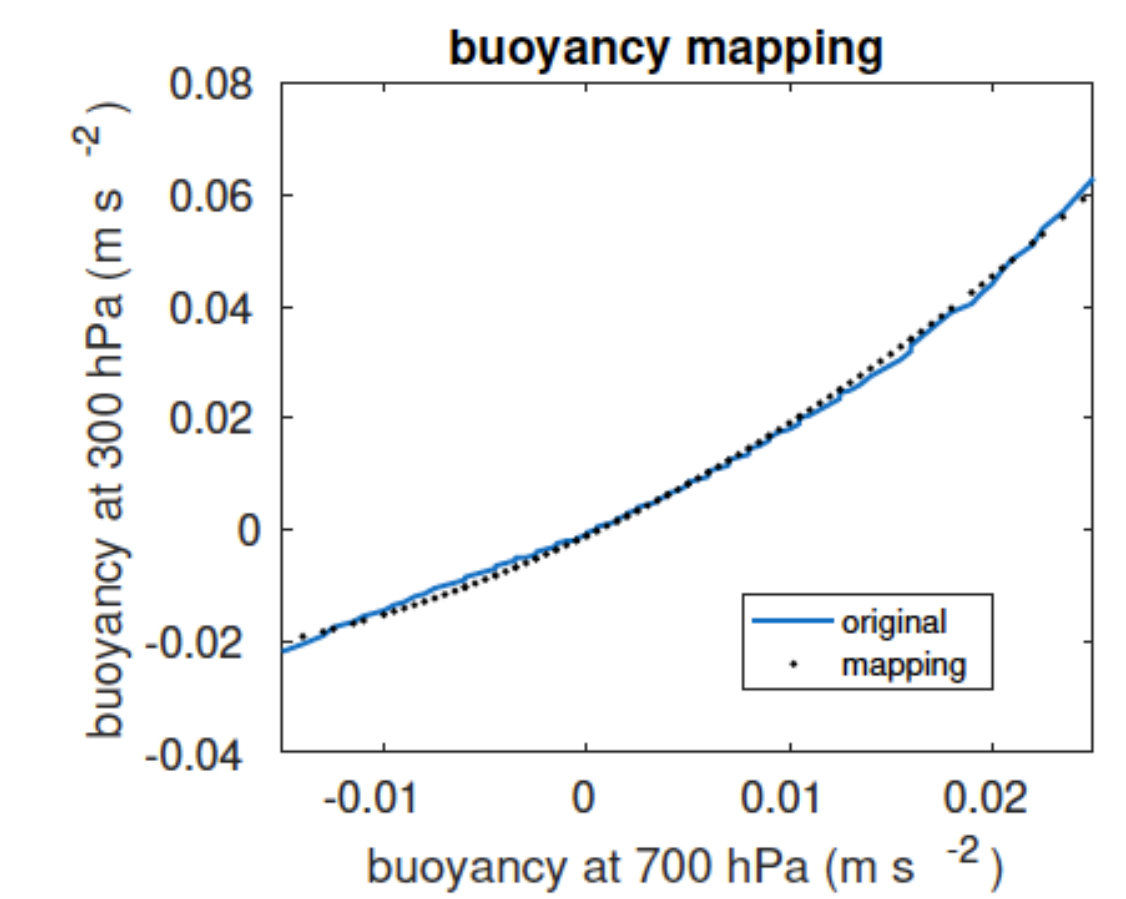
$$F(x(z), y(z), z) = B(x(z), y(z), z) - \frac{dp'_b}{\rho dz}(x(z), y(z), z) - \frac{dp'_{\text{m}}}{\rho dz}(x(z), y(z), z) \quad (3)$$



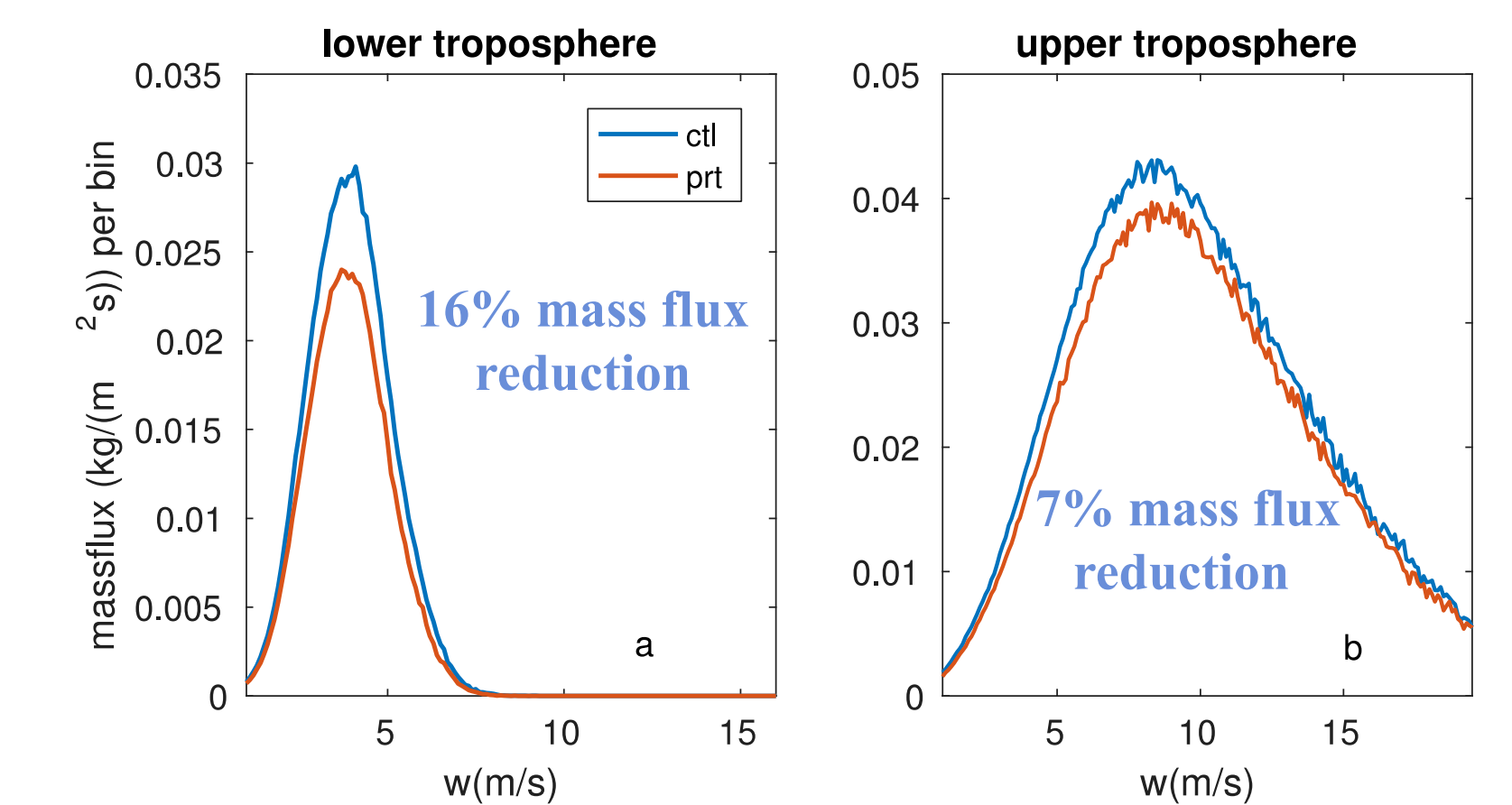
Using Eq. (1)-(3) to

crossing percentage, agrees well with model direct output.

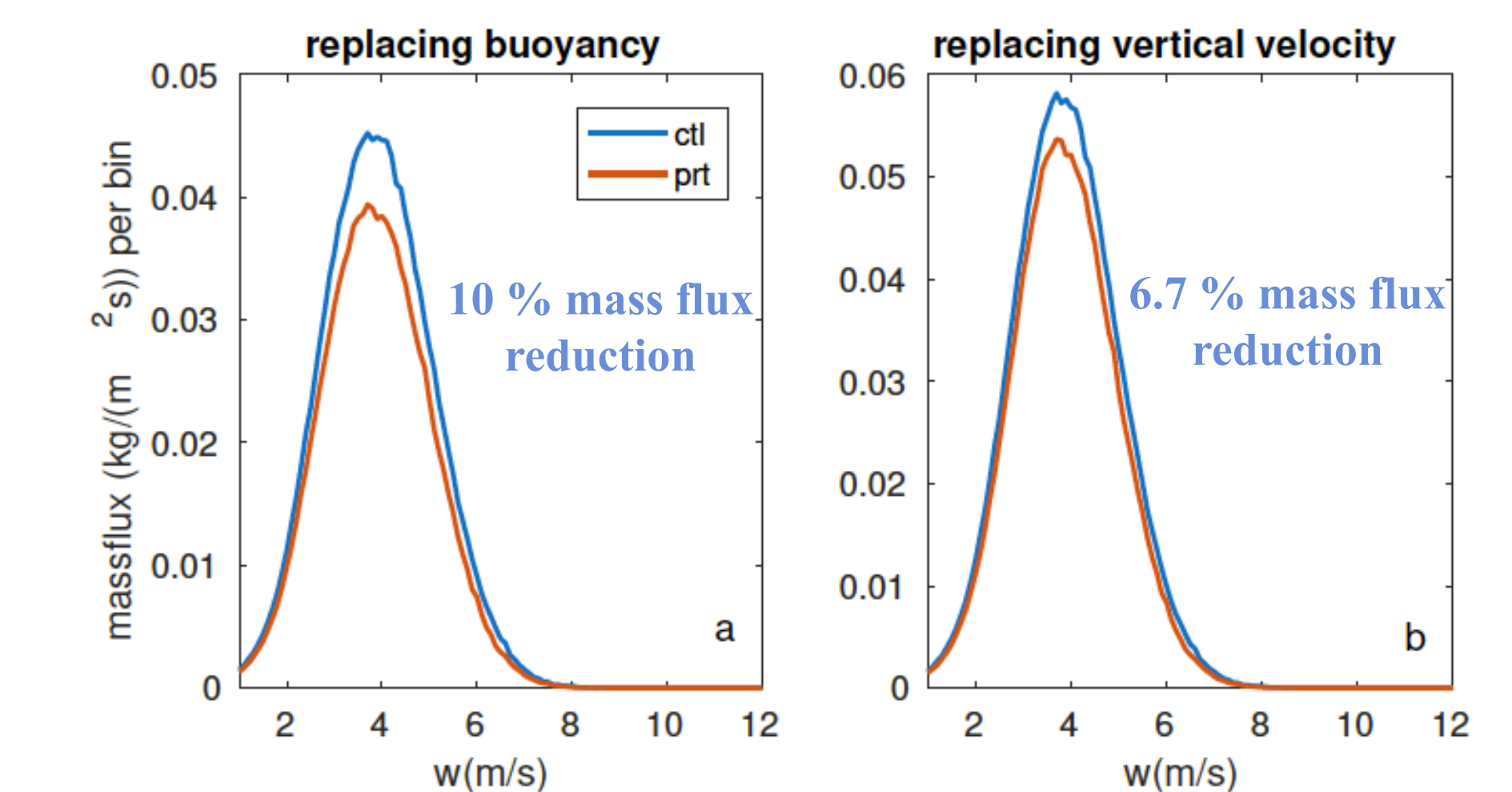
To quantify the effect of the initial vertical velocity, we can, for example, solve Eqs. (1-3) for the 700 hPa case, but with the initial vertical velocity from the 300 hPa case. This is done through non-linear mapping:



Before swapping:



After swapping (lower troposphere):



## Conclusions

- Total water content difference plays a secondary role
- Both vertical velocity and buoyancy play important roles in determining the different convective sensitivity, but velocity is a bit more important than the buoyancy
- Vertical velocity should be included for parameterization to account for correct convective sensitivity

- Kuang, Z. (2010), Linear response functions of a cumulus ensemble to temperature and moisture perturbations and implication to the dynamics of convectively coupled waves., *J. Atmos. Sci.*, 67, 941-962.
- Tulich, S. and B. E. Mapes, Transient environmental sensitivities of explicitly simulated tropical convection. *J. Atmos. Sci.*, 697, 923-940.